



# Network Survivability Modeling and Quantification



Prof. Poul E. Heegaard,  
[poul.heegaard@item.ntnu.no](mailto:poul.heegaard@item.ntnu.no)  
Department of Telematics  
Norwegian University of Science and Technology (NTNU)



Prof. Kishor S. Trivedi  
[kst@ee.duke.edu](mailto:kst@ee.duke.edu)  
Elect. & Comp. Eng. Dept.,  
Pratt School of Engineering  
Duke University



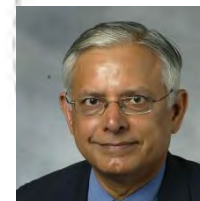
# NTNU, Trondheim, Norway (A), Duke University, Durham, NC (B)



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## Kishor S. Trivedi

### Pratt School of Engineering, Duke University



Kishor S. Trivedi holds the Hudson Chair in the Department of Electrical and Computer Engineering at Duke University, Durham, NC. He has been on the Duke faculty since 1975. He is the author of a well known text entitled, Probability and Statistics with Reliability, Queuing and Computer Science Applications, published by Prentice-Hall; a thoroughly revised second edition (including its Indian edition) of this book has been published by John Wiley. He has also published two other books entitled, Performance and Reliability Analysis of Computer Systems, published by Kluwer Academic Publishers and Queueing Networks and Markov Chains, John Wiley. He is a Fellow of the Institute of Electrical and Electronics Engineers. He is a Golden Core Member of IEEE Computer Society. He has published over 420 articles and has supervised 42 Ph.D. dissertations. He is the recipient of IEEE Computer Society Technical Achievement Award for his research on Software Aging and Rejuvenation. His research interests in are in reliability, availability, performance, performability, security and survivability evaluation of computer and communication systems. He works closely with industry in carrying our reliability/availability analysis, providing short courses on reliability, availability, performability modeling and in the development and dissemination of software packages such as SHARPE and SPNP.



Norwegian University of  
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## Poul E. Heegaard, Norwegian University of Science and Technology



Poul E. Heegaard is Associate Professor and Head of Department at Department of Telematics, Norwegian University of Science and Technology (NTNU). Heegaard has since 2006 been on the faculty at NTNU. From 1999 - 2009 he was a Senior Research Scientist at Telenor R&I. He has previously been a Research Scientist and Senior Scientist at SINTEF Telecom and Informatics (1989-1999). His research interests cover performance, dependability and survivability evaluation and management of communication systems. Special interest is in rare event simulation techniques, and monitoring, routing and management in dynamic networks. He has developed a Java-based traffic generator called [GenSyn](#). His current research focus is on distributed, autonomous and adaptive management and routing in communication networks and services. Heegaard has been active in several EU-IST collaborations.

Heegaard is the author/co-author of a number of research papers, reports and lecture notes. He has given numerous talks in national and international meetings and conferences. He serves in various international organization committees such as General Chair for [RESIM 2012](#), and program committees, such as Dependable Systems and Networks (DSN) 2011. He is frequently an expert reviewer for different journals and PhD committees.





# Summary of tutorial

Critical services in a telecommunication network should be continuously provided even when undesirable events like sabotage, natural disasters, or network failures happen. It is essential to provide virtual connections between peering nodes with certain performance guarantees such as minimum throughput, maximum delay or loss. The design, construction and management of virtual connections, network infrastructures and service platforms aim at meeting such requirements.

In this tutorial we consider the network's ability to survive major and minor failures in network infrastructure and service platforms that are caused by undesired events that might be external or internal. Survive means that the services provided comply with the requirement also in presence of failures. The network survivability is quantified as defined by the ANSI T1A1.2 committee -- that is, the transient performance from the instant an undesirable event occurs until steady state with an acceptable performance level is attained.

The goal of this tutorial is to provide an introduction to the concept and definition of survivability and to demonstrate approaches to model and quantify the survivability in networks. Examples are taken from the survivability of virtual connection over an IP network.





# Tutorial outline

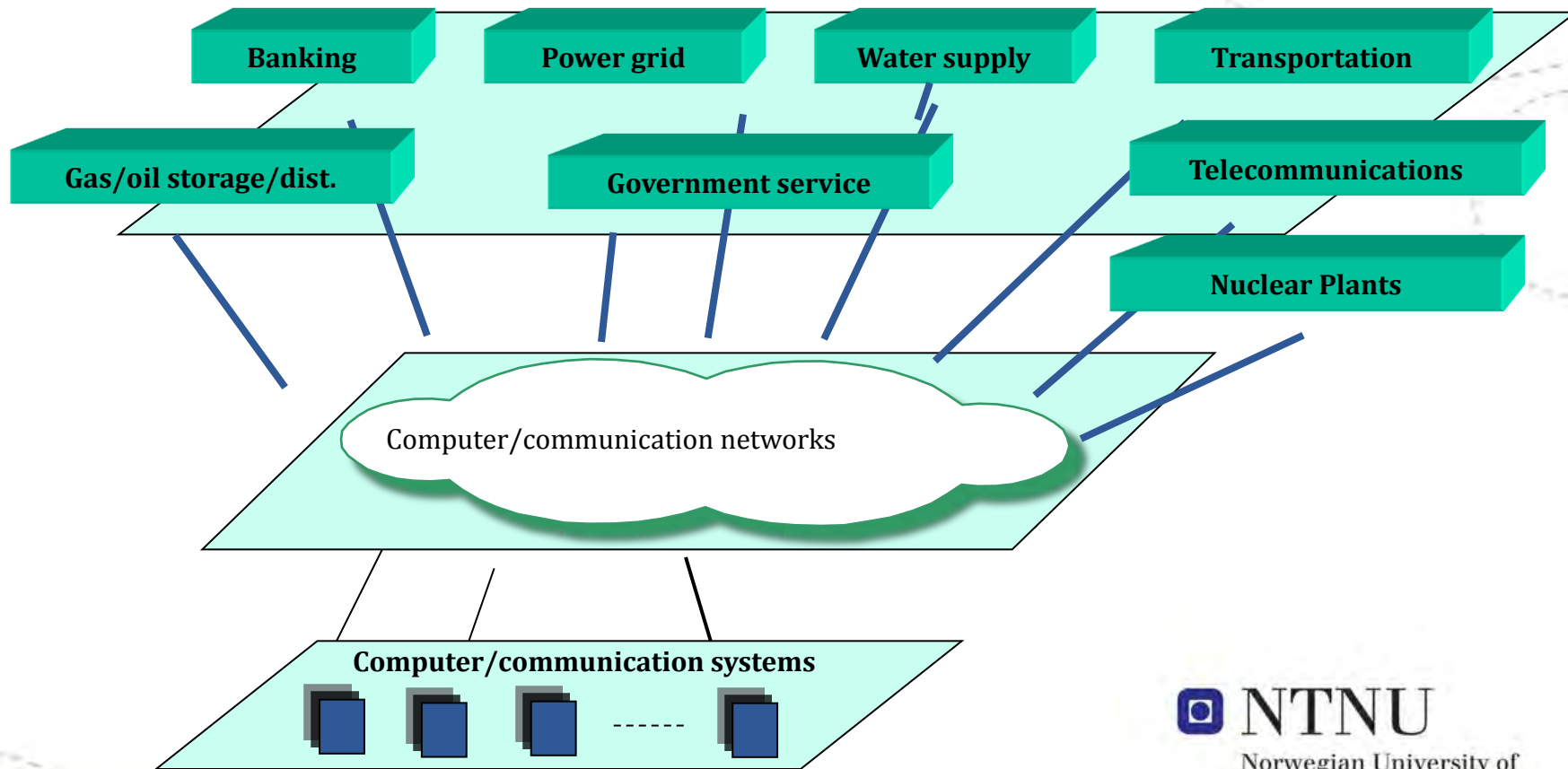
- I. Survivability concepts and definition
- II. Network survivability modeling and quantification
- III. Case studies





# What needs to be survivable?

Critical national infrastructure





# Why survivability?

- Society heavily depends on telecommunication services
- Critical services must be available even under
  - Technical network failures
  - Malicious attack
  - Accidents and natural disasters
- Security, dependability, survivability, availability, reliability...
  - All concerned with trusted services according its requirements
- Differ in their main focus on threats
  - Dependability: physical, design, and interactions
  - Security: recognition and resistance to attacks
  - Survivability: attack, accidents, and failures







# I. Survivability concepts and definitions



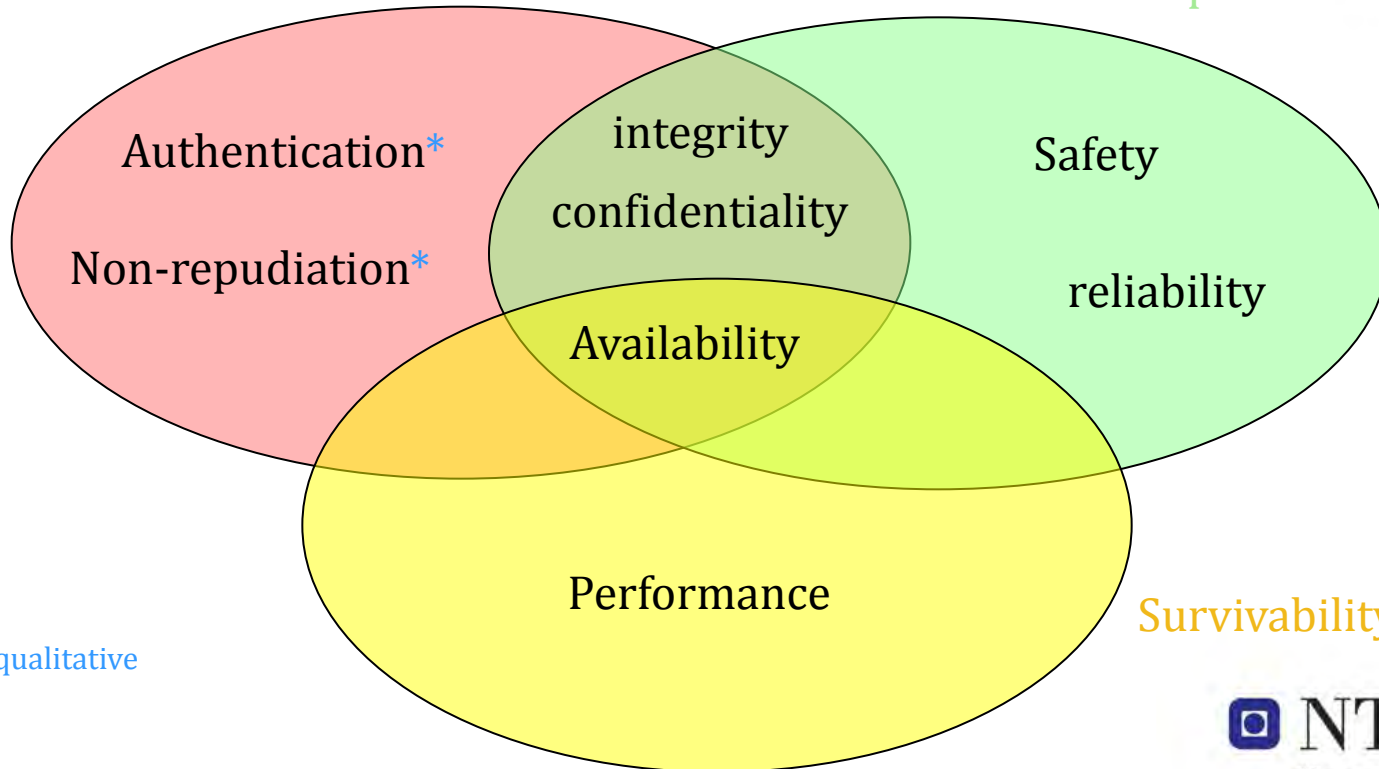
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# Our View on Survivability, Performance, Dependability, and Security<sup>10/140</sup>



Security

Dependability



\*: qualitative

Survivability

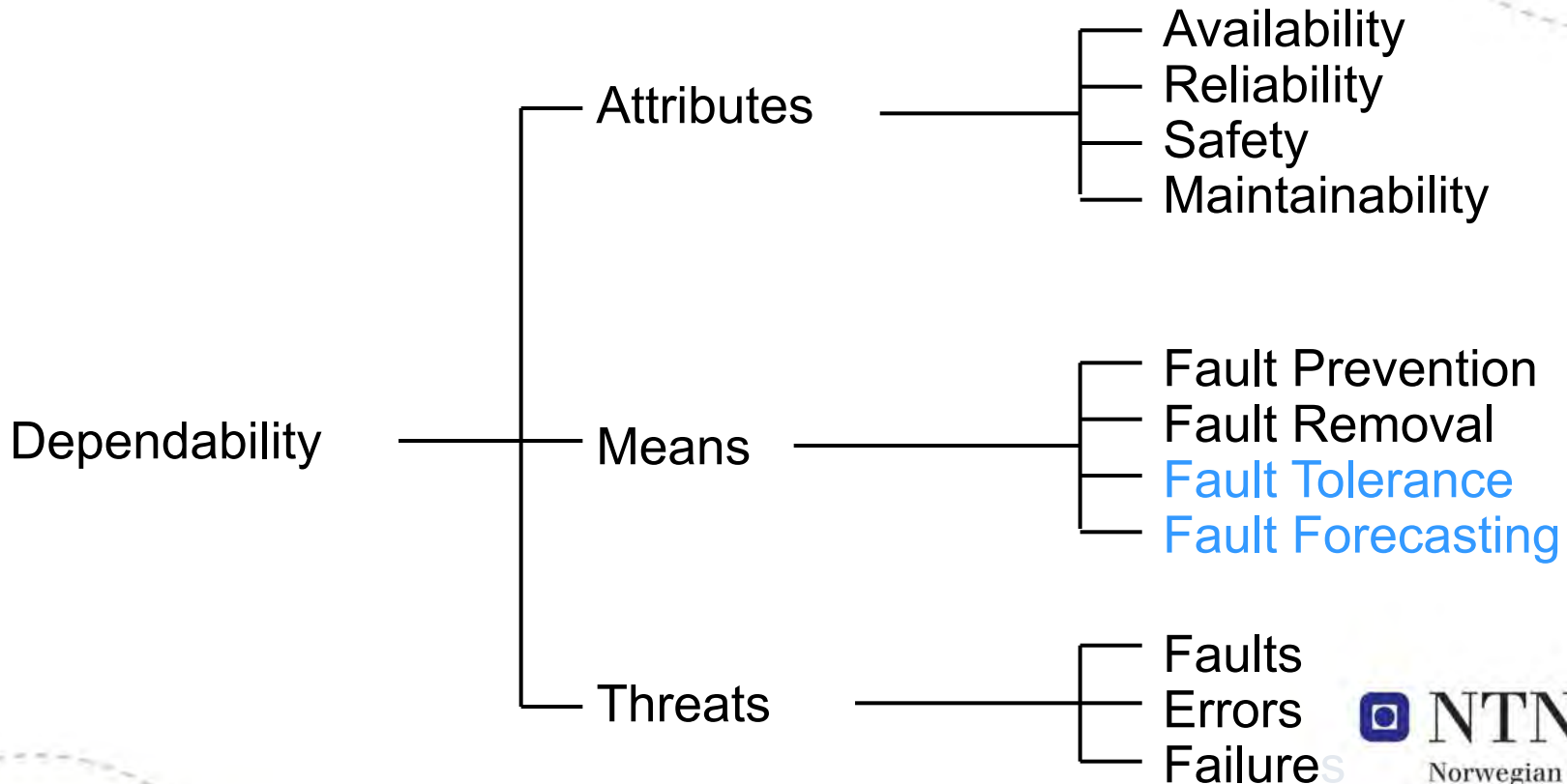
Performance + Availability/Reliability = Performability



# Dependability- An umbrella term



- Trustworthiness of a computer system such that reliance can justifiably be placed on the service it delivers



# MEASURES TO BE EVALUATED



- Dependability
  - Reliability:  $R(t)$ , System MTTF
  - Availability: Steady-state, Transient, Interval
  - Downtime
  - Security, safety

“Does it work, and for how long?”

- Pure (Failure Free) Performance
  - Throughput, Blocking Probability, Response Time (mean, distribution)

“Given that it works, how well does it work?”



# MEASURES TO BE EVALUATED



- Composite Performance and Dependability

“How much work will be done(lost) in a given interval including the effects of failure/repair/contention?”



# Dependability Attributes or Measures

## Dependability Measures

**Reliability**

**Availability**

- **Reliability:** *“The ability of a system to perform a required function under given conditions for a given time interval.”* No recovery is assumed after **system** fails (there can be recovery after a component failure)
- **Availability:** *“The ability of a system to be in a state to perform a required function at a given instant of time or at any instant of time within a given time interval.”*





# IFIP WG10.4

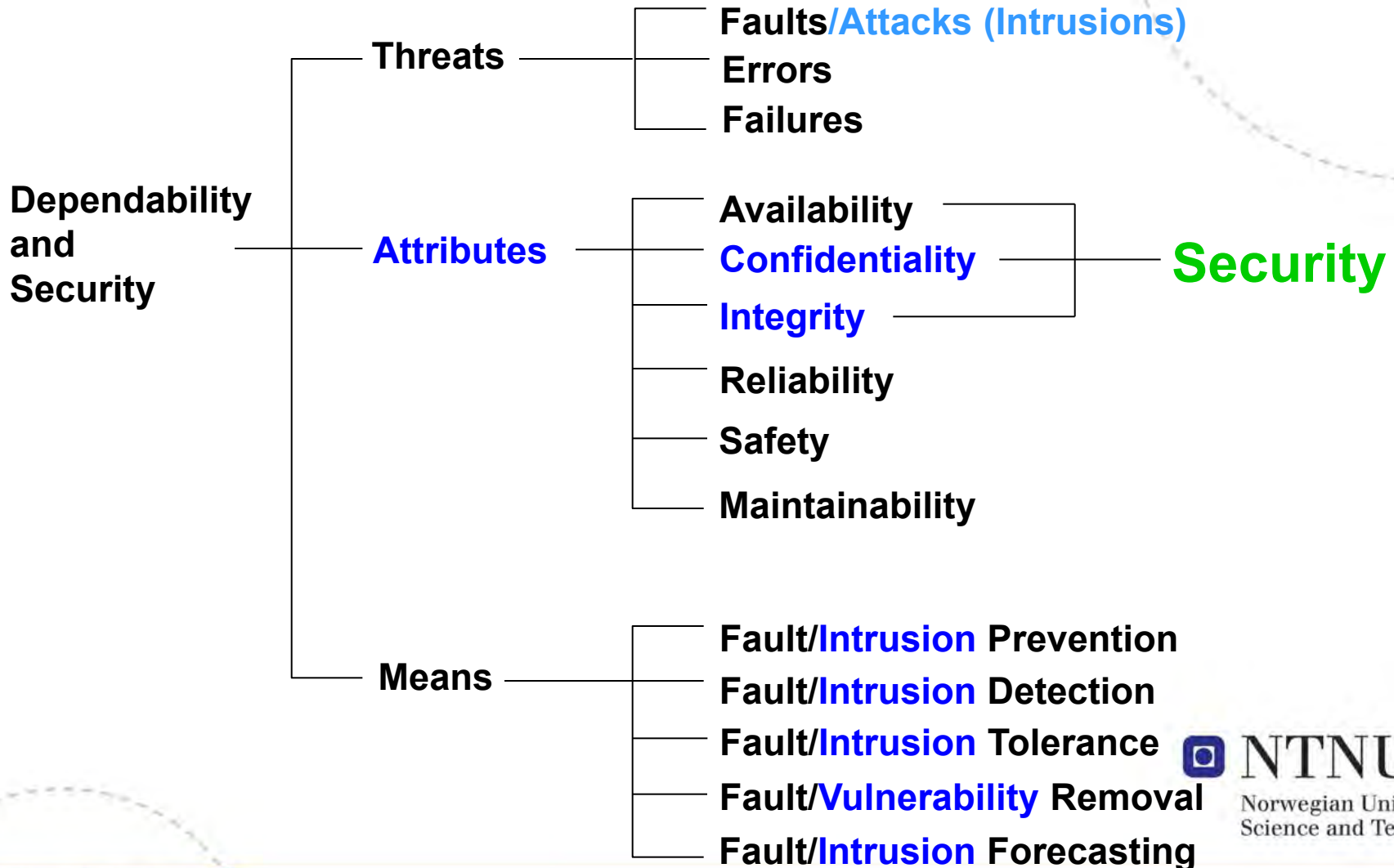


- **Failure** occurs when the delivered service no longer complies with the desired output.
- **Error** is that part of the system state which is liable to lead to subsequent failure.
- **Fault** is adjudged or hypothesized cause of an error.

**Faults** are the cause of **errors** that may lead to **failures**



# Extended Dependability and Security tree





# Survive What?

- Hardware/software faults
  - Programming bugs, hardware failure
- Man-made accidents
  - Cable cuts, operator errors
- Malicious cyber attacks
  - Denial of service, virus/spyware/rogueware
- Natural disasters
  - Fire, flood, earthquake, hurricane
- Terrorist attacks



# Survivability Principles

- **Decentralization**
  - Provide service without reliance on a common reference node in the architecture
- **Redundancy**
  - Provide service by switching (failing) over workload of the affected node(s) or link(s) to standby (backup) node(s) or link(s)
- **Geographic Separation (Diversity)**
  - Placement of standby nodes or links outside of the expected radius of damage of related nodes or links





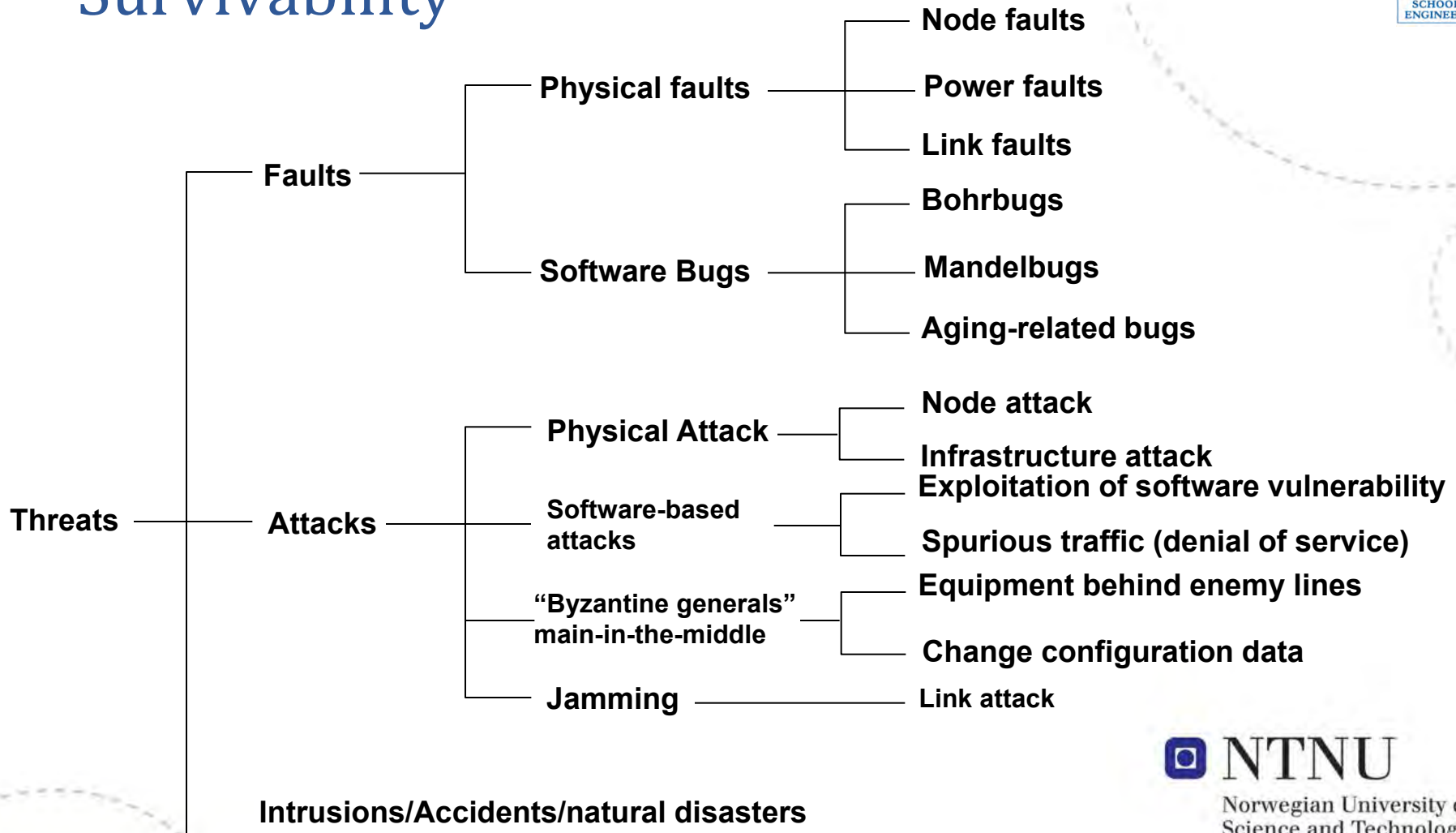
# What Is Survivability?

- **Reliability**
  - Continuity of service, how long will the system work w/o system failure (component failures are allowed)
- **Availability**
  - Readiness of service, how frequently it fails and how quickly can it be repaired
- **Performability**
  - performance in the presence of failure
- **Safety**
  - Avoiding catastrophic consequences (human life)
- **Confidentiality**
  - Preventing unauthorized disclosure
- **Integrity**
  - Preventing improper alteration
- **Survivability**
  - ?





# Threats in Dependability, Security and Survivability







# Survivability, Security, and Fault Tolerance

- Survivability vs. Security
  - Security
    - Availability, confidentiality and integrity
    - Recognition of attacks, resistance to attacks
  - Survivability
    - Broader than security
    - Maintain essential service and recover under attacks and natural disasters
- Survivability vs. Fault Tolerance
  - Fault tolerance does not (normally) consider malicious attacks (Intrusion Tolerance does) and natural disasters
  - Geographic diversity in survivable systems needed to avoid vulnerabilities to massive attacks or disasters

[3] R.J. Ellison, D.A. Fischer, R.C. Linger, H.F. Lipson, T. Longstaff, and N.R. Mead. Survivable network systems: an emerging discipline. Technical report, Technical Report CMU/SEI-97-TR-013, November 1997, revised May 1999.





# Laprie's View on Dependability and Survivability

Concept	Dependability	Survivability
Goal	1) Ability to deliver service that can justifiably be trusted  2) ability of a system to avoid failures that are more frequent or more severe, and outage durations that are longer, than is acceptable to the user(s)	Capability of a system to fulfill its mission in a timely manner
Threats present	1) design faults (e.g., software flaws, hardware errata, malicious logics)  2) physical faults (e.g., production defects, physical deterioration)  3) interaction faults (e.g., physical interference, input mistakes, attacks, including viruses, worms, intrusions)	1) failures (internally generated events due to, e.g., software design errors, hardware degradation, human errors, corrupted data) 2) attacks (e.g., intrusions, probes, denials of service) 3) accidents (externally generated events such as natural disasters)

[A. Avizienis, J. Laprie and B. Randell, Fundamental Concepts of Computer System Dependability, IARP/IEEE-RAS Workshop on Robot Dependability, Seoul, Korea, May 2001.]



# SEI's View on Survivability, Security, and Fault Tolerance

- Survivability vs. Security
  - Security
    - Availability, confidentiality and integrity (non-repudiation and authentication)
    - Recognition of attacks, resistance to attacks
  - Survivability
    - Broader than security
    - Maintain essential service and recover under attacks and natural disasters
    - Adaptation and evolution to attacks
- Survivability vs. Fault Tolerance
  - Fault tolerance does not (normally) consider malicious attacks (Intrusion Tolerance does)
  - Geographic diversity in survivable systems needed to avoid vulnerabilities to massive attacks or disasters



[3] R.J. Ellison, D.A. Fischer, R.C. Linger, H.F. Lipson, T. Longstaff, and N.R. Mead. Survivable network systems: an emerging discipline. Technical report, Technical Report CMU/SEI-97-TR-013, November 1997, revised May 1999.

# Knight's View on Survivability, Dependability, Security, and Fault Tolerance



- Survivability vs. security
  - In critical information systems security attacks are not a major cause of service failures so far
  - Security faults can be included in survivability requirements as a comprehensive approach
- Survivability vs. dependability
  - Survivability is a property of dependability (an attribute of dependability in Laprie terminology)
  - Other properties (attributes a la Laprie) include reliability, availability, safety, etc.
- Survivability vs. fault tolerance
  - Fault tolerance is a design mechanism (means a la Laprie) to achieve certain dependability properties
  - Other mechanisms (means a la Laprie) include fault avoidance, fault elimination, fault forecasting



[1] J. Knight and K. Sullivan, On the definition of survivability, TR-CS-00-33, University of Virginia, Dec., 2000.

[2] J. Knight, E. Strunk and K. Sullivan, Towards a Rigorous Definition of Information System Survivability, DISCEX 2003.



# Qualitative Definitions of Survivability

- National Communication System Technology & Standards [1]
  - The **ability** of a system, subsystem, equipment, process, or procedure to continue to **function** during and after a natural or man-made **disturbance**.
- Peter G. Neumann [2]
  - Survivability is the **ability** of a system to satisfy and to continue to satisfy critical **requirements** in the face of **adverse conditions**
- CMU/SEI [3]
  - Survivability is the **capability** of a system to fulfill its **mission**, in a timely manner, in the presence of **attacks, failures, or accidents**.
- All of them point to the transient behavior of system after a failure, attack or a natural disaster

**Survivability** is the *system's* ability to continuously deliver *services* in compliance with the given *requirements* in the presence of failures and other *undesired events*.

[1] Federal standard 1037C, Telecommunications: Glossary of telecommunication terms, 1996

[2] P. G. Neumann, Practical Architectures for Survivable Systems and Networks, SRI International, CA, 2000.

[3] R. J. Ellison et al, Survivable network systems: an emerging discipline, TR CMU/SEI-97-TR-013, Nov., 1997, revised May 1999.



# Quantitative Definition of Survivability

- Quantitative Definition [8]. Suppose a measure of interest  $M$  has the value  $m_0$  just before a “failure” happens. The survivability behavior can be depicted by the following attributes:
  - $m_a$  is the value of  $M$  immediately after the occurrence of failure,
  - $m_u$  is the maximum difference between the value of  $M$  and  $m_a$  after the failure,
  - $m_r$  is the restored value of  $M$  after some time  $t_r$ , and
  - $t_R$  is the time for the system to restore the value  $m_0$ .

**Survivability quantification.** The measure of interest  $M$  has the value  $m_0$  just before a failure occurs. The survivability behavior can be depicted by the following attributes:  $m_a$  is the value of  $M$  just after the failure occurs;  $m_u$  is the maximum difference between the value of  $M$  and  $m_a$  after the failure;  $m_r$  is the restored value of  $M$  after some time  $t_r$ ; and  $t_R$  is the relaxation time for the system to restore the value of  $M$ .

- This definition is proposed by the T1A1.2 network “[Survivability performance working group](#)”. By this definition, survivability depicts the time-varying performance (measure  $M$ ) of the system after a failure, attack or a natural disaster occurs.



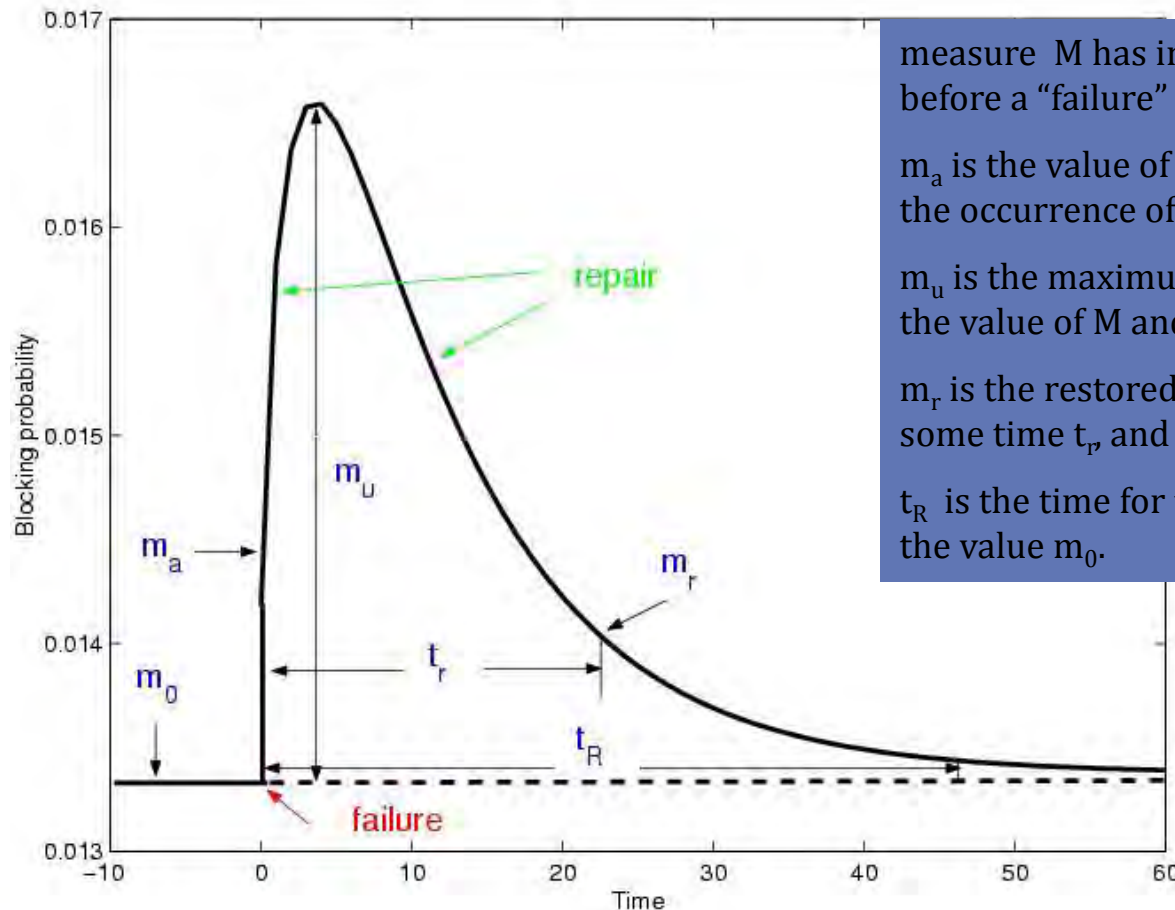
[8] T1A1.2 Working Group on Network Survivability Performance, Technical report on enhanced network survivability performance, Feb., 2001.

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# Quantitative Definition of Survivability



measure  $M$  has initial value  $m_0$  just before a "failure"

$m_a$  is the value of  $M$  immediately after the occurrence of failure,

$m_u$  is the maximum difference between the value of  $M$  and  $m_a$

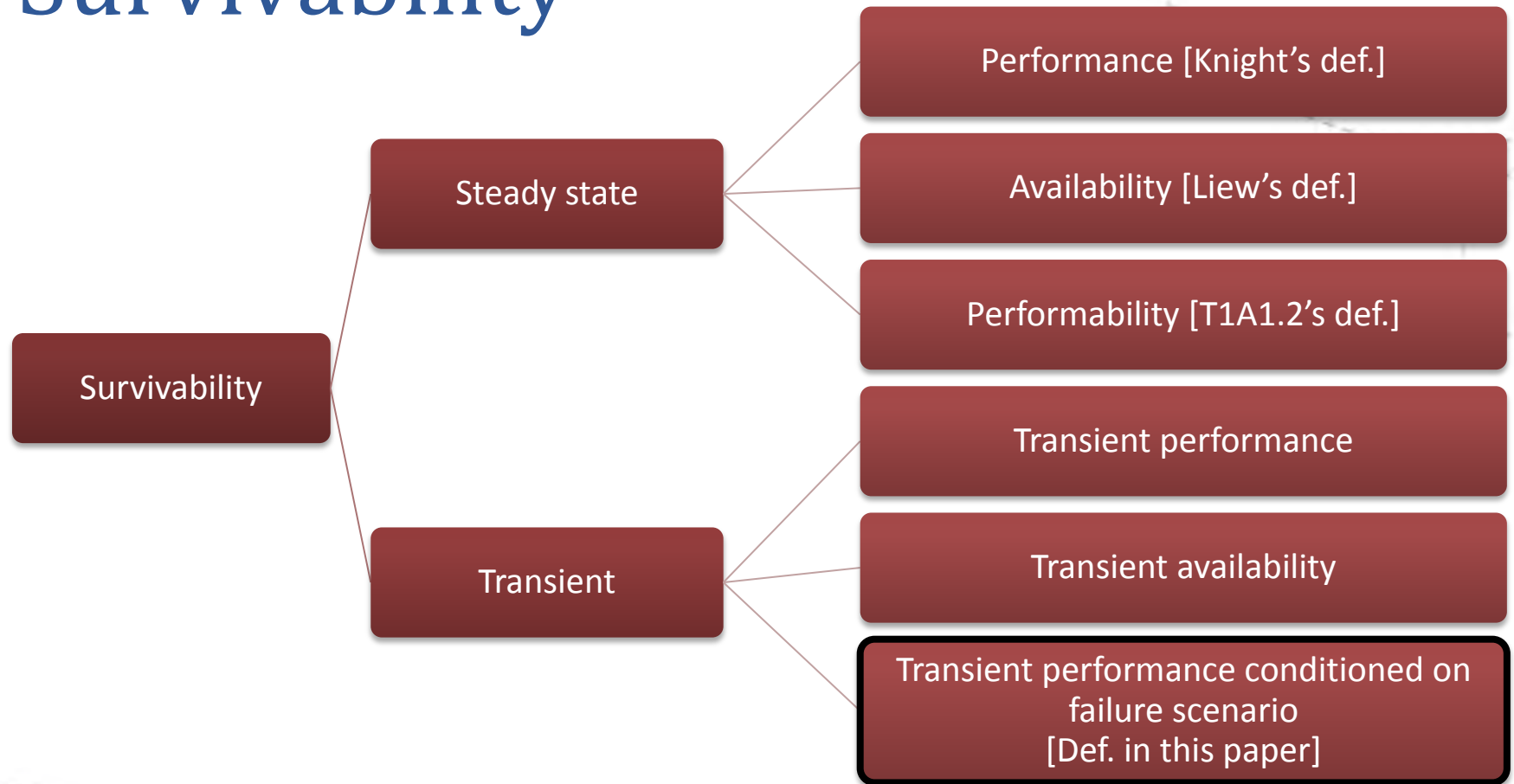
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# Qualitative Definitions of Survivability



From Yun Liu's thesis

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# Survivability Research at Duke University and NTNU



- Analysis approach
  - Develop, parameterize, and solve Markov and non-Markov models including failure modes, traffic patterns, and resource contention.
  - T1A1.2 based survivability measures do NOT depend on the disaster rate; this may be considered good as the disaster rate is hard to quantify in practice



# Survivability Research at Duke University and NTNU



- Publications

- **Poul E. Heegaard and Kishor Trivedi. "Network Survivability Modeling". *Computer Networks*, [Volume 53, Issue 8 \(2009\)](#), pp. 1215-1234. Elsevier.**
- Poul E. Heegaard and Kishor Trivedi. "Survivability Quantification of Communication Services". In proceedings from The 38th Annual IEEE/IFIP International Conference on Dependable Systems and Networks (DSN 2008). June 24-27, 2008, Anchorage, AK, USA, pp 462-471.
- Transient behavior of ATM networks under overloads IEEE INFOCOM' 96, pages 978-985, San Francisco, CA, March 1996.
- Network survivability performance evaluation: a quantitative approach with applications in wireless ad-hoc networks ACM International Workshop on Modeling, Analysis and Simulation of Wireless and Mobile Systems (MSWiM' 02), Atlanta, GA, September 2002.
- A general framework of survivability quantification Proc. of 12th GI/ITG. Conf. On Measuring, Modelling and Evaluation of Computer and Communication Systems (MMB'04)
- Survivability analysis of telephone access network Proc. of 15th IEEE International Symposium on Software Engineering (ISSRE'04)



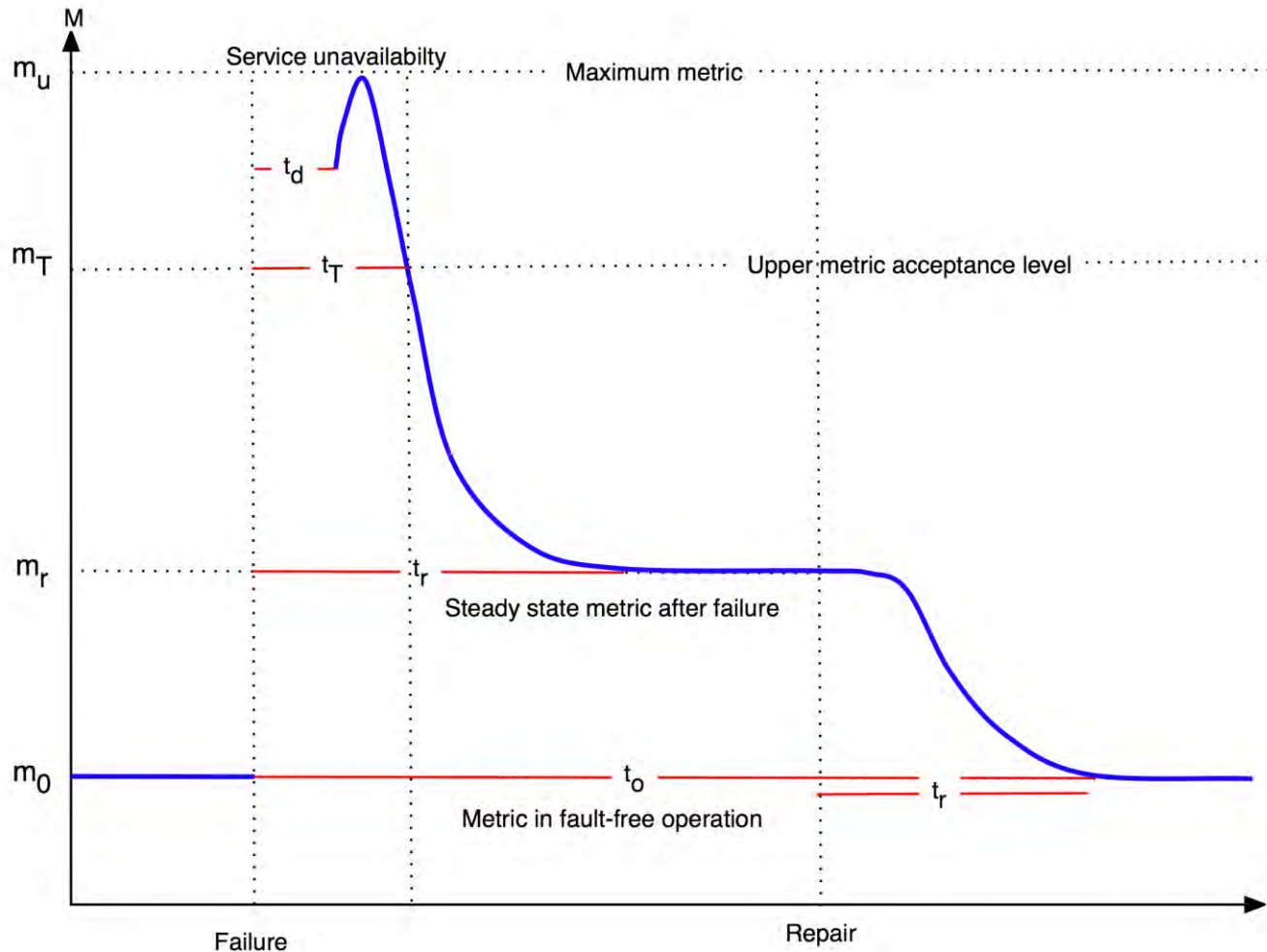


## II. Network survivability modeling and quantification





# Network survivability quantification



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# Implications of T1A1.2 Definition

- System is initially assumed to be in **steady state** (pure performance model) with all components functioning
- **Force a failure** in the system and study the **transient behavior** until it reaches the original steady state upon completion of repair



# A General Quantification Procedure

- Step 1
  - Develop the pure availability model in which the resources (hardware and/or software) fail and get repaired (or rebooted).
- Step 2
  - Develop a pure performance model and obtain the steady state results of the pure performance model, which reflects the resource usage and other system state information before a failure happens. The performance model could have arrival and service of tasks reflected.
- Step 3
  - Combine the availability and performance models obtained in the first two steps into a composite model.
- Step 4
  - Choose a survivability measure of interest. Force a specific failure in the system and construct a truncated model. In order to reflect the system resource usage before the failure happens, initial probability must be appropriately assigned for the truncated model.
- Step 5
  - Perform the transient analysis of the truncated composite model.



# An illustrative example 1: A telecom switching system

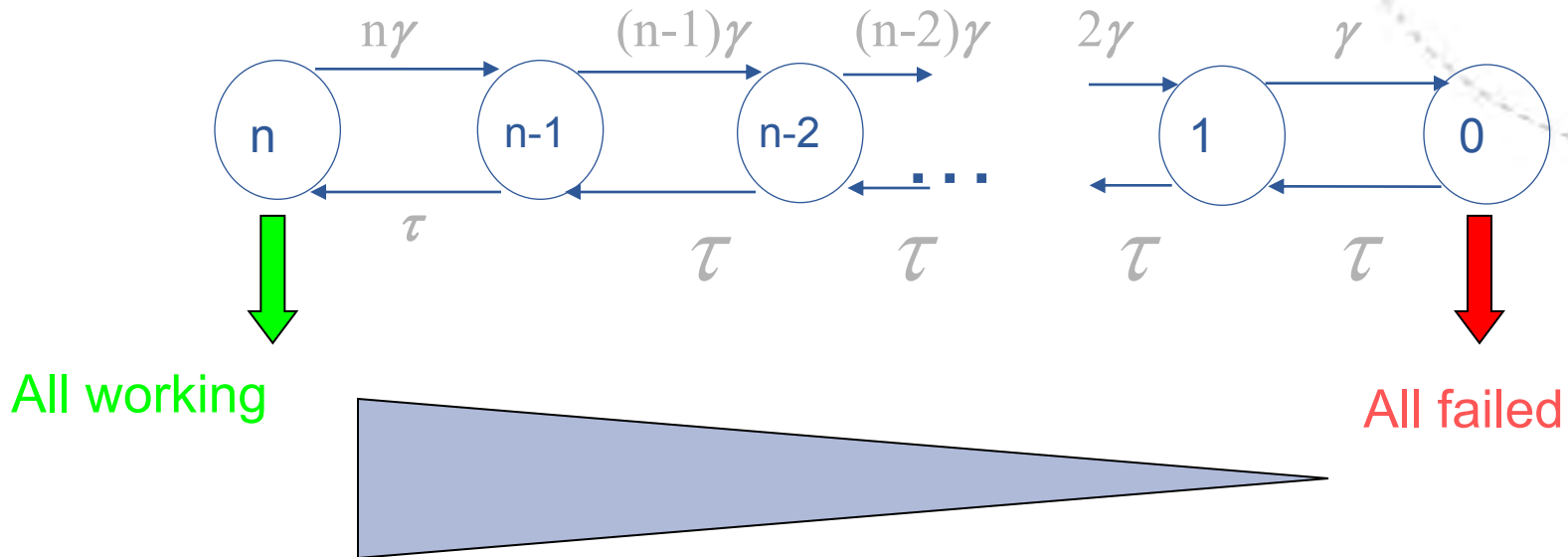


- Assumptions

- A telecom switching system with  $n$  trunks
- Call inter-arrival time  $Exp(\lambda)$
- Call holding time  $Exp(\mu)$
- Time to failure  $Exp(\gamma)$
- Time to repair  $Exp(\tau)$
- Single repair facility



# Pure Availability Model



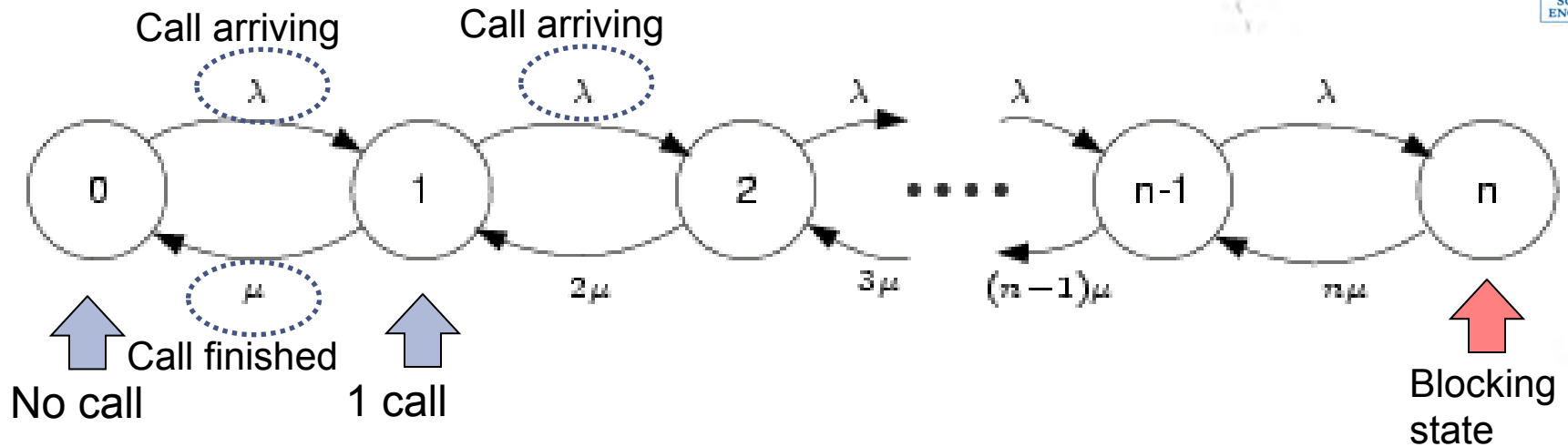
Resource  
degradation

$$\pi_i^A = \frac{\left(\frac{\tau}{\gamma}\right)^i / i!}{\sum_{k=0}^n \left(\frac{\tau}{\gamma}\right)^k / k!}$$

$$n=25, \gamma=0.002 \text{ s}^{-1}, \tau=0.1 \text{ s}^{-1}$$



# Pure Performance Model



Steady state closed-form solution:  
Erlang B Formula

$$\pi_j^P = \frac{\left(\frac{\lambda}{\mu}\right)^j / j!}{\sum_{k=0}^n \left(\frac{\lambda}{\mu}\right)^k / k!}$$

Blocking probability:

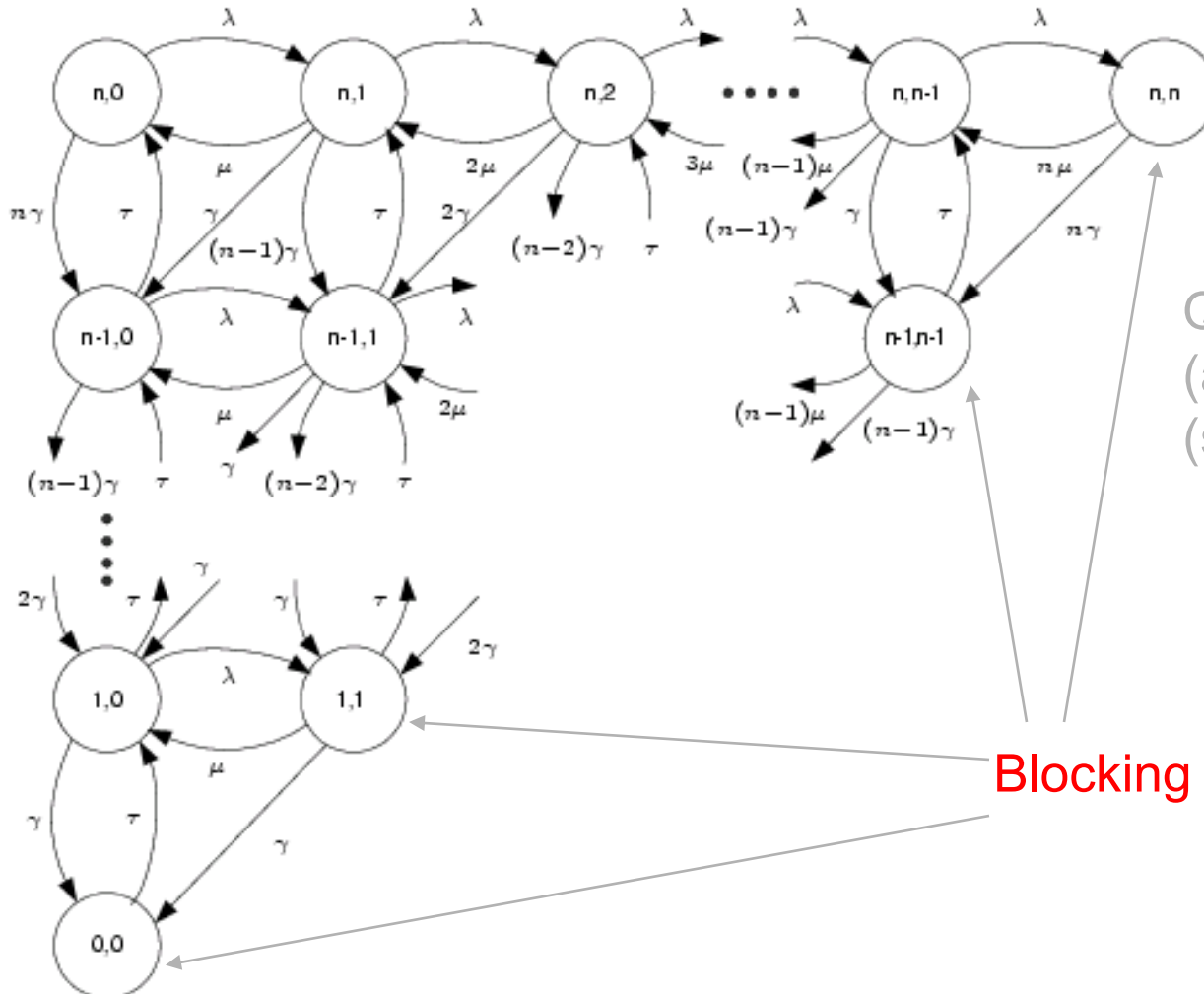
$$P_{bk} = \pi_n^P$$

$$n=25, \lambda=5 \text{ s}^{-1}, \mu=0.3 \text{ s}^{-1}$$

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# Composite Performability Model



Q: What state(s) is (are) blocking state(s)?

**Blocking states**



# Performance, Availability, and Performability

## Measure of Interest : $P_{bk}$

- Performance
  - From pure performance model
  - Steady state blocking probability  $P_{bk}$
  - $P_{bk} = \pi_n^P = 0.013376$
- Availability
  - From pure availability model
  - $P_A = 1 - \pi_n^A = 1 - 2.6935 \times 10^{-18}$
- Performability (PA type)
  - From composite model
  - $P_{bk}' = \sum_{k=0}^n \pi_{k,k}^C = 0.020178$



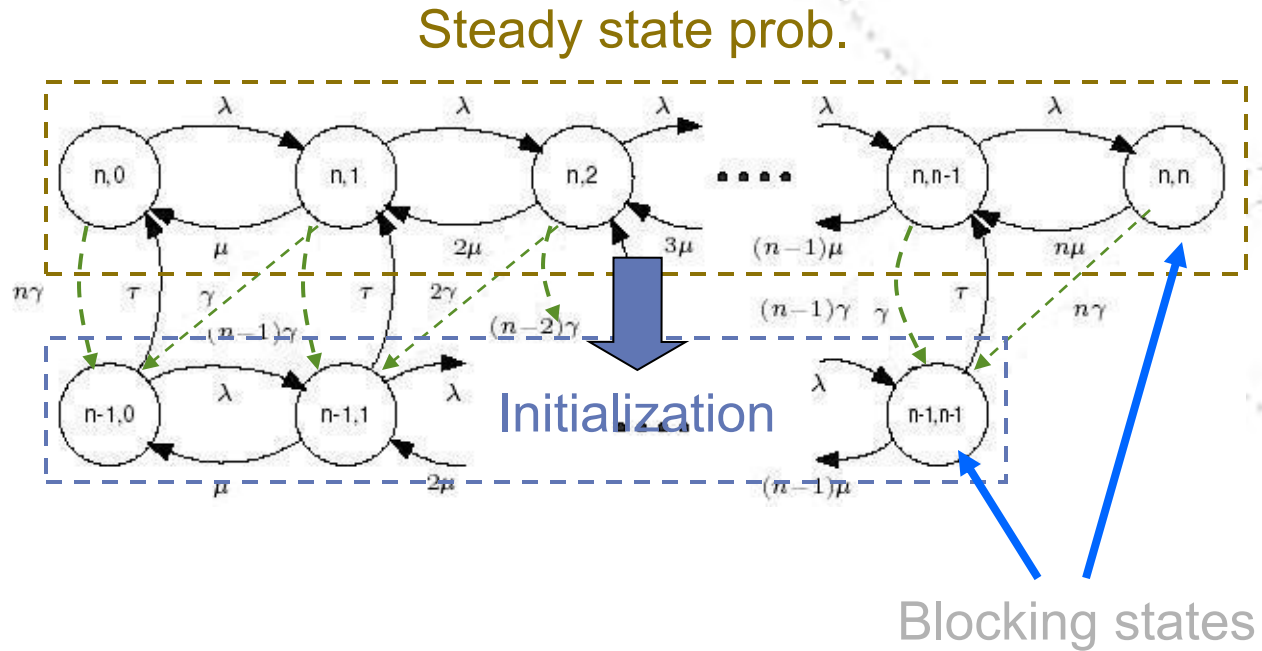
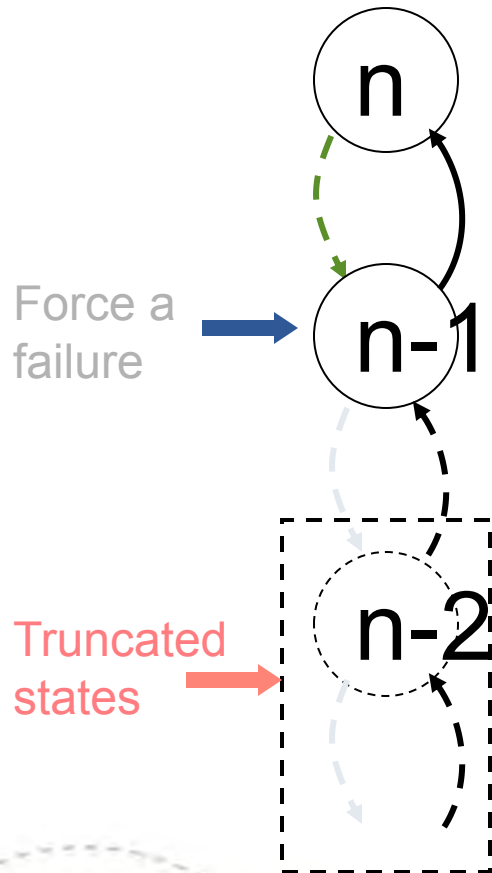


# Survivability Quantification Approach

- System operating in steady state
- Force a failure:
  - Initial state probabilities for the degraded mode states
  - Transient solution of the truncated performability model



# Truncated Performability Model

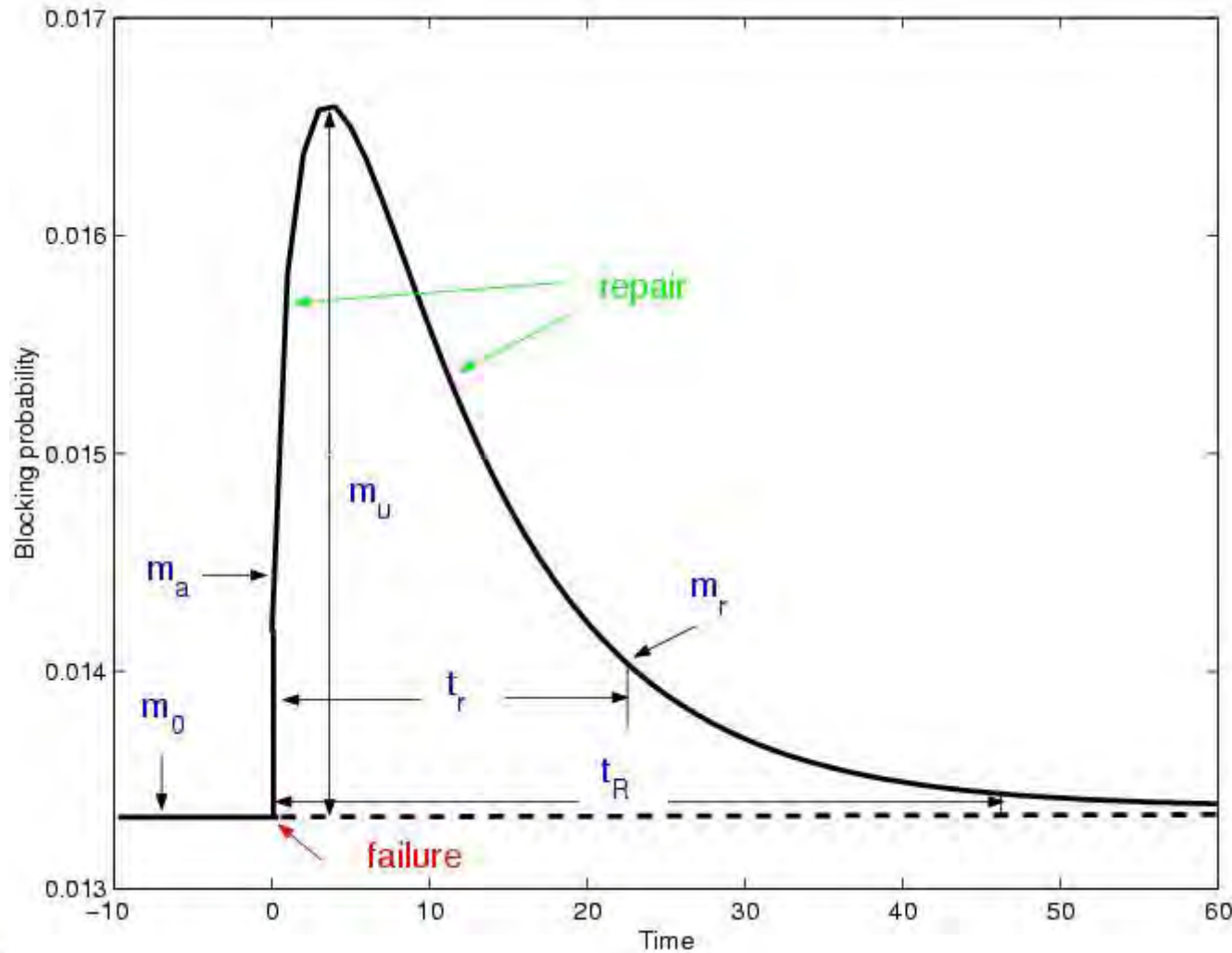


(forced) Failure transitions





# Survivability Results

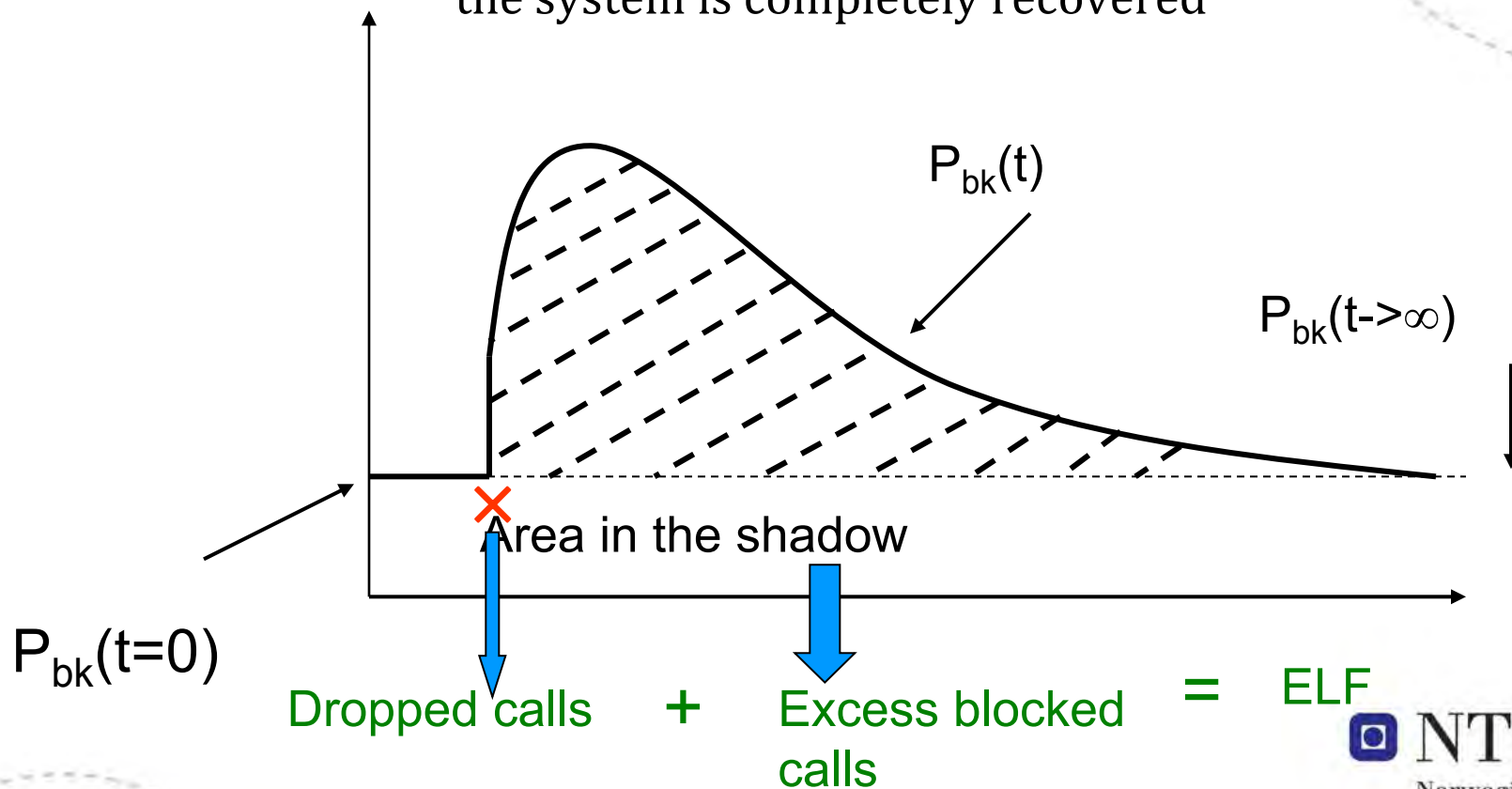


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# Another Survivability Measure: Excess Loss Due to Failure (ELF)

ELF: a survivability measure reflecting the total loss before the system is completely recovered





# ELF results

Relaxation time*	Call loss due to the 1 <sup>st</sup> failure $N_d$	Extra call loss due to blocking $N_b$	ELF
39s	0.6557	0.2457	0.9014

$$N_d = \frac{j}{n} \pi_j^P$$

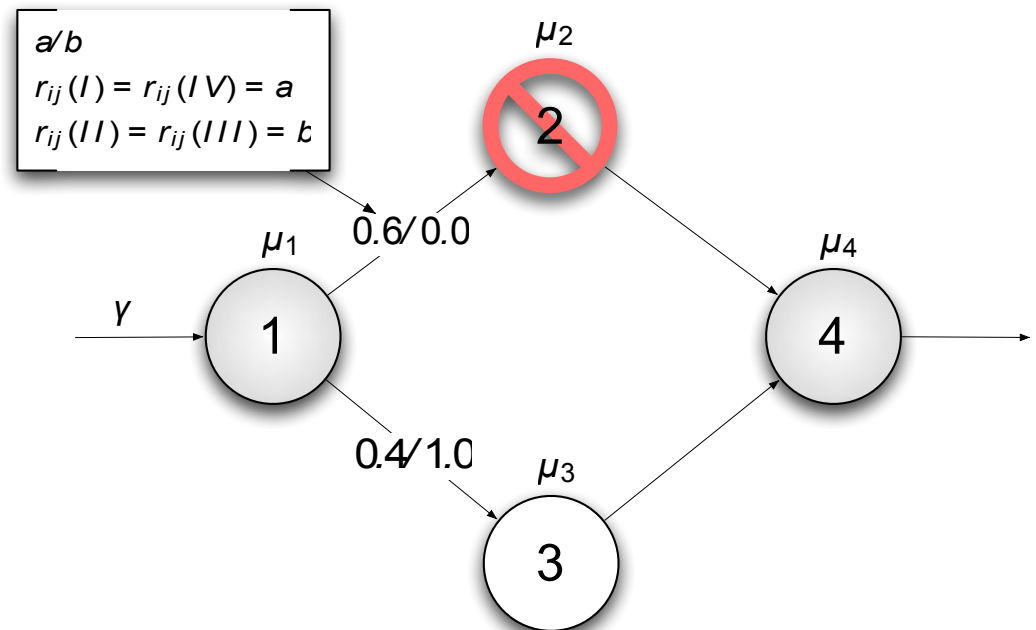
$$N_b = \int_0^{t_R} (P_{bk}(t) - P_{bk}(t \rightarrow \infty)) \lambda dt$$

\*: based on a relative error of 0.1%, i.e., 100.1% of the original blocking prob. restored



# Illustrative example 2: Network with 4 nodes

- Simulation model (Simula/DEMOS)
- Stochastic Reward Net (Generalized PetriNets) model
- CTMC model of each node
- Closed form solution
- Comparisons





# Network with 4 nodes: Approaches

- Simulation
  - DEMOS/Simula
  - Discrete event, process-oriented simulation model
- Analytical
  - SRN: Stochastic Reward Networks
    - Full CTMC, same as simulation model
    - Solved by SPNP and SHARPE
  - CTMC: (Decomposed) Markov models
    - Combined performance and dependability model
    - Product-form approximation
    - Solved by SHARPE

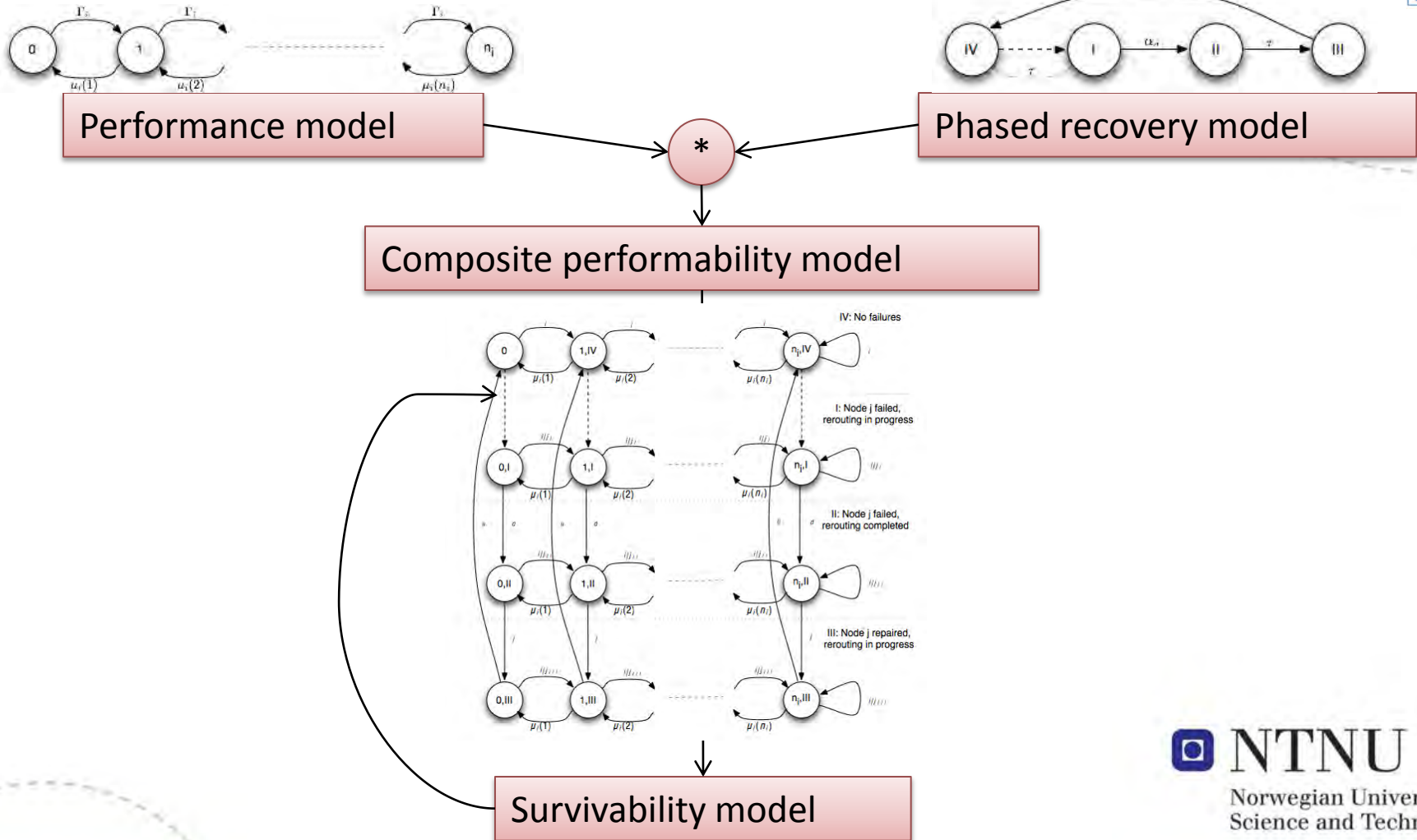




# Objective

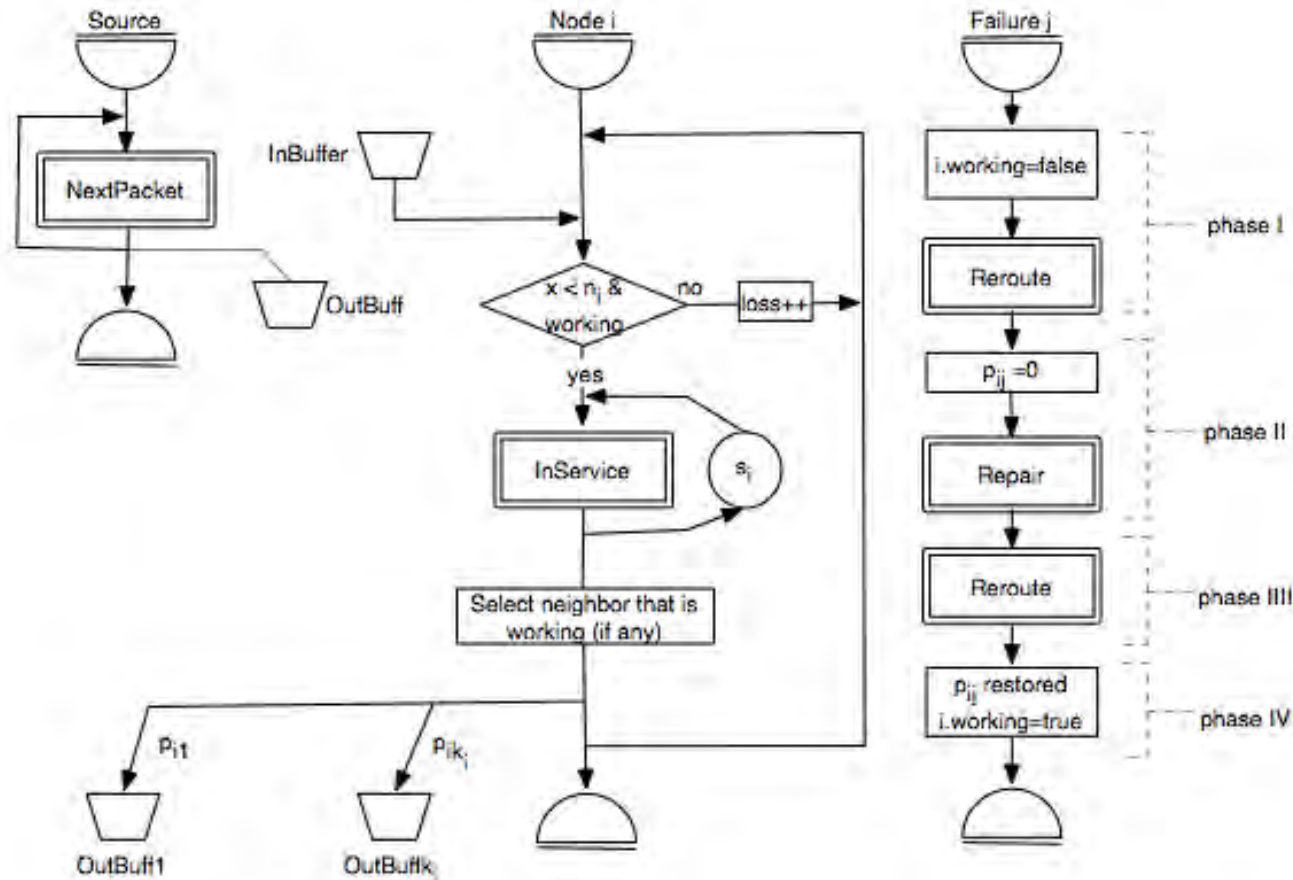
- Performance in networks with virtual connections
- Transience from occurrence of an undesired event until steady state operation is restored
- Routing in acyclic, directed graph
- Directed from SRC->DST nodes
- Goal: Survivability model of performance after network failure(s)

# Modeling approach





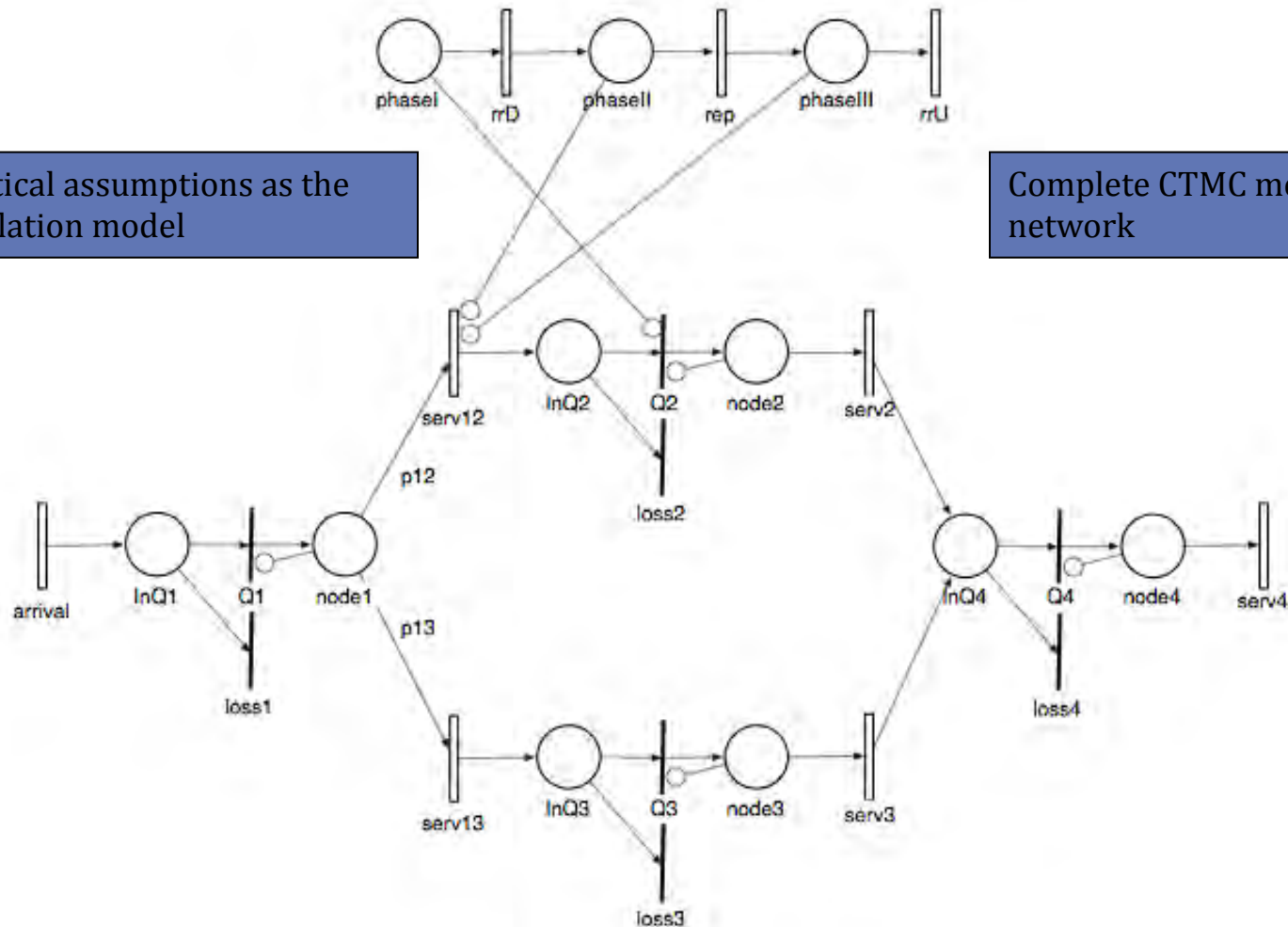
# Network with 4 nodes: Simulation model



# Network with 4 nodes: Stochastic Reward Net model

Identical assumptions as the simulation model

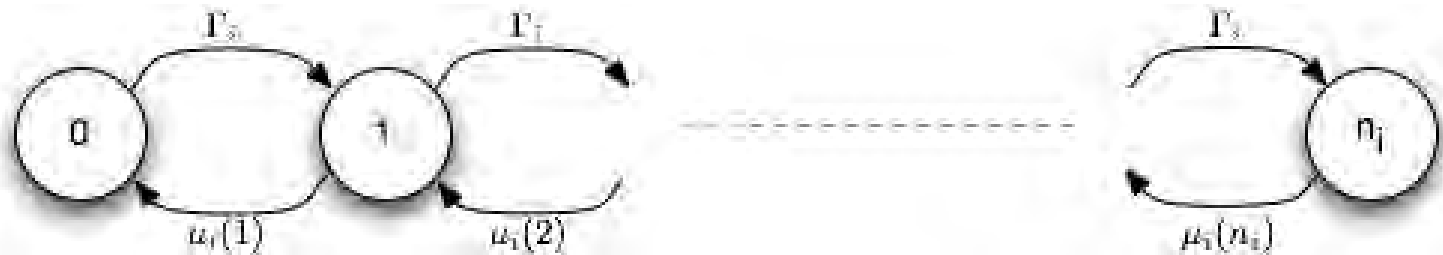
Complete CTMC model of network





# Network with 4 nodes: CTMC Performance model

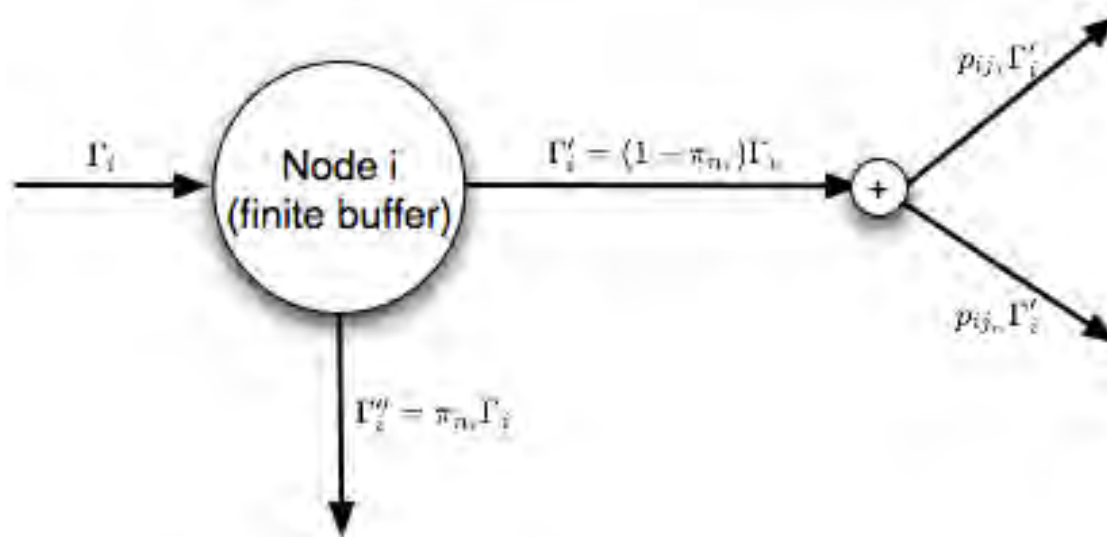
- Decomposed CTMC to reduce number of states
- Nodes modeled separately
- The arrival intensities change when node or link fails
- The resource utilization model below is solved for each set of intensities



# CTCM: Arrival intensities to a node



- Assume acyclic graph from SRC to DST

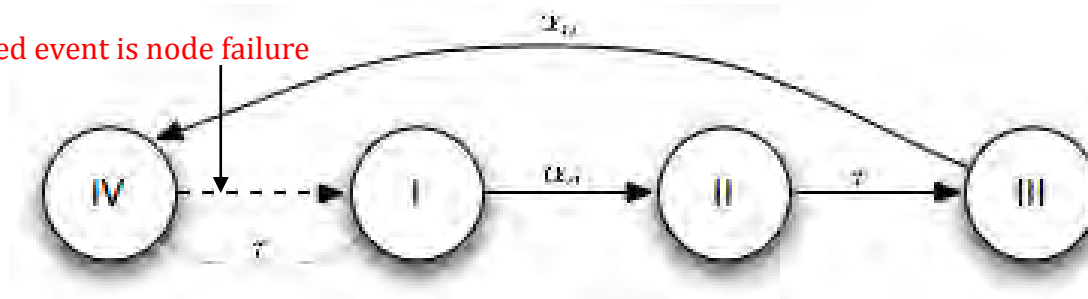




# Network failure and rerouting

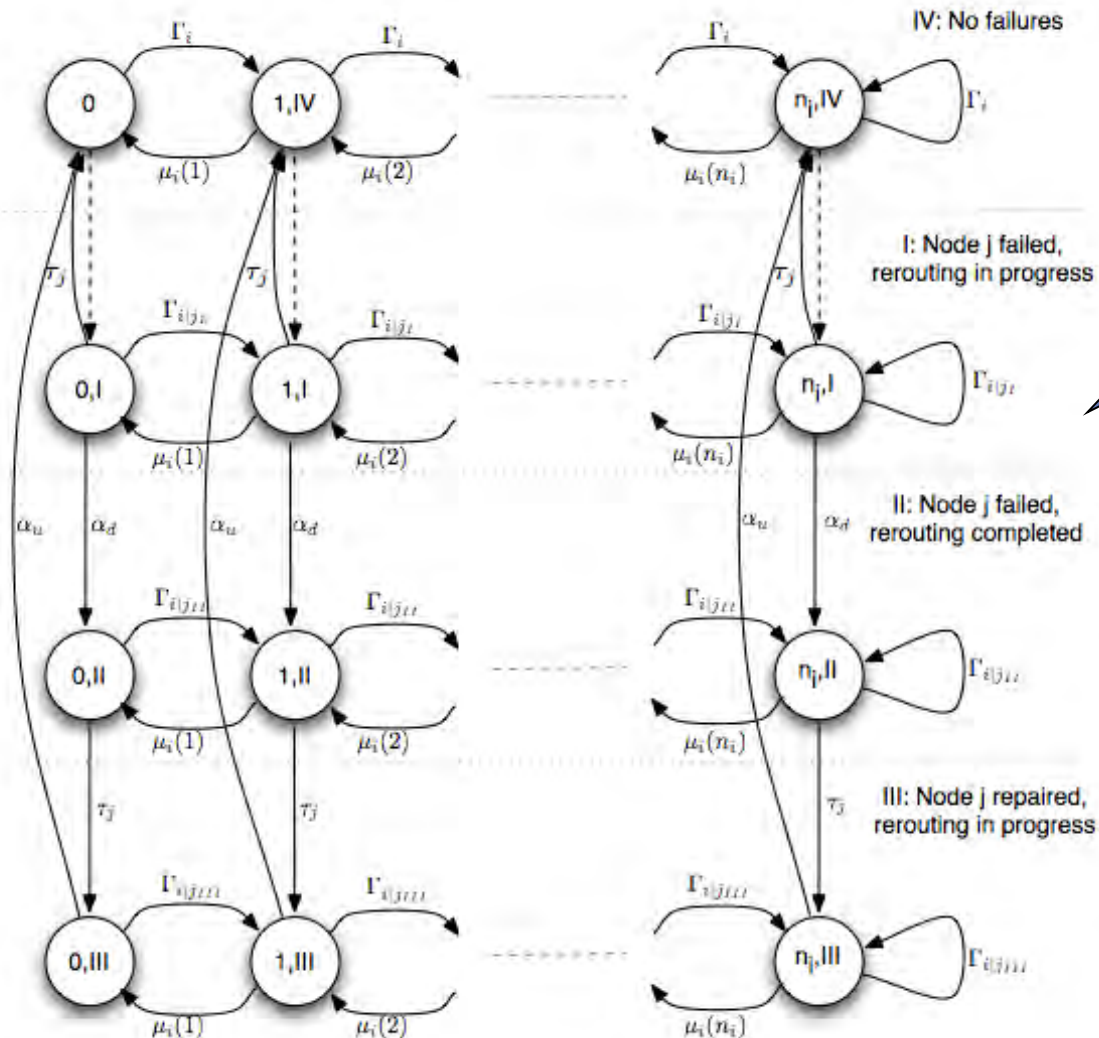
- Phase I:
  - Rerouting after failure is  $T_D \sim \exp(\alpha_D)$
- Phase II:
  - Restoration time is  $T_R \sim \exp(\tau)$
- Phase III
  - Rerouting after failure is  $T_U \sim \exp(\alpha_U)$

Undesired event is node failure

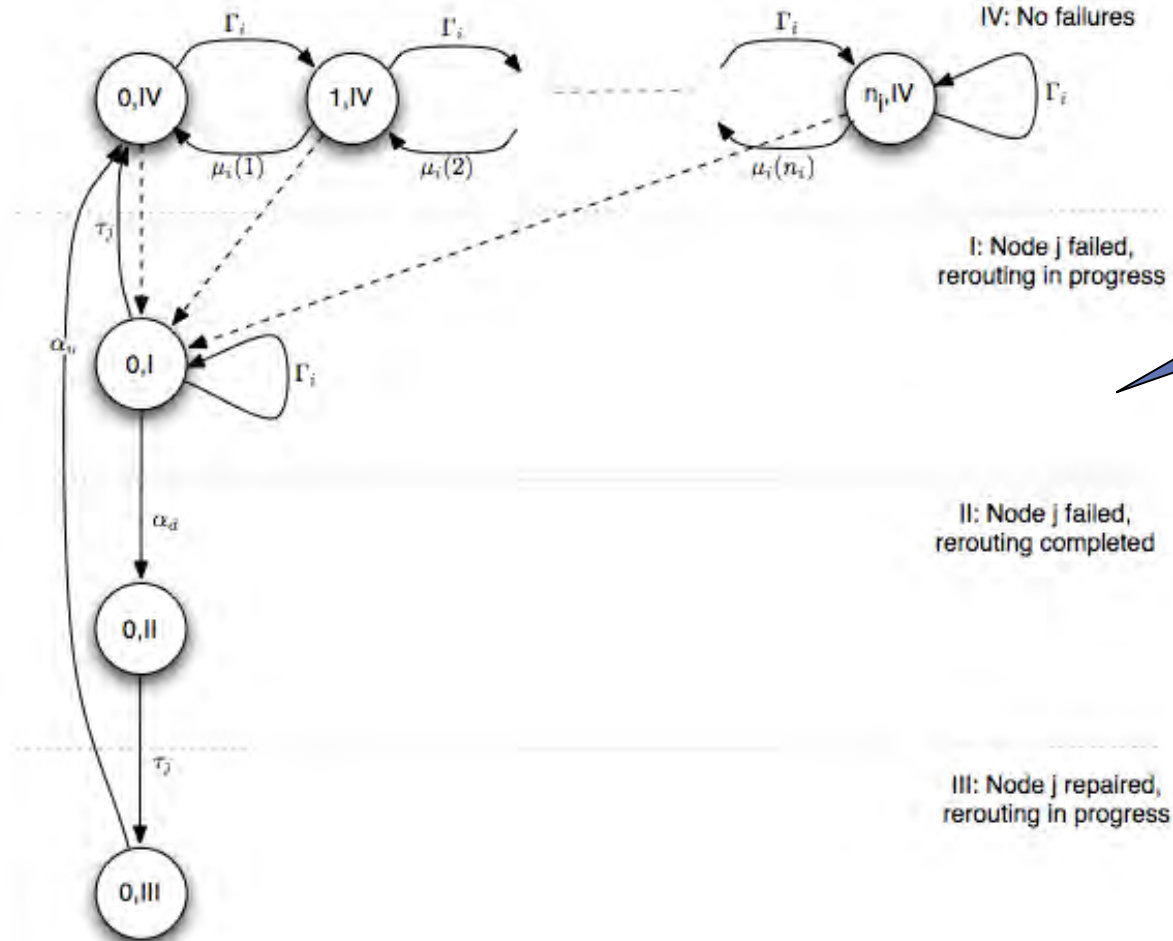




# CTMC: Combine models



# CTMC: Combine models



I: Node j failed,  
rerouting in progress

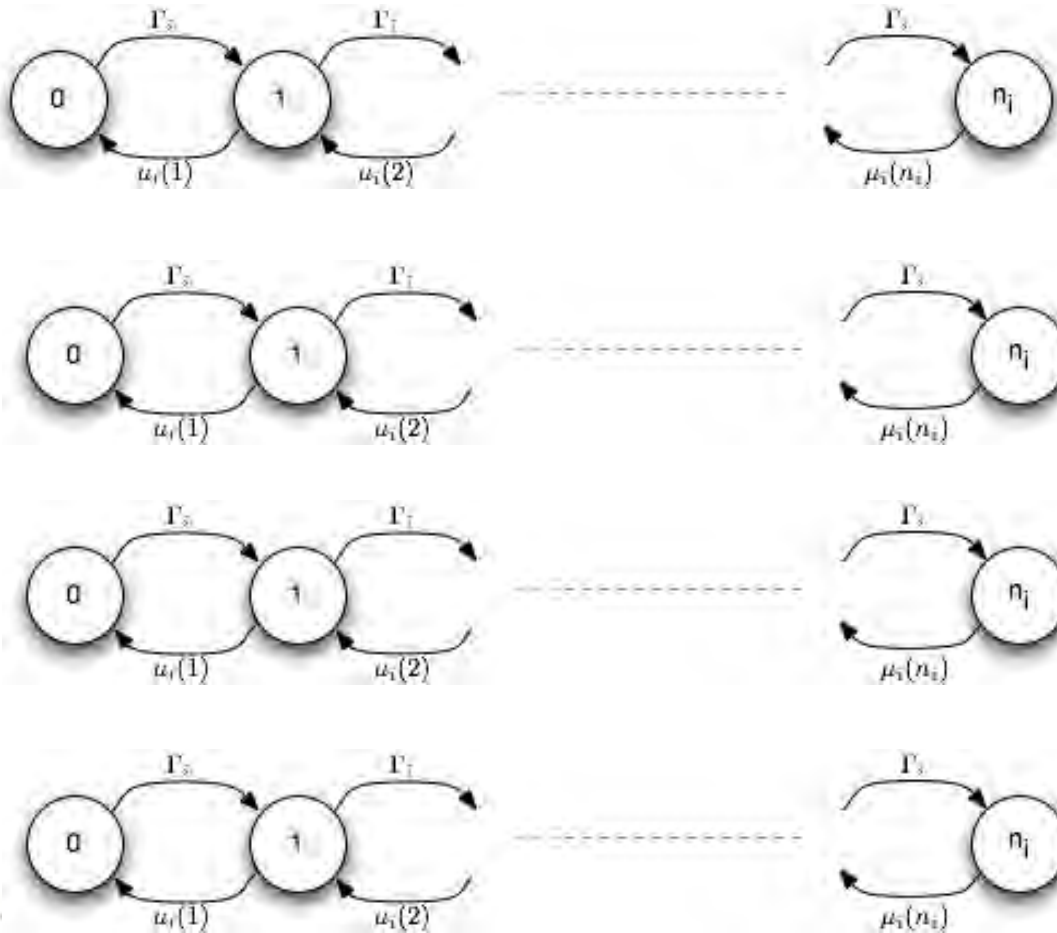
Failed node

II: Node j failed,  
rerouting completed

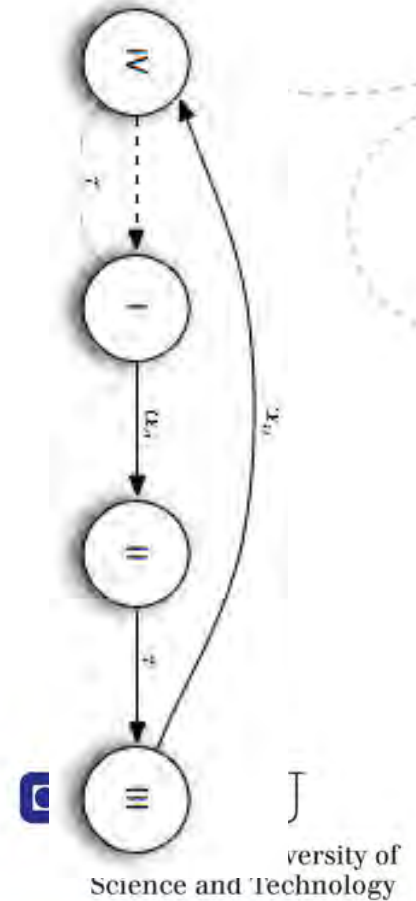
III: Node j repaired,  
rerouting in progress

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# CTMC: Combine models



\*





# CTMC: Combine models

- Number of states in combined model
  - Transient solution of  $N_{\text{node}}$  models with  $N_{\text{res}} \times N_{\text{phase}}$  states
- Product-form approximation
  - When arrival and service rates are “significantly” higher than rerouting and failure rates
  - This means when the state of the performance model at state changes in the dependability model does not have a significant impact of the transient behavior
  - Solve  $N_{\text{node}} \times N_{\text{phase}}$  models with  $N_{\text{res}}$  states and one with  $N_{\text{phase}}$



# CTMC: Combine models

- Arrival & service rates are much larger than rerouting & restoration rates
  - Product form solution can be assumed
  - Do not need to consider initial states in failure and rerouting model
- State probability at time  $t$  of node  $k$  is
  - $P_k(t; \mathbf{x}, i) = \pi_k(\mathbf{x}) * p(t, i)$ ,  
where state  $\mathbf{x} = 1, \dots, n_k$ , phase  $i = I, \dots, IV$



# Performance metrics

- Packet loss,

$$l_k(t) = \sum_{i=I}^{IV} \pi_k(n) \text{RL}_k(n, i) p(t, i)$$

- Throughput,

$$l(t) = \sum_{k=1}^{N_{node}} l_k(t) / \Gamma_s$$

$$\rho(t) = 1 - l(t)$$



# Performance metrics

- Delay,

$$EN_k(t) = \sum_{i=1}^{IV} RD_k(x, i) \pi_k(x) p_k(t, i)$$

$$d(t) = \sum_{k=1}^{N_{node}} EN_k(t) / \Gamma_s$$





# Rewards in Markov model

- Reward

$$R_k(x, i); k = 1, \dots, N_{\text{node}}, x = 0, \dots, N_{\text{res}}, i = I, \dots, IV$$

- Reward packet loss

- $RL_k(x, i) = 0$  for all states and phases except

- for each node and all phases  $i$ :  $RL_k(N_{\text{res}}, i) = \Gamma_k$

- for all states in phase I of the failed node  $RL_k(x, I) = \Gamma_k$

- Reward delay: (Number in system+Little)

- $RD_k(x, i) = x$  for all states and phases except

- for the failed node  $RD_k(x, i) = 0; i = I, II, III$



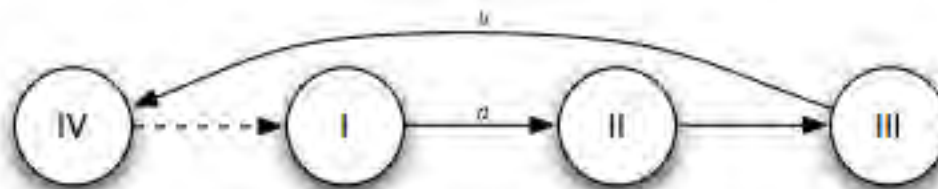


# CTMC model of each node



Performance model

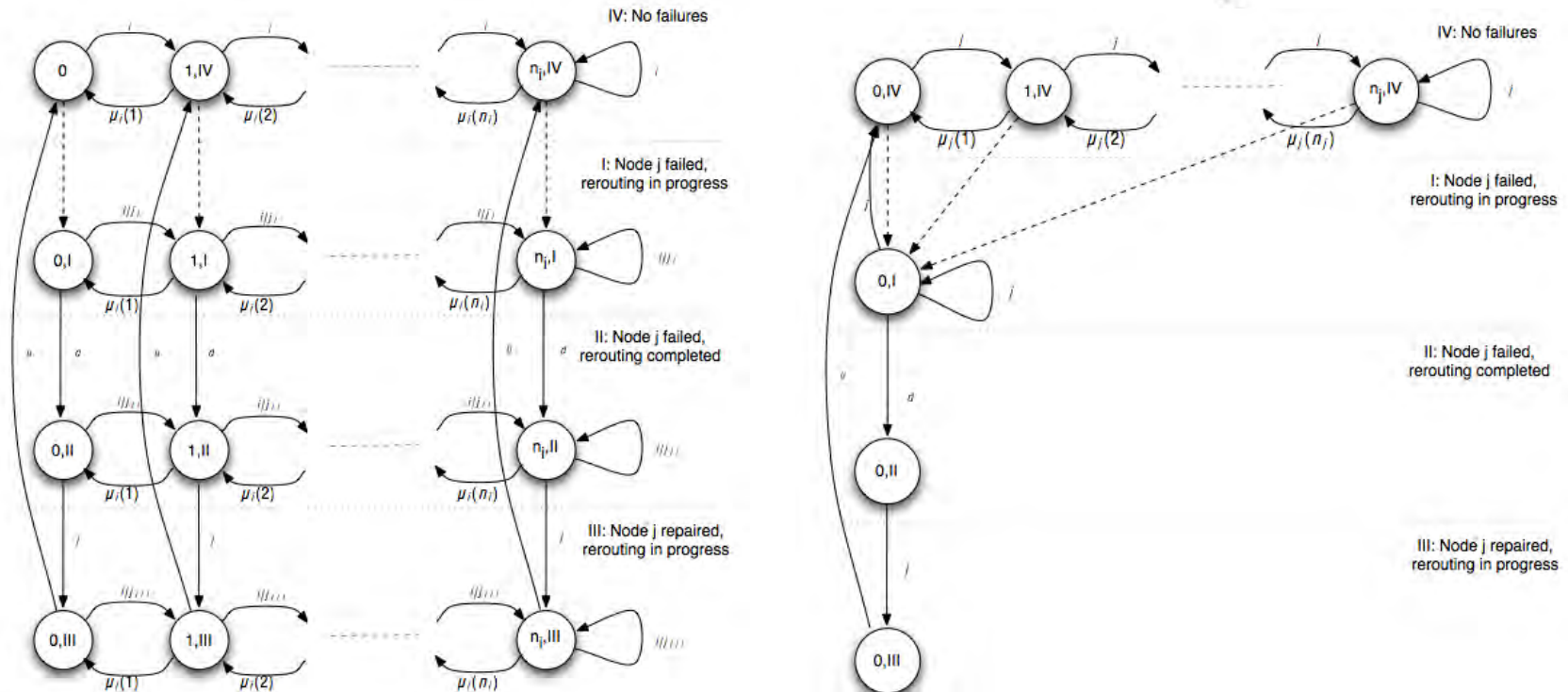
Assume product form solution (Jackson)



Availability model

# CTMC model of each node

## Survivability models



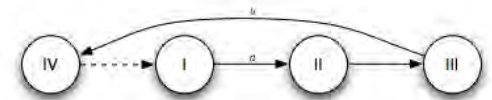
Non-failed node

Failed node



# Closed form solution

- Assume product form solution (Jackson Network)
- Determine steady state performance of each phase,  $p_{j,i}$ 
  - I. Immediately after a failure
  - II. Rerouting completed after failure
  - III. Restoration/repair done
  - IV. Rerouting completed after repair (normal operation)
- Assign rewards,  $r_{j,i}$ , and determine expected rewards
- Determine transient probabilities of each phase,  $p_i(t)$
- Assumptions
  - Event rate in performance models high
  - Event rate in availability model low
  - At phase changes: Immediate change between steady state solutions



$$\text{Transient reward: } R(t) = \sum_j \sum_i p_{j,i} r_{j,i} p_i(t)$$



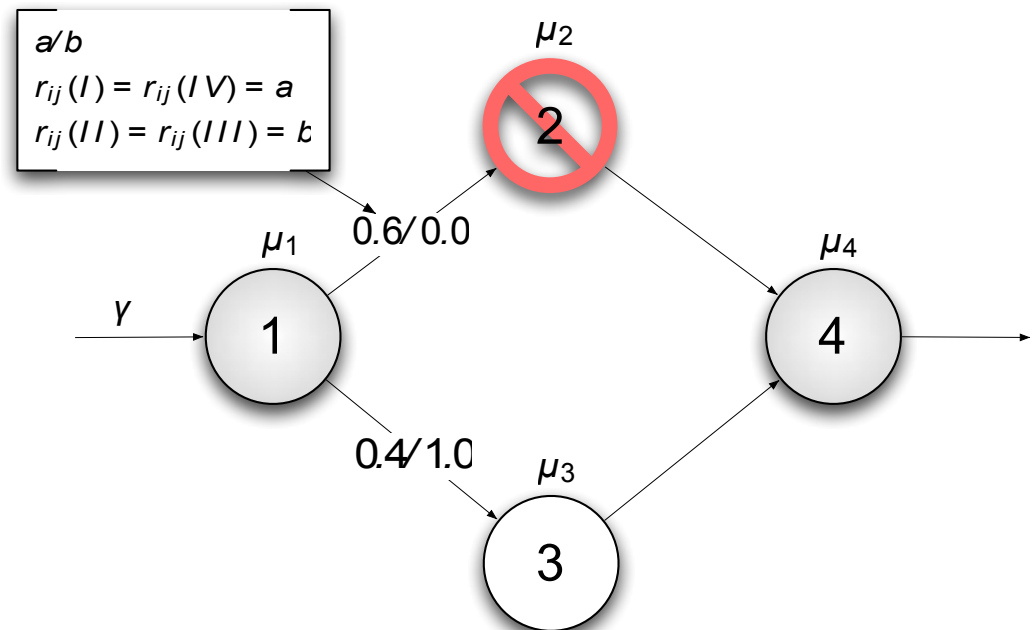
# Solving the models

- SRN
  - Transient solution of model with  $N_{\text{node}} \times N_{\text{res}} \times N_{\text{phase}}$  states
- Depomposed CTMC
  - Transient solution of  $N_{\text{node}}$  models with  $N_{\text{res}} \times N_{\text{phase}}$  states
- Depomposed CTMC
  - Steady state solution of  $N_{\text{node}} \times N_{\text{phase}}$  models with  $N_{\text{res}}$  states
  - Transient solution of one model with  $N_{\text{phase}}$  states



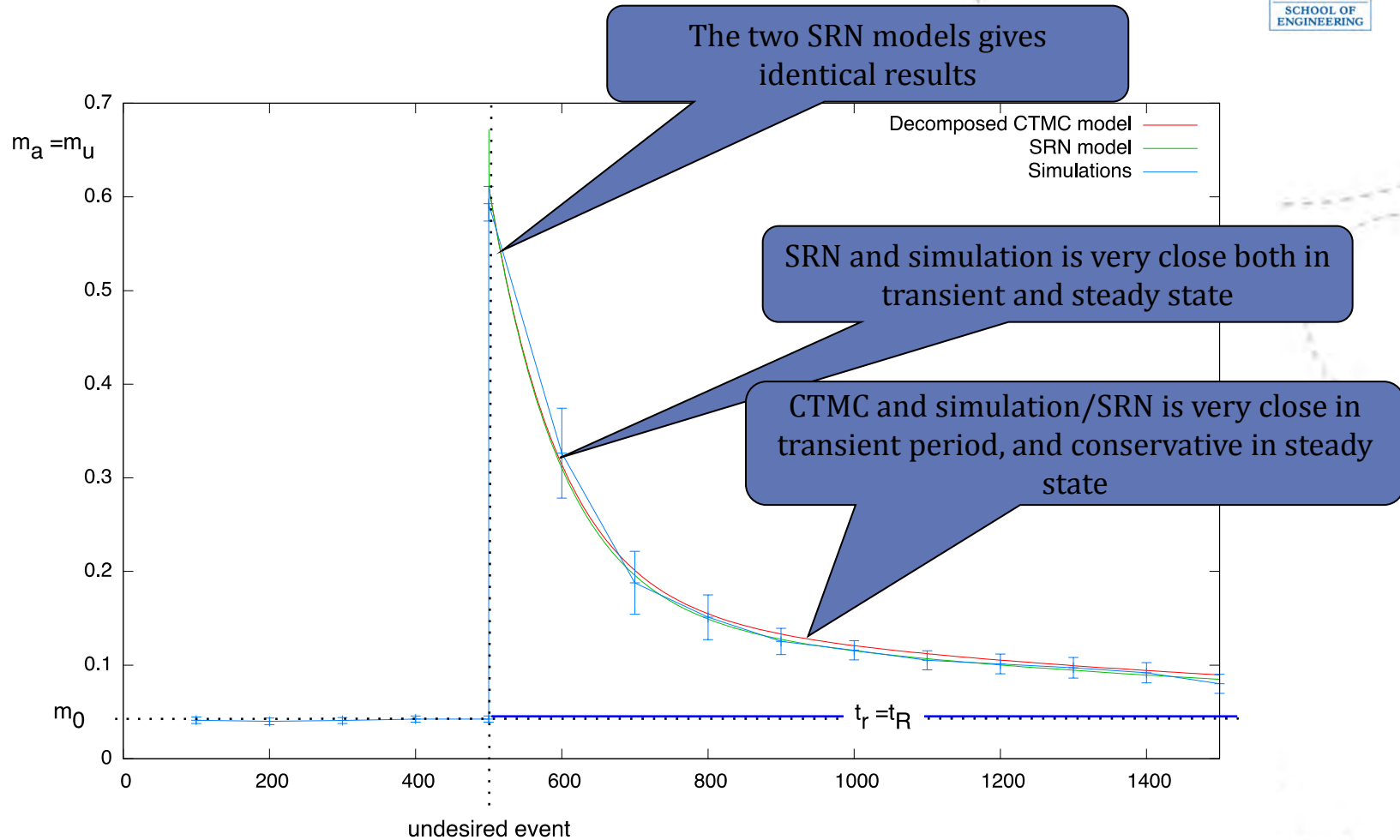
# Illustrative example 1: Network with 4 nodes

- Simulation model (Simula/DEMOS)
- Stochastic Reward Net (Generalized PetriNets) model
- CTMC model of each node
- Closed form solution
- Comparisons



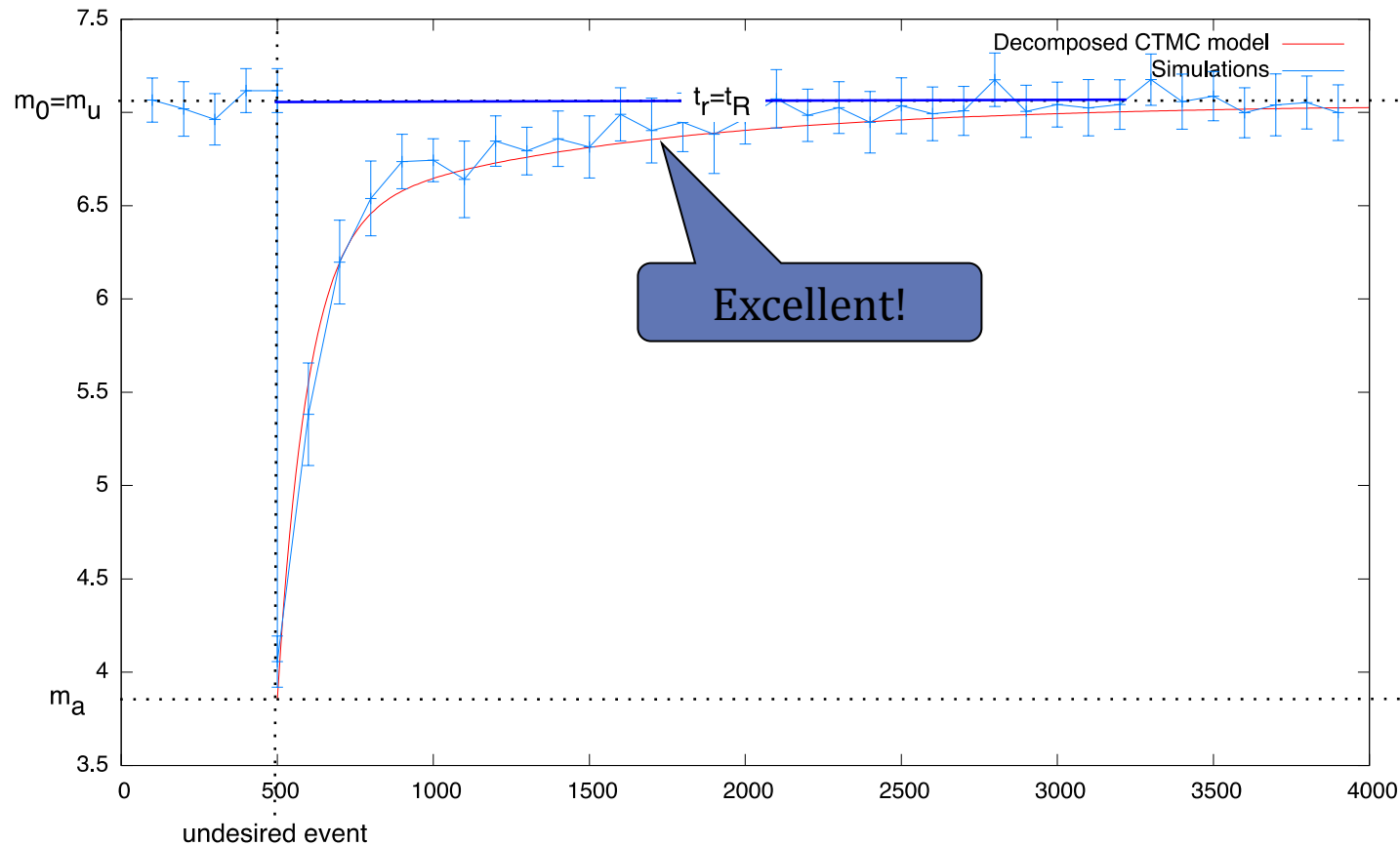


# Network with 4 nodes: loss ratio





# Network with 4 nodes: average number in system



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## III. Case studies



COURTESY: DURHAM CONVENTION AND VISITORS BUREAU



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# Application in Real sized network

- System
  - packet switched, telecommunication network
- Service
  - virtual connection between specific peering nodes in the network
- Requirement
  - maximum packet loss probability and end-to-end delay of non-lost packets in the virtual connections
- Undesired events
  - link and node failures caused by attacks, accidents, and software and hardware failures

# Why does the voice network need to be survivable



- Telecommunications network
  - Voice network
  - Data network
- The voice network is a part of the critical infrastructure.
- Other critical infrastructure depends on the voice network for effective functioning; for example
  - emergency services
  - government services
  - banking and finance
- There are several examples of the failure of the voice network as a result of catastrophic events.
- Many architectures concentrate high density trunks and lines at switch nodes, which exacerbates the extent of communication loss after a catastrophic event.



# Telecommunications system failures

- Externally caused events (North American examples)
  - Hinsdale, Illinois central office switch fire, May 1988
  - San Francisco Bay Area earthquake, October 1989
  - Oakland fire storm, October 1991
  - Judge Thomas senate vote, October 1991
  - Events of September 11, 2001
  - North America power outage, August 14, 2003
- Internally caused events (North American examples)
  - Signaling System 7 (SS7) outage, January 1990
  - Newark fiber cut, January 1991
  - New York power outage, September 1991

# Classical PSTN network hierarchy of switches



**Class 1**  
**Regional**

Physical  
Realization

Logical  
Structure

**highly survivable**

- Diverse switch locations
- SDH/SONET facility protection
- Alternate routes between offices

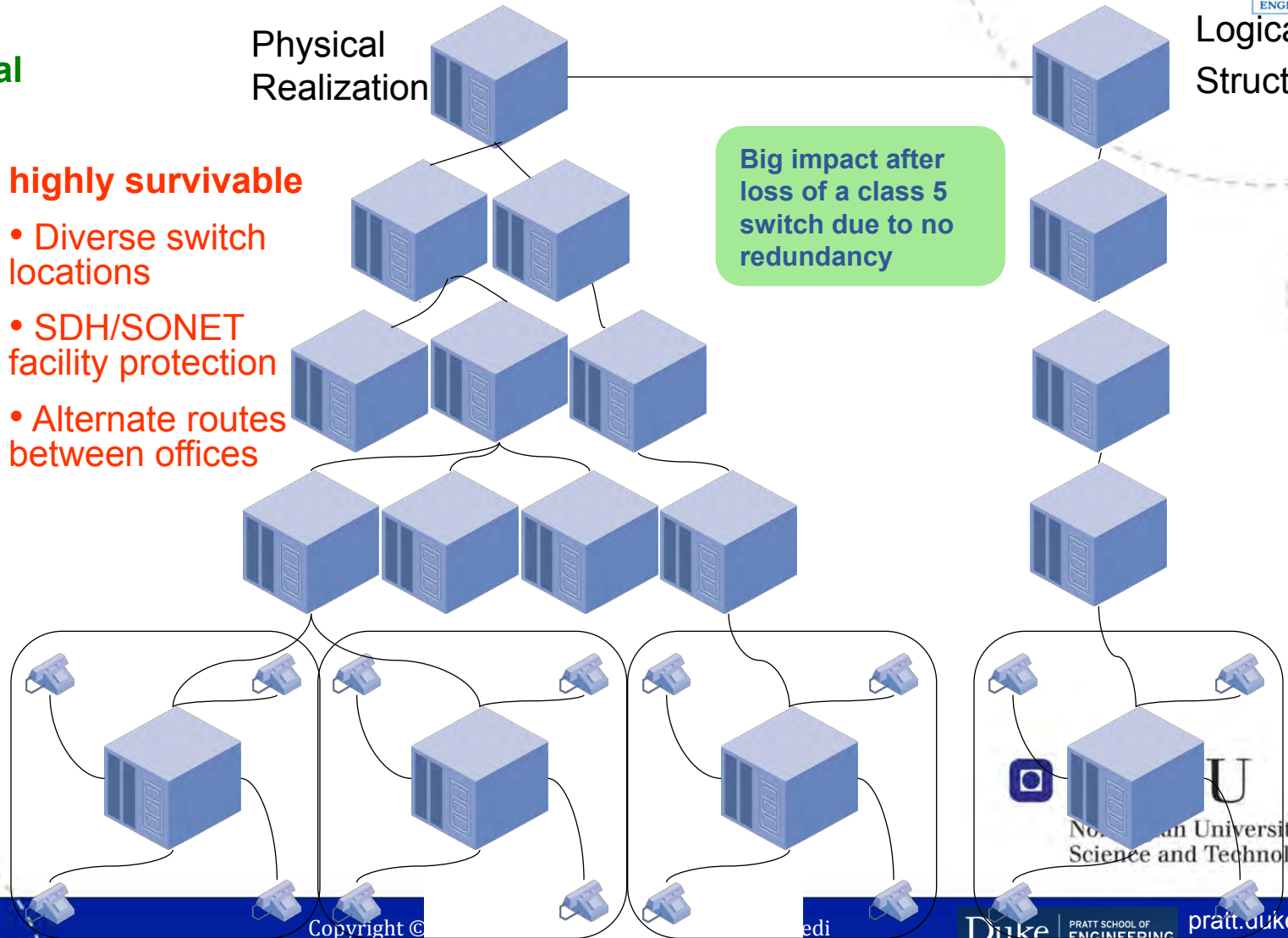
Big impact after loss of a class 5 switch due to no redundancy

**Class 2**  
**Sectional**

**Class 3**  
**Primary**

**Class 4** Toll

**Class 5**  
**Local**

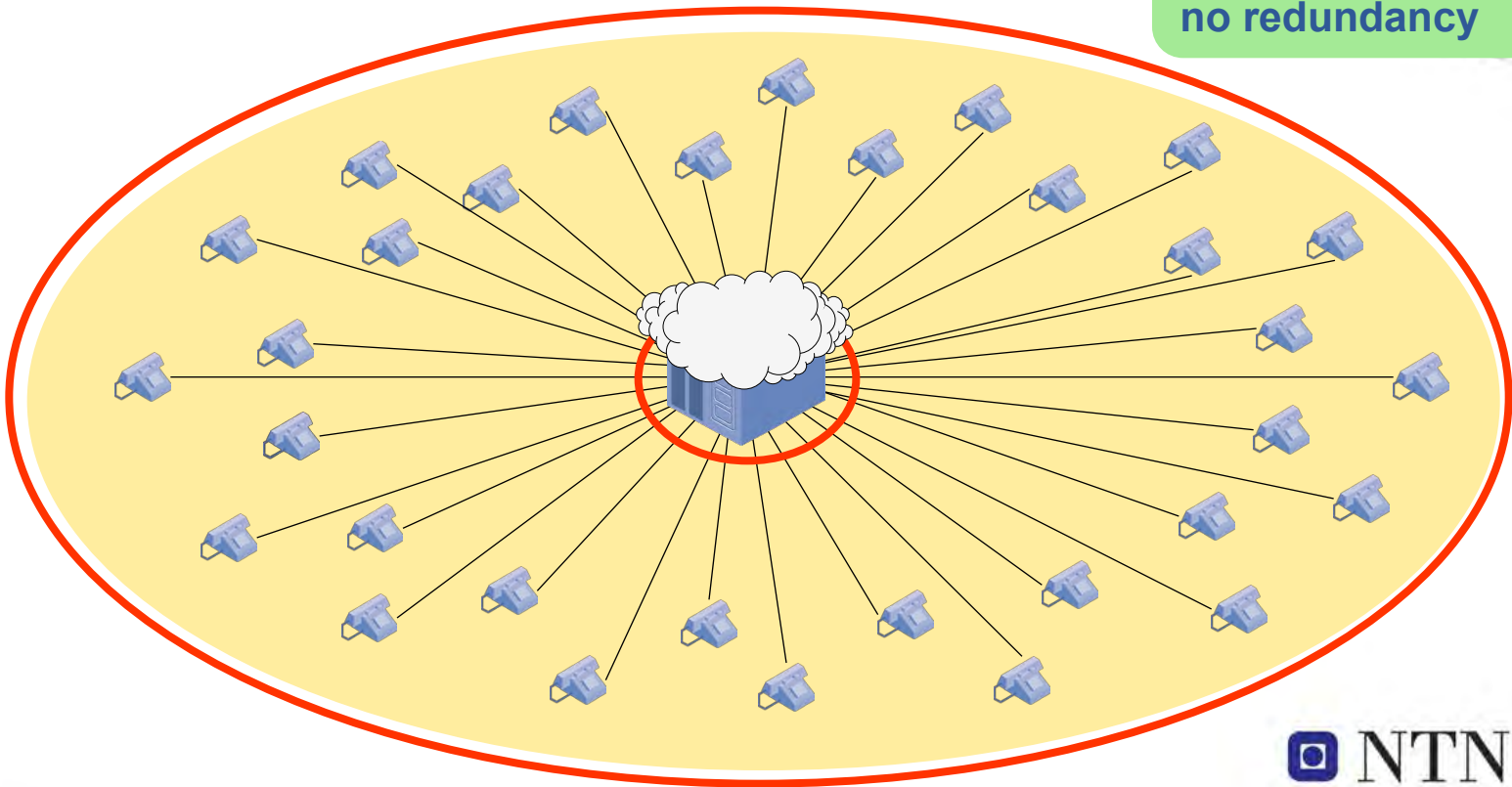


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# Class 5: more problematic

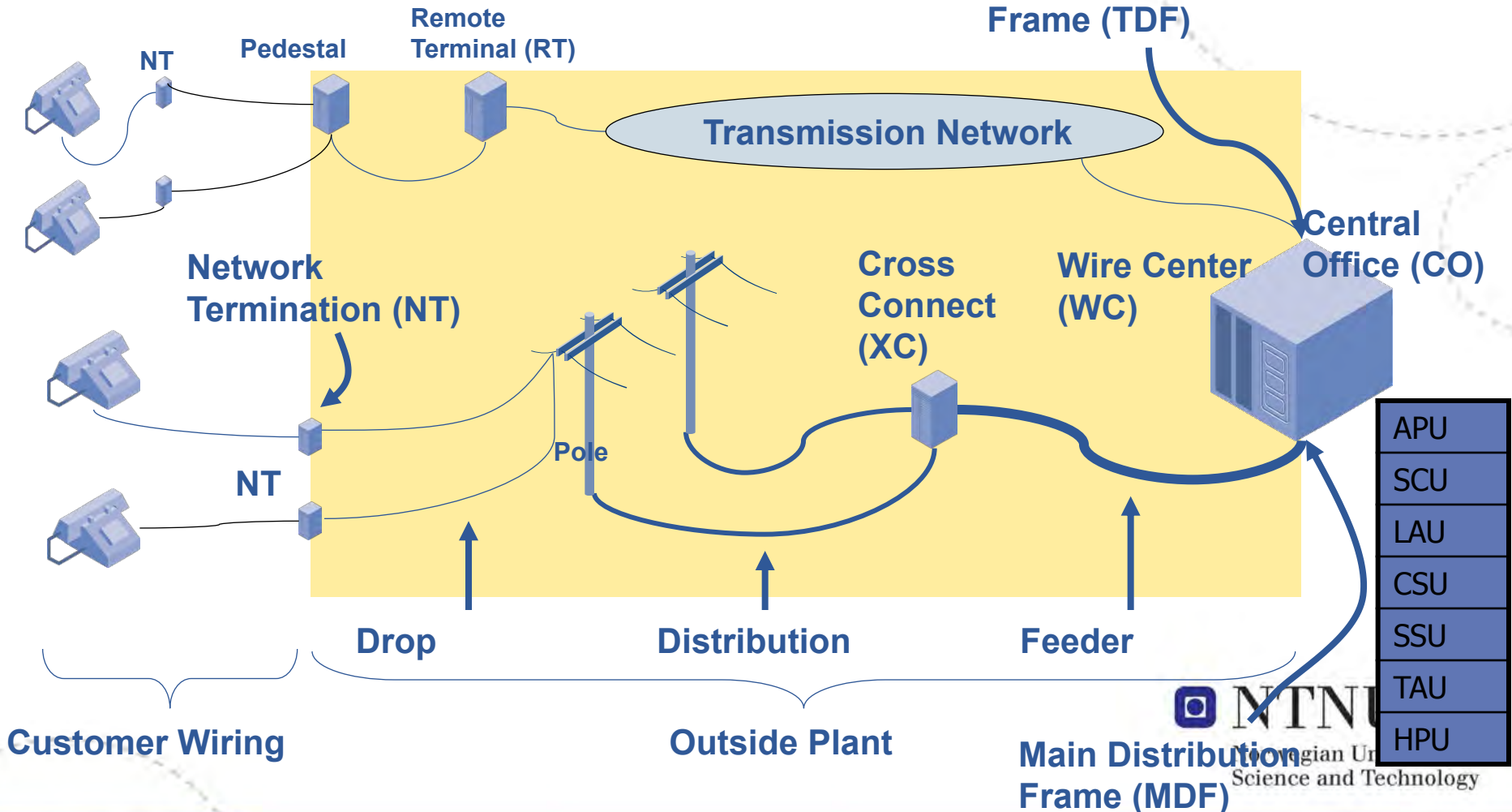
Big impact after loss of a class 5 switch due to no redundancy



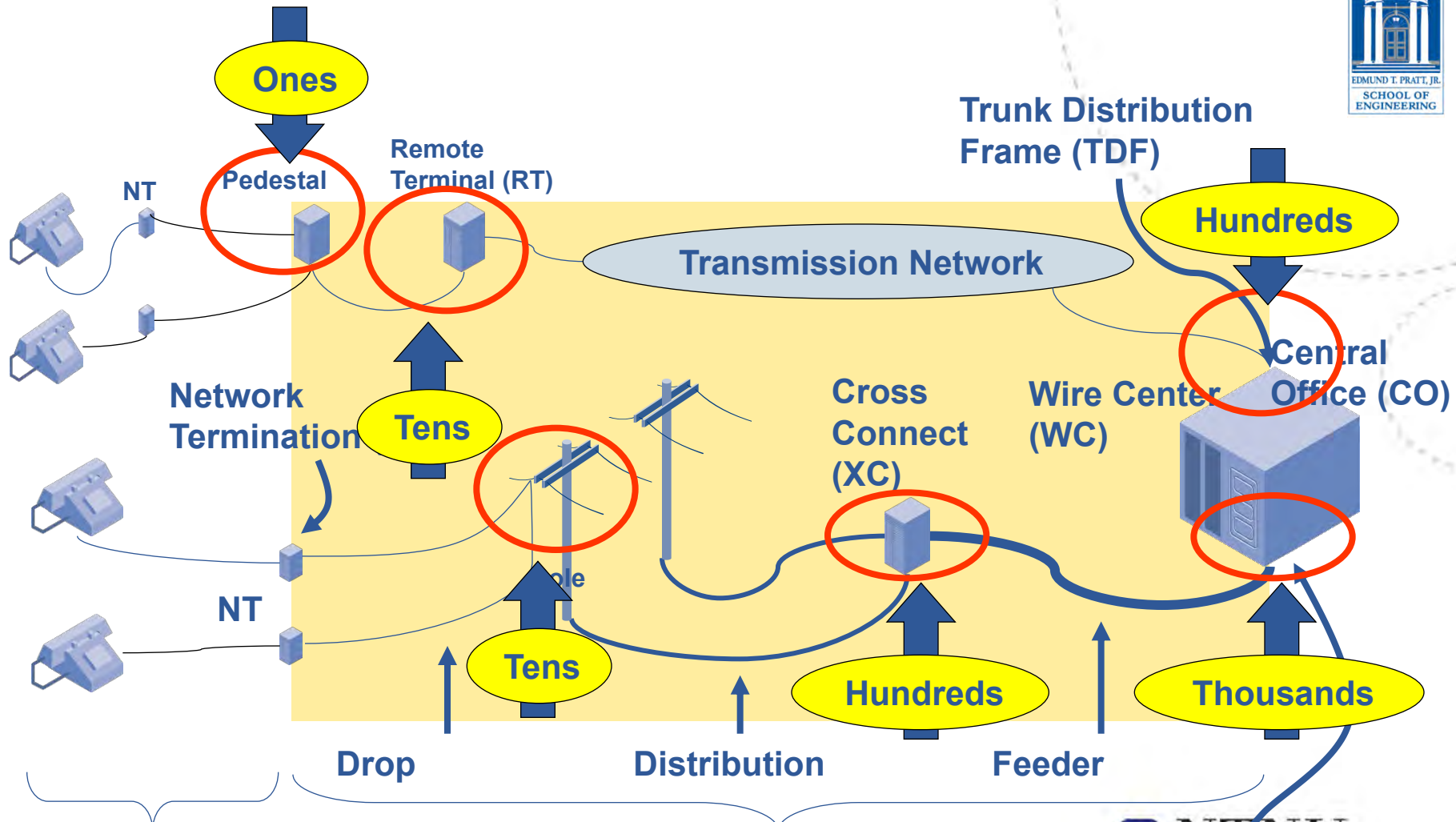
10,000 or more pair of wires meet at a single point

# Telephony terms

LAU	Line Access Unit
CSU	Call Processing Unit
HPU	Central Host Unit



# Increasing wire concentration approaching central office




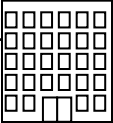

Customer Wiring

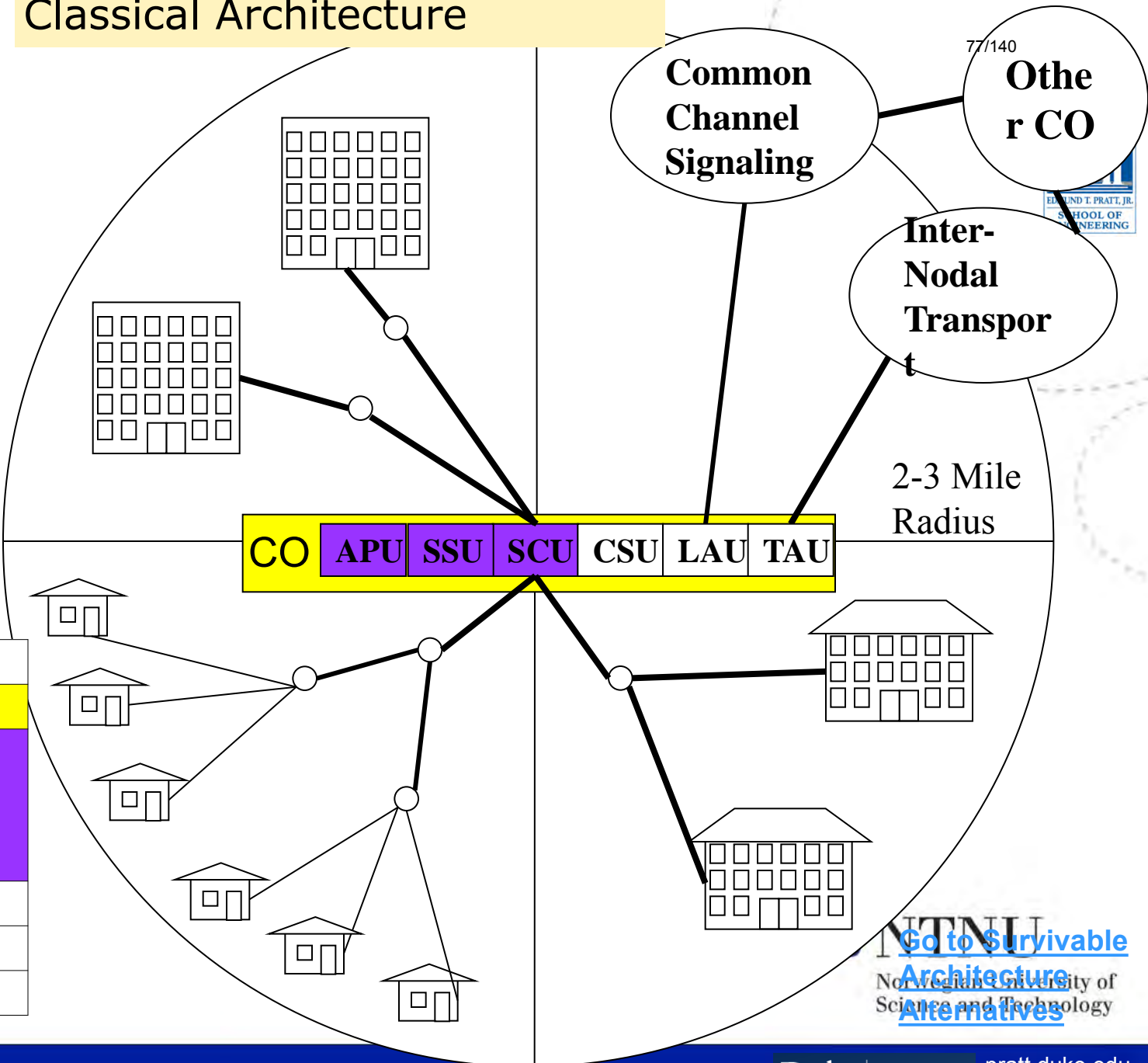
Outside Plant

Main Distribution Frame (MDF)



# Classical Architecture

Symbol	Meaning
○	Wiring Cross-Point
—	Multi-Pair Cable
—	Drop Cable
	Single Family Residence
	Business
	Multi-Family Dwelling



Unit	Type
CO	Central Office
HPU	Host
APU	Administrative
SSU	Signaling
SCU	Communications
CSU	Call Service
LAU	Line Access
TAU	Trunk Access

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**Other CO**



**Inter-Nodal Transport**

2-3 Mile Radius

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[Go to Survivable Architecture Alternatives](http://www.ntnu.no)



# Layered architecture



Layer		Nodal Elements
1	Customer premise equipment and access network	Elements owned by the subscriber and the copper wire network between the subscriber and a telephone company LAU
2	Line cards	Nodal elements providing signal conversion and transport between the subscriber and other layers
3	Call processing	Nodal elements providing call management
4	Transport	Transport equipment such as ADMs, Digital Cross-Connect systems and transmission cables that interconnect nodal elements
5	Central elements	Elements of the digital switch that must remain centralized
6	Trunks	Inter-switch trunks that provide routes between PSTN offices
7	Application	Auxiliary elements that provide services, i.e., voice mail, conference bridges, E9-1-1



[16] V. B. Mendiratta and C. A. Witschorik. Telephone service survivability. In IEEE workshop on the design of reliable communication networks (DRCN2003), October 2003.

# New options for different layers



Layer	Option 1	Option 2	Option 3
1. CPE and Access Network	Direct wire to CO	Shortened loop LAU at or near site	
2. Line Cards (LAU)	RT at or near site	Multiple small LAUs at or near site	
3. Call Processing	Distributed CSU (single switch)	Multi-switch CSU architecture	Emergency CSU/LAU combination
4. Transport	General diversity and redundancy principles apply		
5. Central Elements	Active/Active HPU	Active/Standby HPU	
6. Trunks	General diversity and redundancy principles apply		
7. Application	General diversity and redundancy principles apply		



# HPU Synchronization

- HPU functions include:
  - Management of global resources: intra-switch fabric, trunks, and signaling links
  - Administrative activities: billing, operations support system (OSS) links, and human/machine interaction
- Databases on the standby HPU are kept synchronized with the active HPU through periodic updates and tape backups
  - Line additions/deletions
  - New hardware
  - Dialing plans
  - Subscriber features
  - Outside facilities
- Frequency and integrity of updates determines the time required (syn rate) and the success rate (syn coverage) of restoring the system to a working state after loss of an HPU
- HPU synchronization
  - Near instantaneous with some coverage (A/S I)
  - Delay before service is restored with perfect coverage + all subscribers (A/S II), 50% subscribers (A/A)





# Survivable architecture alternatives

Layer	Classical Architecture	Survivable Architectures		
		A/S I	A/S II	A/A
2. Line Cards	All LAUs at CO	Multiple LAU at or near site		
3. Call Processing	All CSUs at CO	Distributed CSU, Single Switch		
5. Central Elements	All at CO	HPU active/standby	HPU active/standby	HPU active/active
Syn.	-	w/prob. $c$	w/prob. 1	w/prob. 1

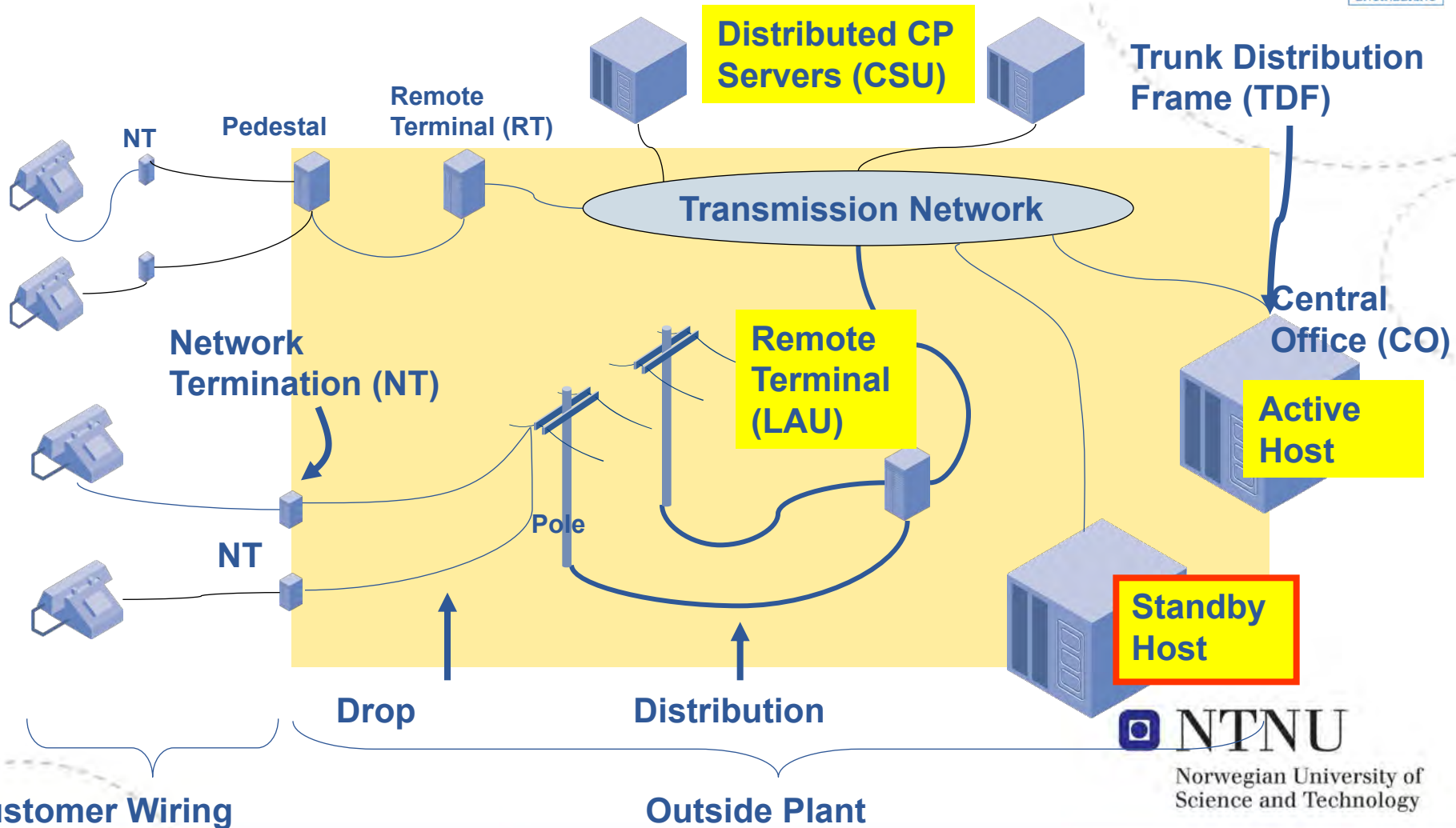
**Active/standby:** the standby HPU takes over all the customers and trunks when the active HPU is destroyed in a disaster

**Active/active:** load sharing, each HPU serves half customers with half trunks

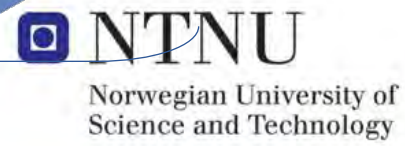
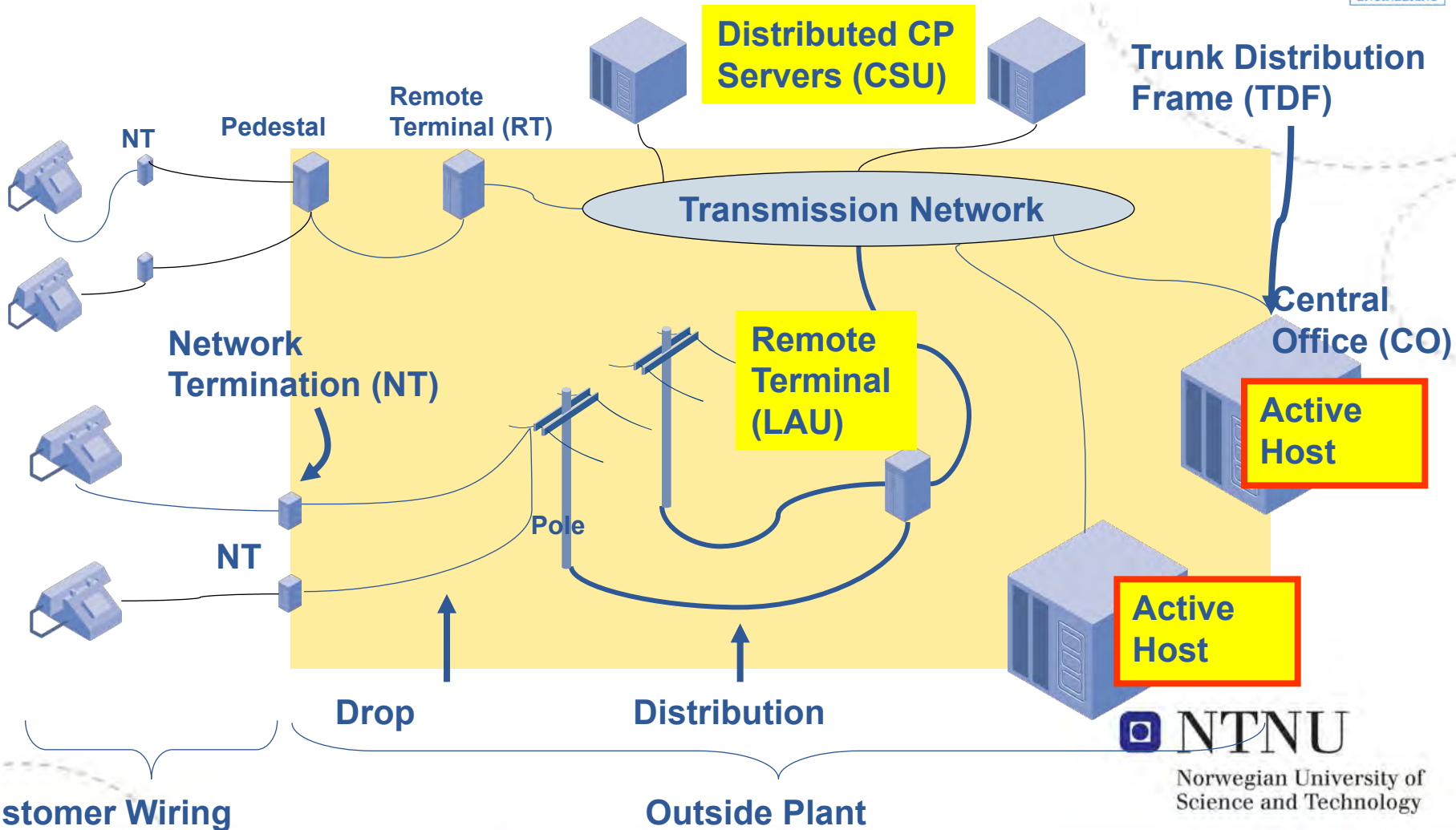


# Architecture A/S I, A/S II: Reduce Length of Copper Loops

Distribute Call Processing + Active/Standby Host



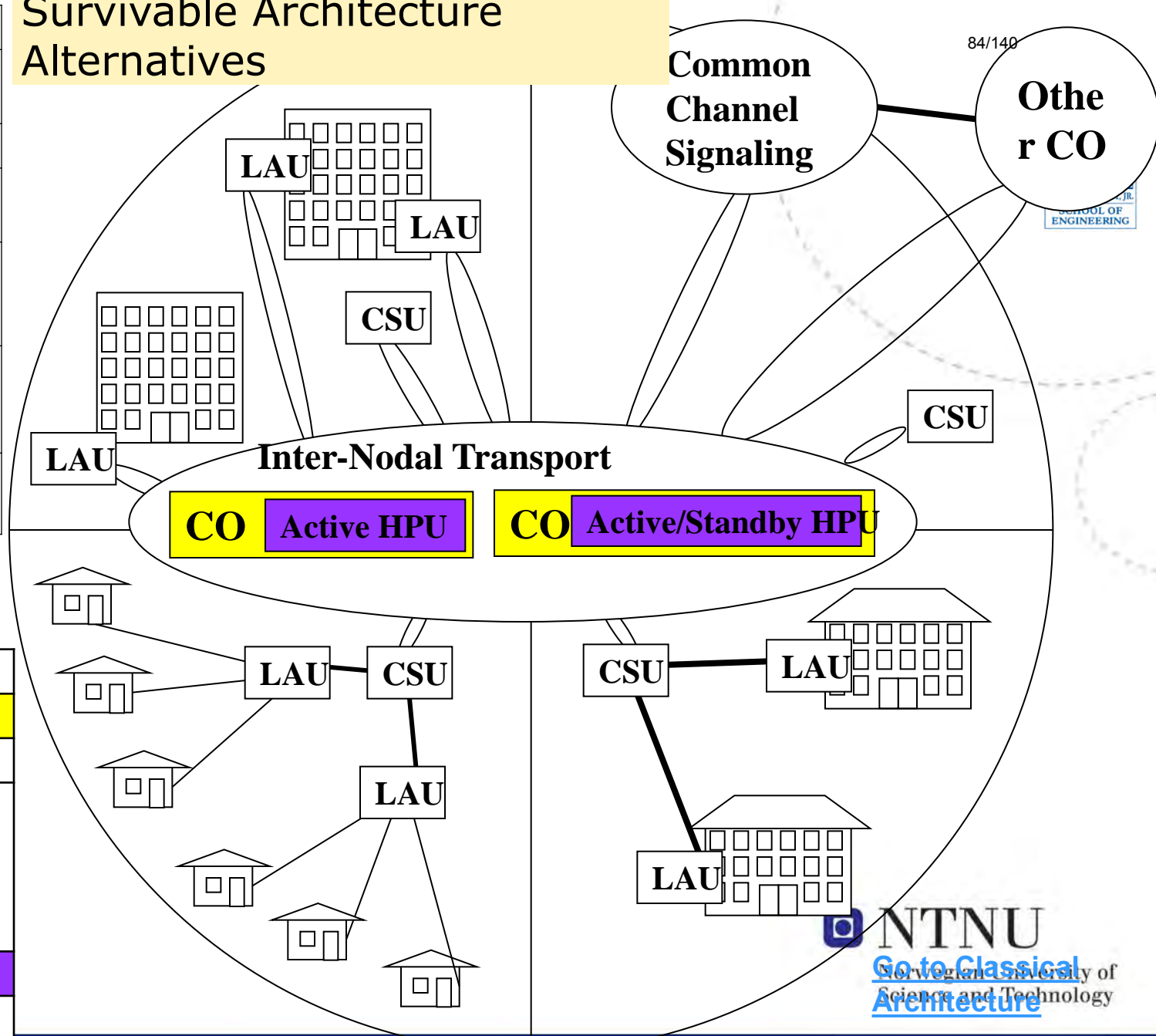
# Architecture A/A: Reduce Length of Copper Loops + Distributed Call Processing + Active/Active Host



# Survivable Architecture Alternatives

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Symbol	Meaning
	Multi-Pair Cable
	Drop Cable
	Protected Cable
	Single Family Residence
	Business
	Multi-Family Dwelling



Unit	Type
CO	Central Office
APU	Administrative
CSU	Call Service Communications Signaling Trunk Access
HPU	Host Processing
LAU	Line Access

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# Architectures A/S I, A/S II, A/A

- Distributed CSU
  - Maintain basic service ( $r_b \times 100\%$  of total traffic) when HPU fails
  - Reduced capacity ( $r_r \times 100\%$  of total trunks) for basic service
- Redundant HPU
  - Active/standby A/S I
    - Switchover coverage
    - Synchronization probability
  - Active/standby A/S II
    - Switchover coverage
    - Synchronization delay ( $r_p \times 100\%$  of customers get service before synchronization)
  - Active/active A/A
    - Load sharing, each serves half subscribers
    - Switchover coverage
    - Synchronization delay ( $r_p \times 100\%$  of customers get service before synchronization)
- Failure scenario
  - Loss of one active HPU



# System parameters

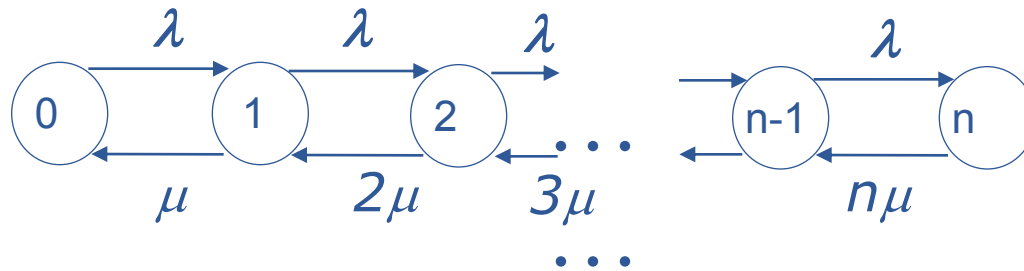
- Total capacity  $n$ : 10000 trunks
- Call arrival rate  $\lambda$ : 100 / sec<sup>-1</sup>
- Mean call holding time  $\mu^1$ : 100 seconds
- Disaster rate  $\lambda_f$ : 1 / year<sup>-1</sup>
- Mean detection time  $\delta_d^{-1}$ : 1 second
- Mean switchover time  $\delta_r^{-1}$ : 60 seconds
- Switchover coverage of architecture A/S I, A/S II  $q$ : 0.9
- Switchover coverage of architecture A/A  $v$ : 0.9
- Syn. probability  $c$ : 0.99
- Mean syn. time  $\delta_s^{-1}$ : 10 minutes
- Mean manual recovery time  $\mu_r^{-1}$ : 2 hours
- Mean manual repair time  $\mu_R^{-1}$ : 10 days
- Mean reconfiguration time  $\beta^1$ : 10 minutes
- Partial service probability  $r_p$ : 0.99
- Basic traffic percentage  $r_b$ : 0.4
- Local trunk facility percentage  $r_r$ : 0.4





# Pure performance model

What happens before the occurrence of failure?



Steady state closed-form solution:  
Erlang B Formula

$$\pi_j = \frac{(\lambda/\mu)^j / j!}{\sum_{k=0}^n (\lambda/\mu)^k / k!}$$

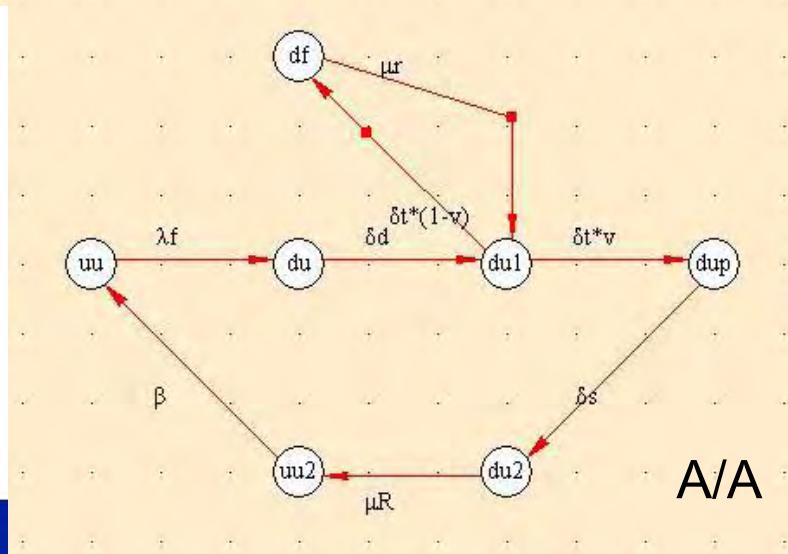
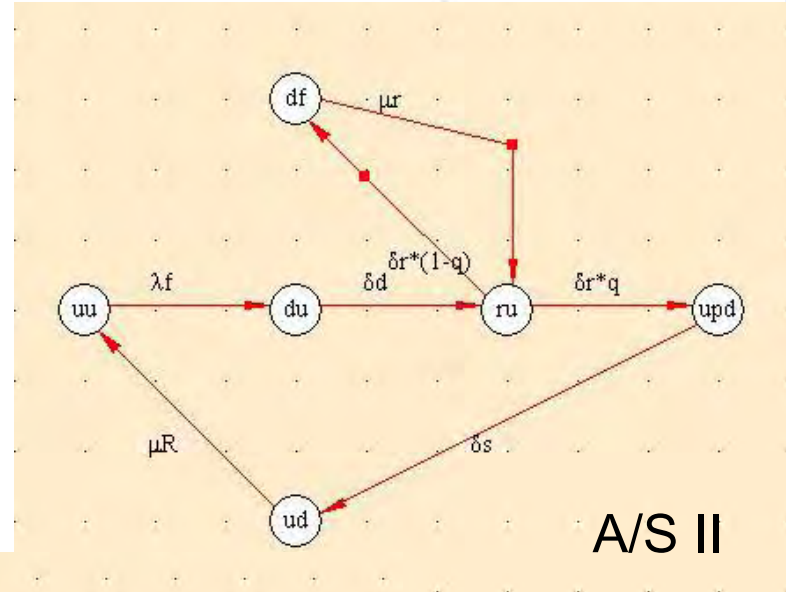
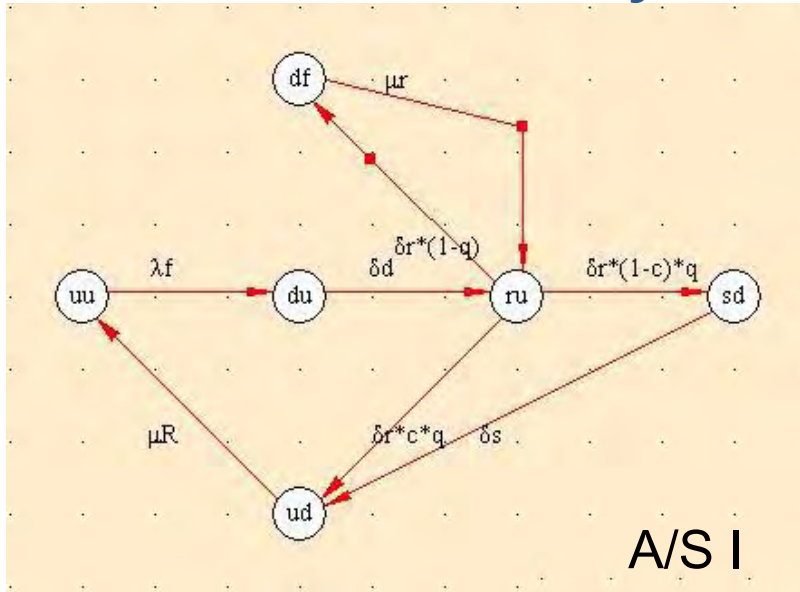
Blocking probability:

$$P_{bk} = \pi_n$$

Expected number of calls in the system:

$$\sum_{k=0}^n k \pi_k$$

# Pure availability models: A/S I, A/S II, A/A





# Pure performance analysis:

blocking probability  $P_{bk}$

State	A/S I	A/S II	A/A
(u,u)	0.0079366	0.0079366	0.01120
(u,d)	0.0079366	0.0079366	-
(d,u)	0.6050	0.6050	0.3056
(r,u)	0.6050	0.6050	-
(d,f)	0.6050	0.6050	0.6050
(s,d)	0.6050	-	-
(u <sub>p</sub> ,d)	-	0.08829	-
(d,u <sub>2</sub> ),(u,u <sub>2</sub> )	-	-	0.007937
(d,u <sub>1</sub> )	-	-	0.3056
(d,u <sub>p</sub> )	-	-	0.008045



# Pure availability analysis: steady state

- Steady state availability

- A/S I

- Up states: uu, ud
- Down states: du, df, ru, sd
- $P_{\text{coA}} = P(\text{uu}) + P(\text{ud}) = 0.999994$

- A/S II

- Up states: uu, ud    Partial up state: upd
- Down states: du, df, ru
- $P_{\text{coA}} = P(\text{uu}) + P(\text{ud}) + P(\text{upd}) * r_p = 0.999992$

- A/A

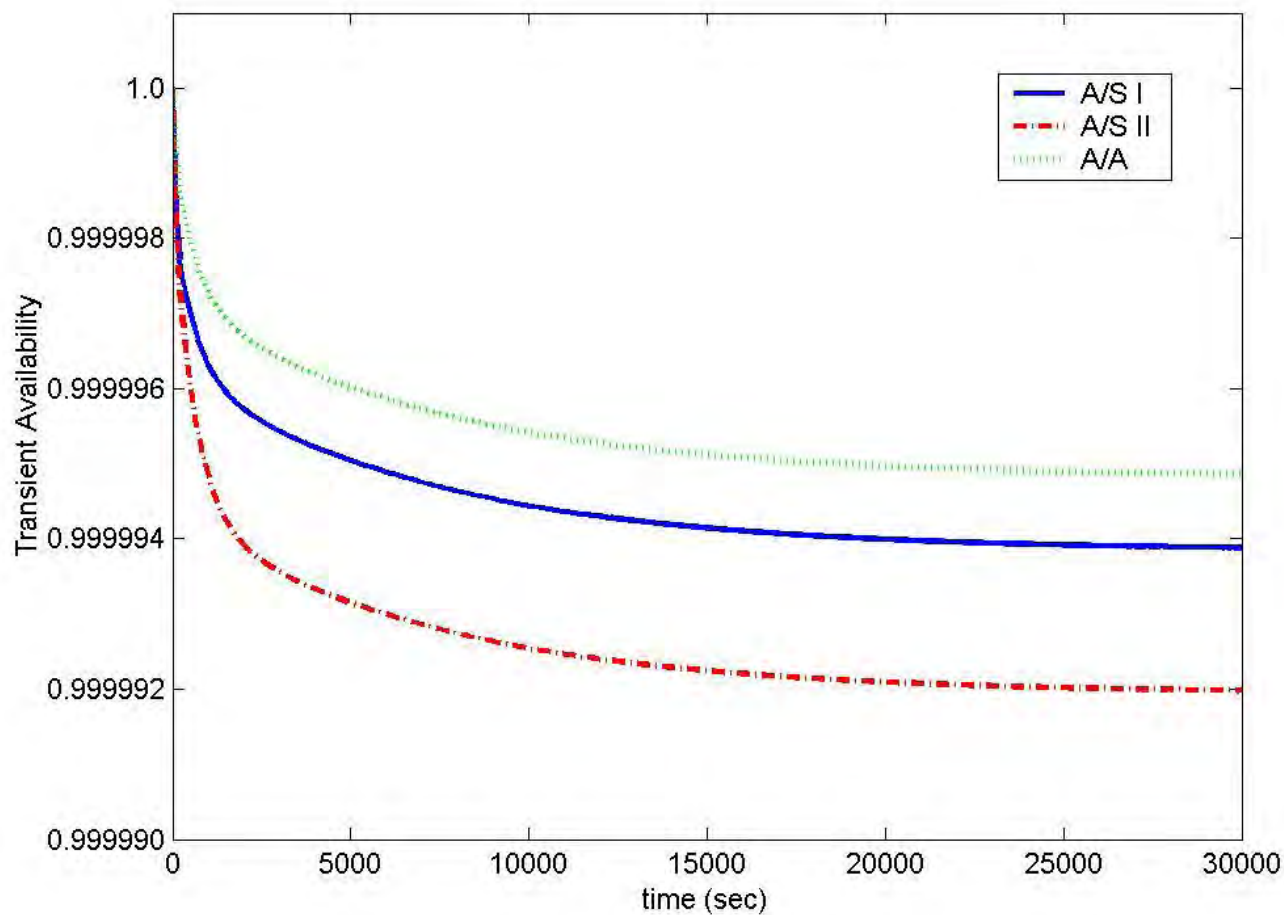
- Up states: uu, uu2, du2    Partial Up State: du, du1, dup
- Down states: df
- $P_{\text{coA}} = P(\text{uu}) + P(\text{uu2}) + P(\text{du2}) + P(\text{du}) * 0.5 + P(\text{du1}) * 0.5 + P(\text{dup}) * (0.5 + r_p / 2) = 0.999995$

- Expected Downtime

- A/S I: 3.15 minutes per year
- A/S II: 4.20 minutes per year
- A/A: 2.63 minutes per year

Availability hereinafter means capacity-oriented availability (COA),  $P_{\text{COA}} = 1$  means full capacity

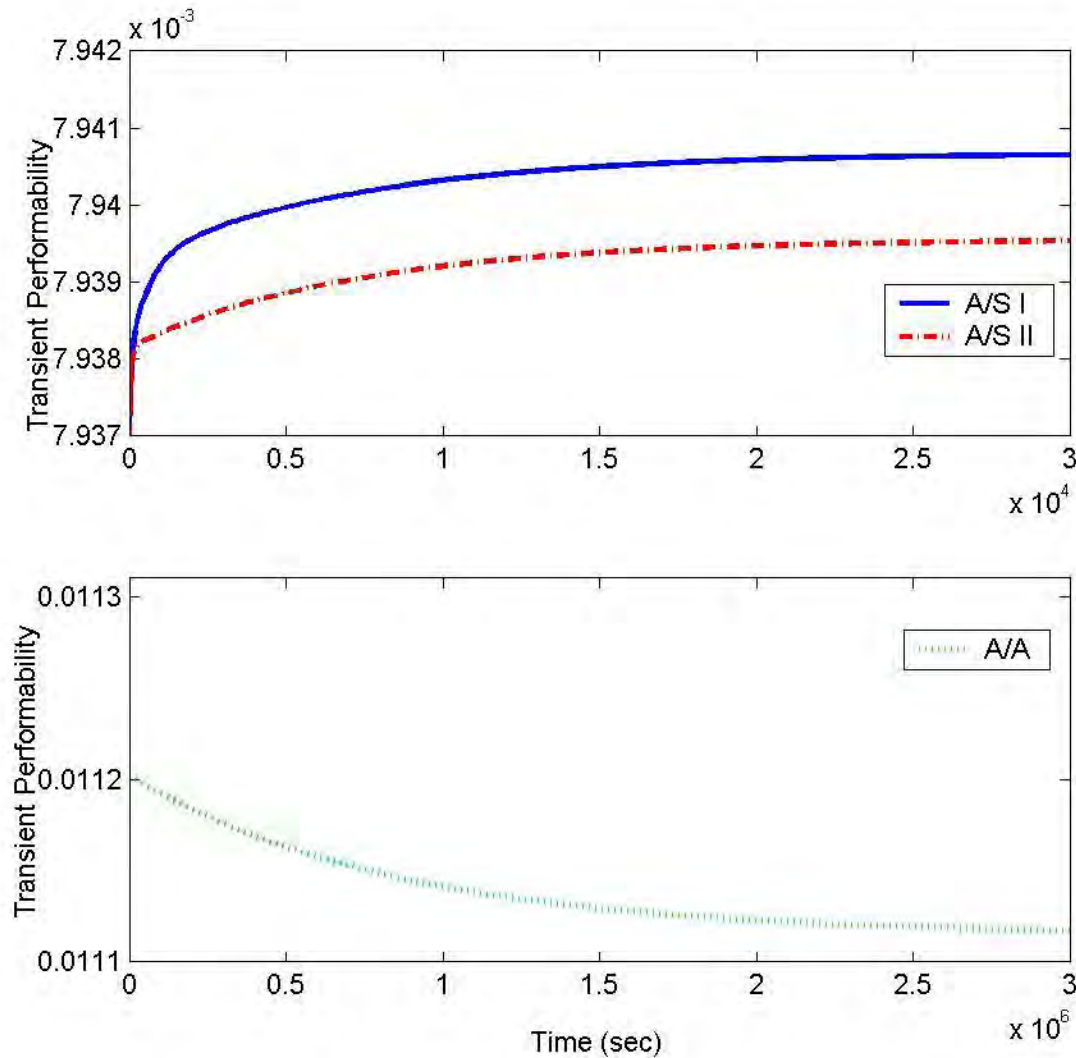
# Pure availability analysis: transient







# Performability results



Steady state:

A/S I: 0.0079404

A/S II: 0.0079393

A/A: 0.01115

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# Model modification for survivability definition: A/S I

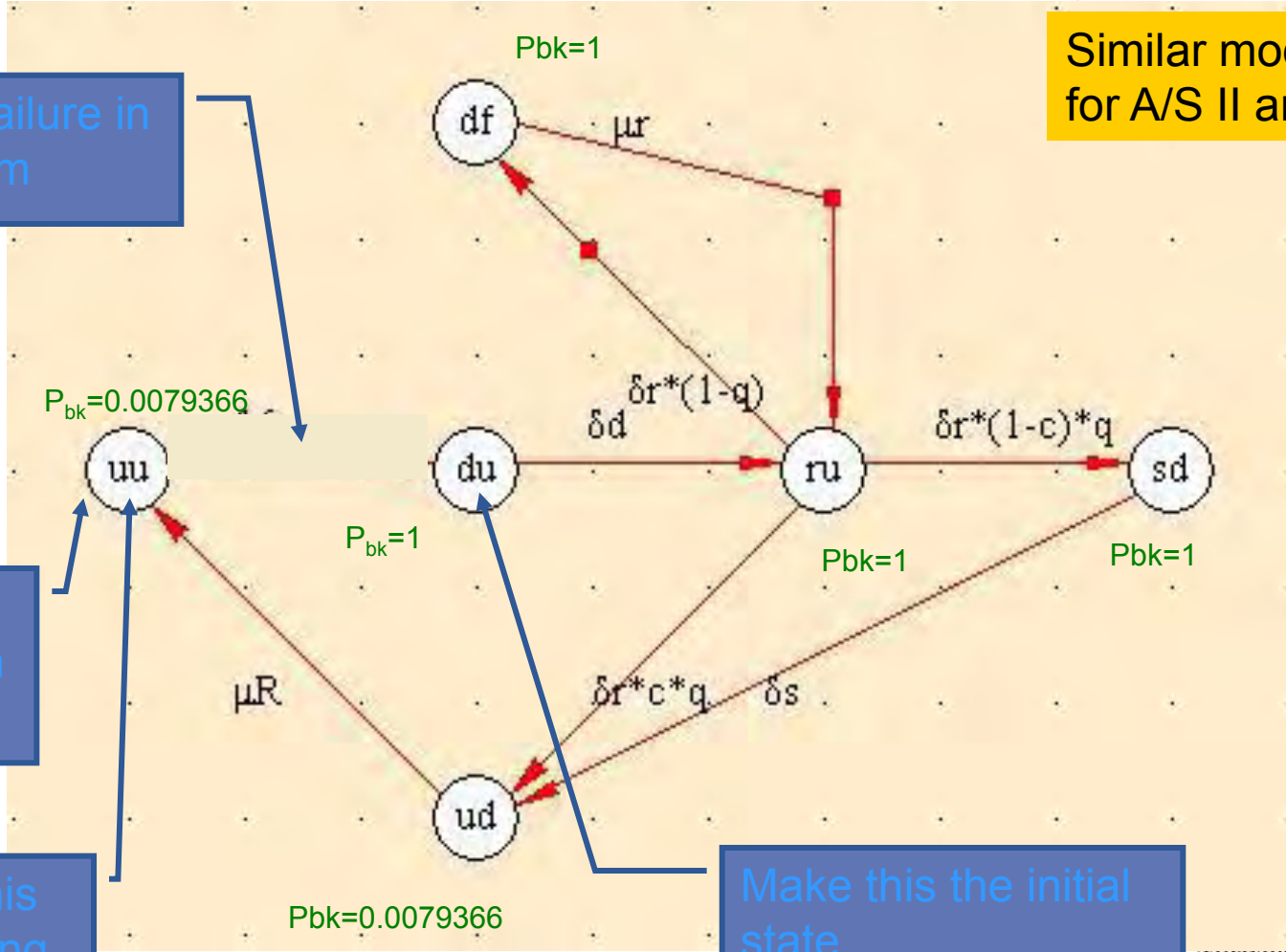
Similar modification for A/S II and A/A

Force a failure in the system

Normally operating in this state

Make this Absorbing state

Make this the initial state

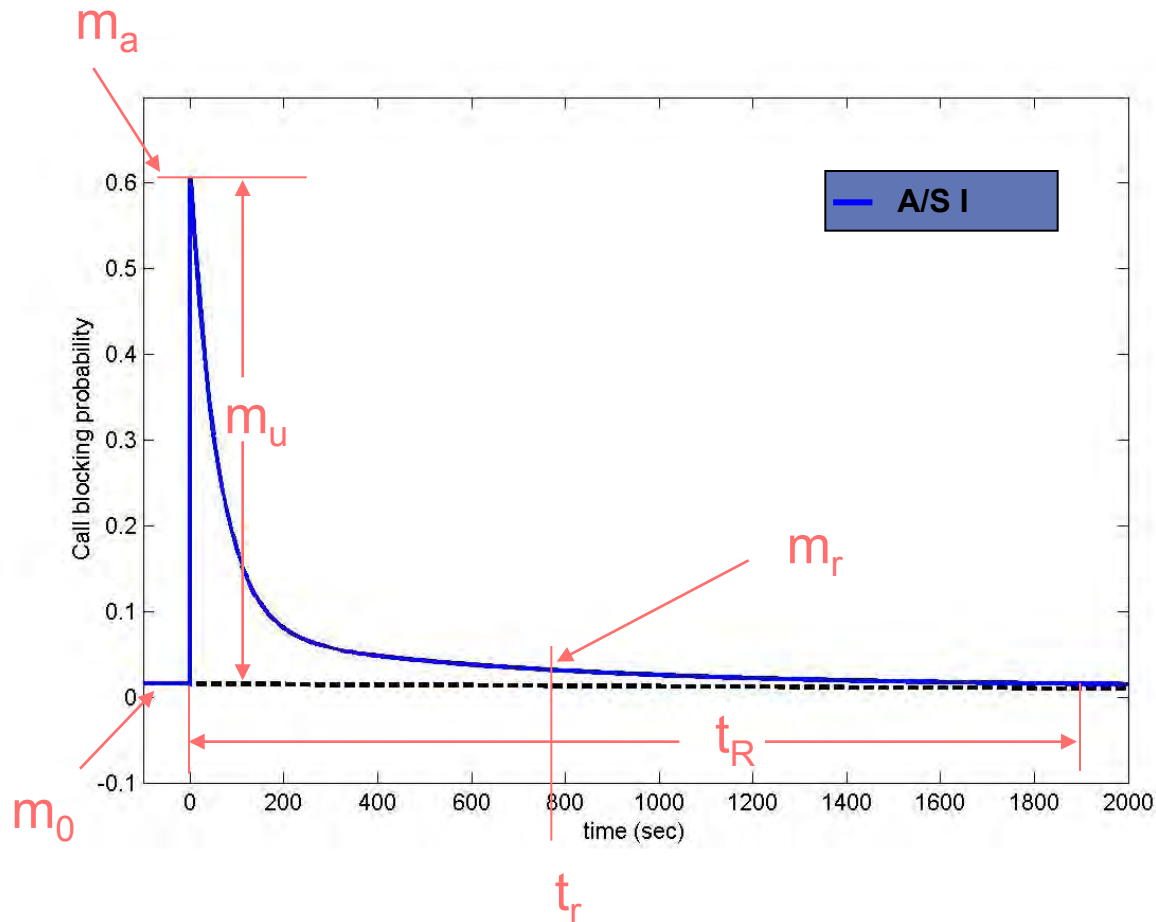




# Implication of the modification

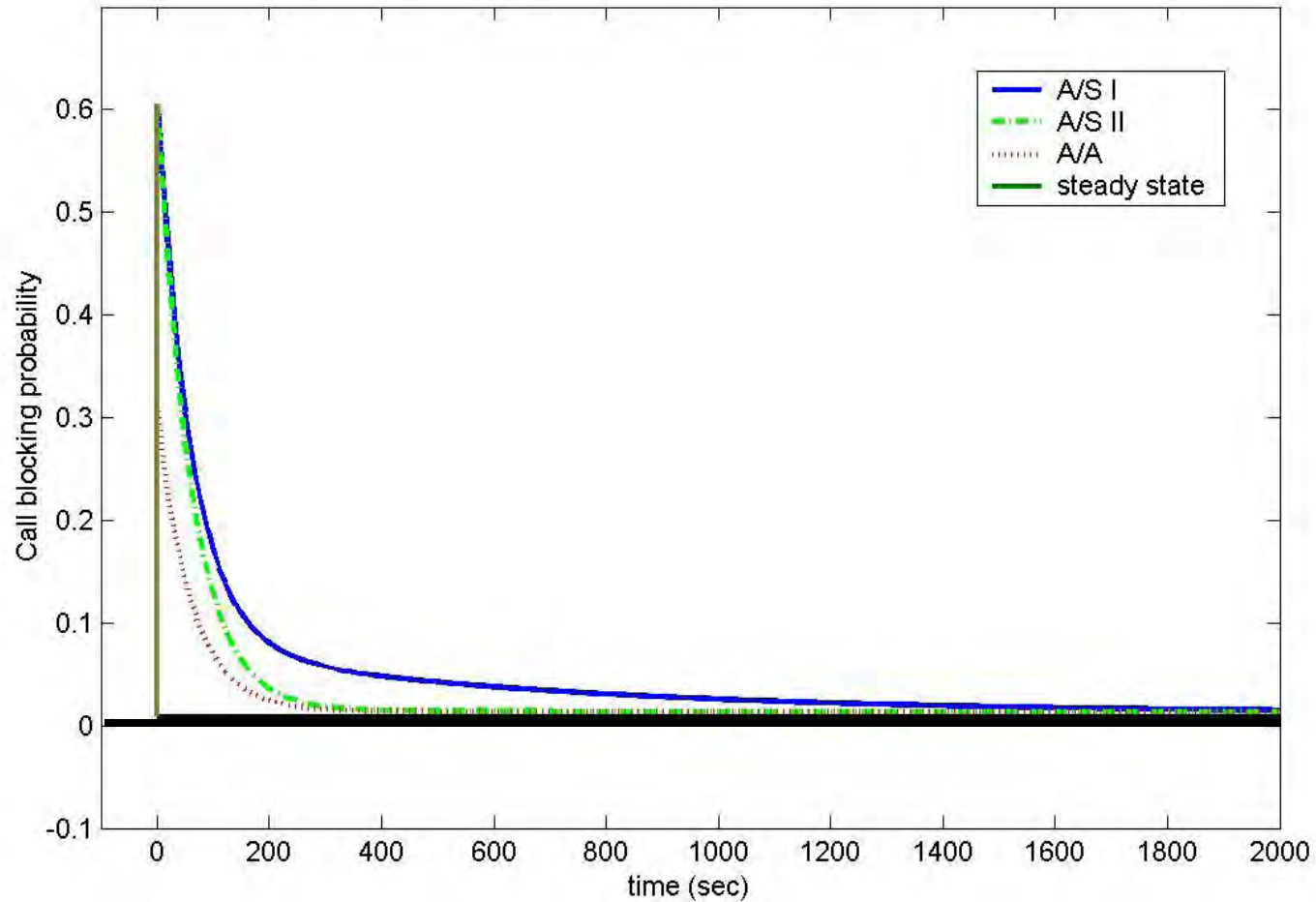
- What does it mean when transition ( $\lambda_f$ ) is removed?
  - A failure is injected into the system
  - All the system survivability measures do **not** depend on the value of  $\lambda_f$
  - All previous performance/availability/performability measures and the first two survivability measures do depend on the value of  $\lambda_f$
  - It is usually difficult to have agreement on the value of  $\lambda_f$  in practice. Therefore, those measures depending on  $\lambda_f$  are controversial.
  - This is the reason why only the T1A1.2 definition gives an important, useful and novel survivability measure.

# Survivability results: A/S I



- 0 sec  
 $P_{bk} = 0.6050 = 76.2 \times P_{bk} (uu)$
- 10 sec  
 $P_{bk} = 0.5309 = 66.9 \times P_{bk} (uu)$
- 10 min  
 $P_{bk} = 0.0378 = 4.76 \times P_{bk} (uu)$
- 1 hr  
 $P_{bk} = 0.01183 = 1.49 \times P_{bk} (uu)$
- 10 hr  
 $P_{bk} = 0.00798 = 1.005 \times P_{bk} (uu)$

# Survivability results



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# Survivability results



	A/S I	A/S II	A/A
$m_0$	0.007937	0.007937	0.01120
$m_a$	0.6050	0.6050	0.3056
$m_u$	0.5971	0.5971	0.2944
$m_{rr}$ ( $t_r=10$ sec)	0.5309	0.5229	0.2602
$m_{rr}$ ( $t_r=10$ min)	0.03778	0.01391	0.01356
$m_{rr}$ ( $t_r=10$ hr)	0.01183	0.01164	0.01163
$t_R^*$	31610 sec	31550 sec	4300 sec

\*A relative error 1% is assumed for calculating  $t_R$



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# Comparison – ELF



	Call loss due to failure	Extra call loss due to blocking	ELF
A/S I	9920	11874	21794
A/S II	9920	8436	18266
A/A	4944	2465	7409



# Survivability ranking

	A/S I	A/S II	A/A
$P_{full}^*$	3	2	1
$E[N]$	3	2	1
$N_{0\%}$	3	2	1
$m_a^*$	3	2	1
$m_r^*$ t=10 min	3	2	1
$m_r^*$ t=1 hour	3	2	1
$t_R$	3	2	1
ELF	3	2	1

$P_{full}$  is the steady state prob. of providing full service

$m_a^*$ ,  $m_r^*$  are relative values with respect to  $p_{bk}(uu)$



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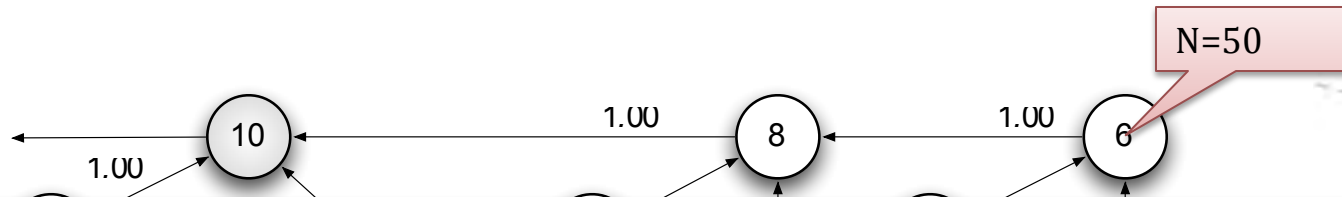
# Interpretation of results



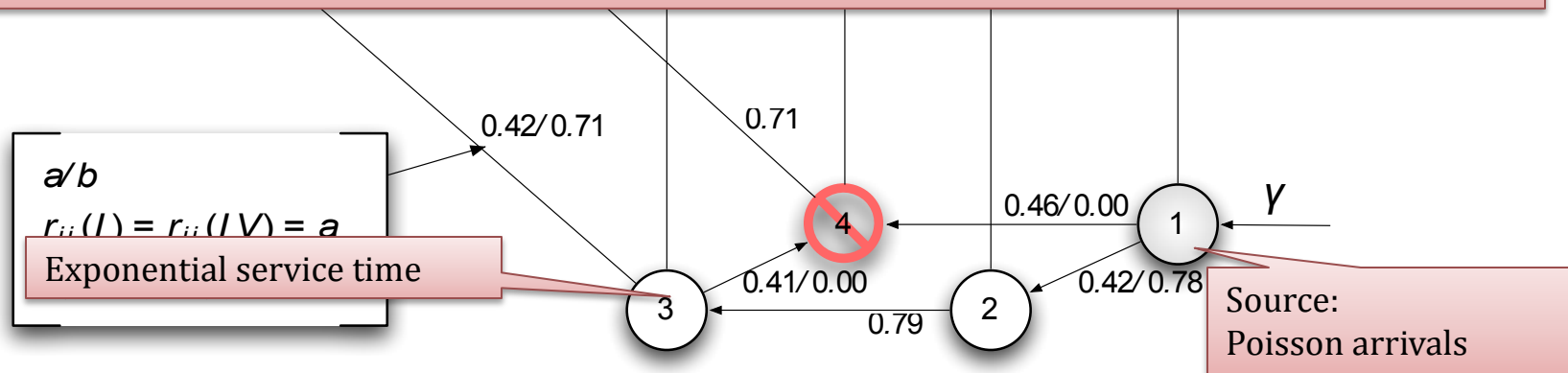
- Active/active A/A offers the best survivability in most cases
  - however, it is most complex and costly in terms of development and operation
  - also requires changes to the signaling network
- Active/standby A/S II offers better survivability than active/standby A/S I
  - this is due to the synchronization delay associated with A/S I
  - A/S II is a more realistic scenario
- Architecture can be chosen by different criteria
- There are tradeoffs between survivability, cost, and operations complexity
- Architecture choice also depends on subscriber type
  - Residential
    - desirable to have basic service in shortest time for all customers after a disaster event
  - Business or government
    - desirable to have full service to a certain group of customers immediately after a disaster event
  - Precedence and preemption schemes can be implemented to give priority of service to govt and service personnel
    - gives priority subscribers better probability of call completion after a disaster event
- Finally, the choice of architecture depends on the loss scenarios that are important



# Objectives and target system



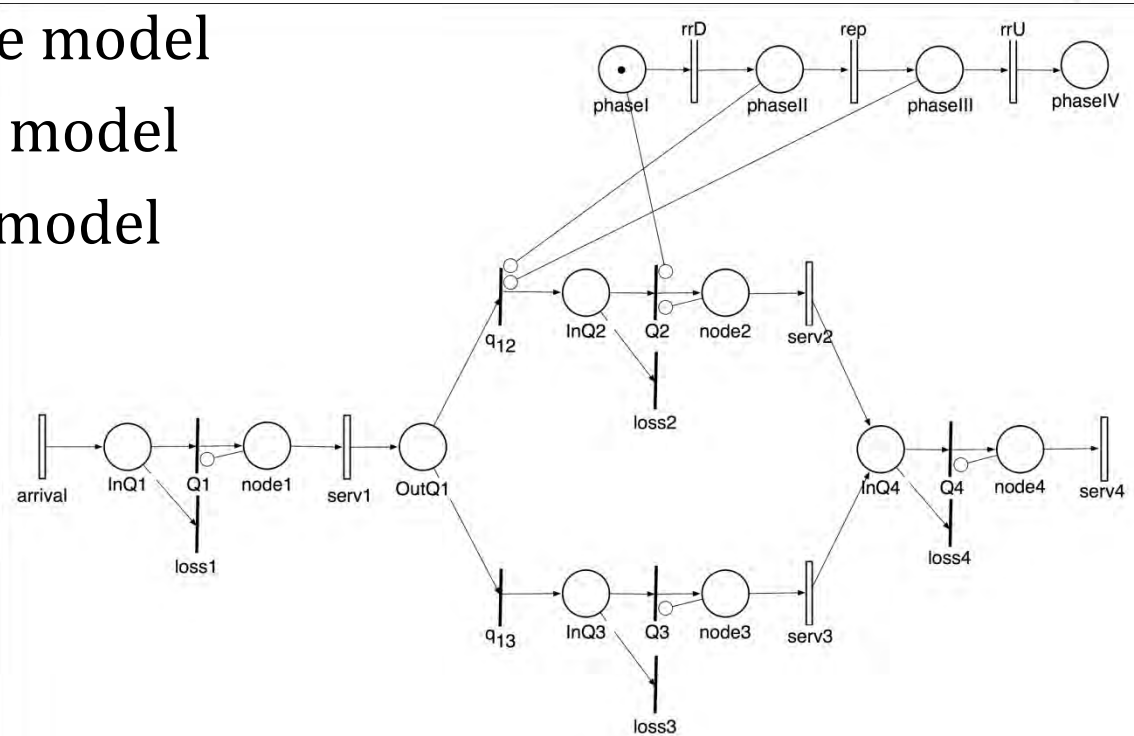
- Transient performance in networks with virtual connections
- From occurrence of an undesired event until steady state operation is restored
- Goal: Survivability model of performance after network failure(s)

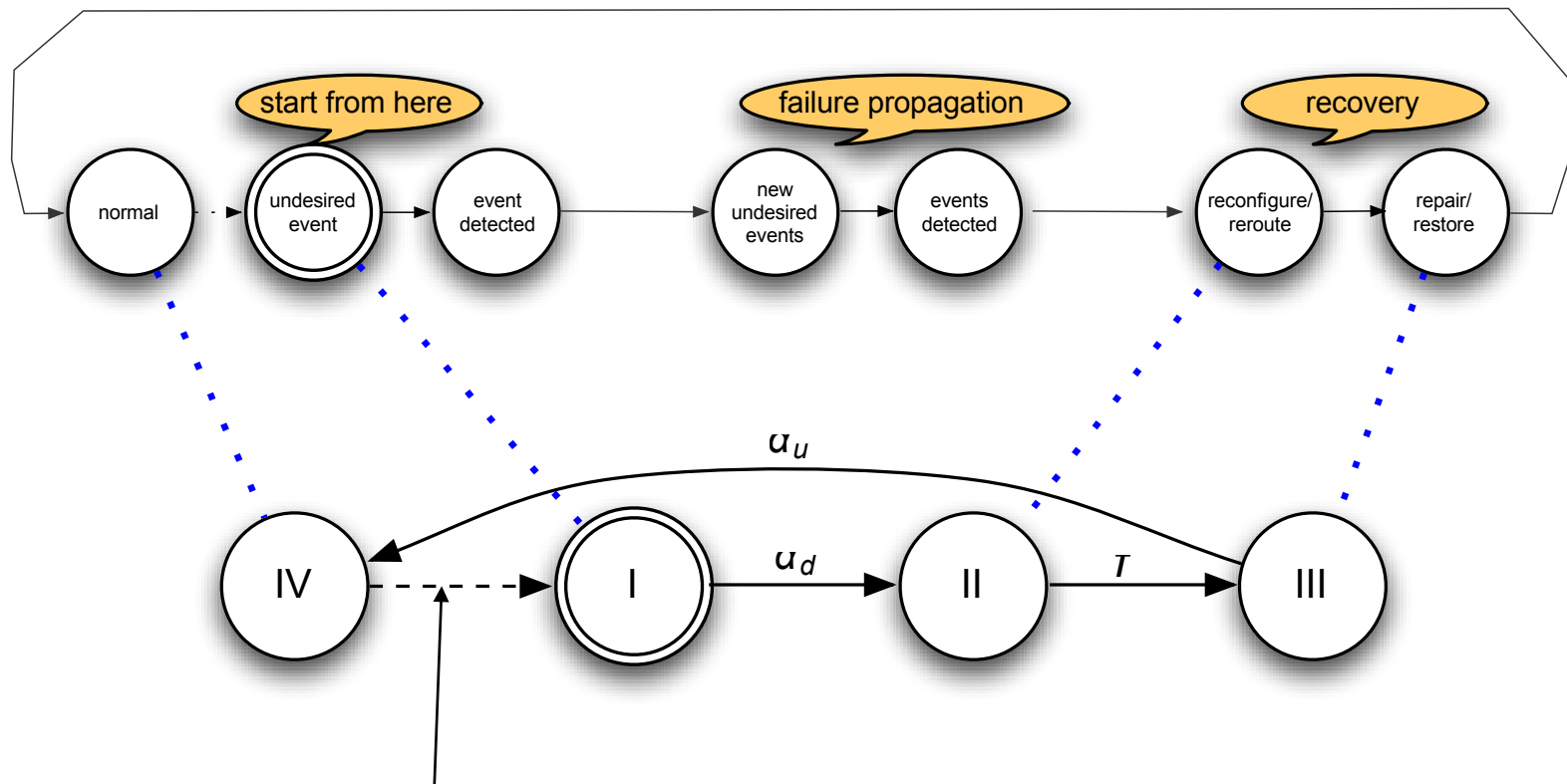




# Network survivability models

- Phased recovery model
- Modeling approach
- Complete composite model
- Space-decomposed model
- Time-decomposed model



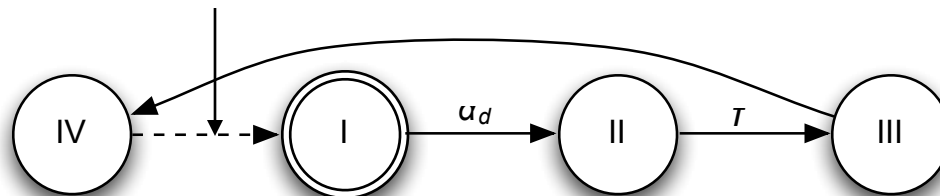




# Phased recovery model

- Phase I:
  - Rerouting after failure is  $T_D \sim \exp(\langle \lambda_D \rangle)$
- Phase II:
  - Restoration time is  $T_R \sim \exp(\lambda)$
- Phase III:
  - Rerouting after failure is  $T_U \sim \exp(\langle \lambda_U \rangle)$
- Phase IV:
  - Fault free network with default routing

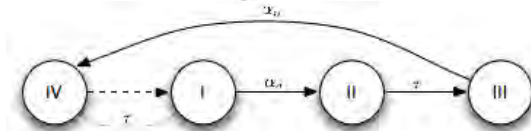
Undesired event is node failure



# Modeling approach



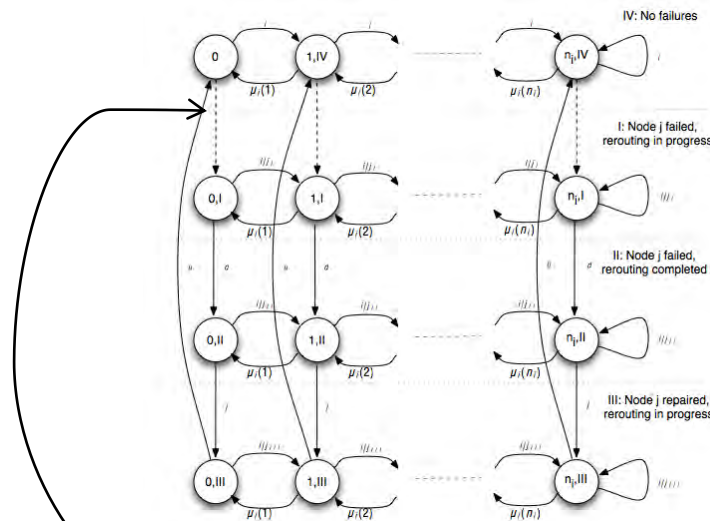
Performance model



Phased recovery model



Composite perfrmability model



Survivability model

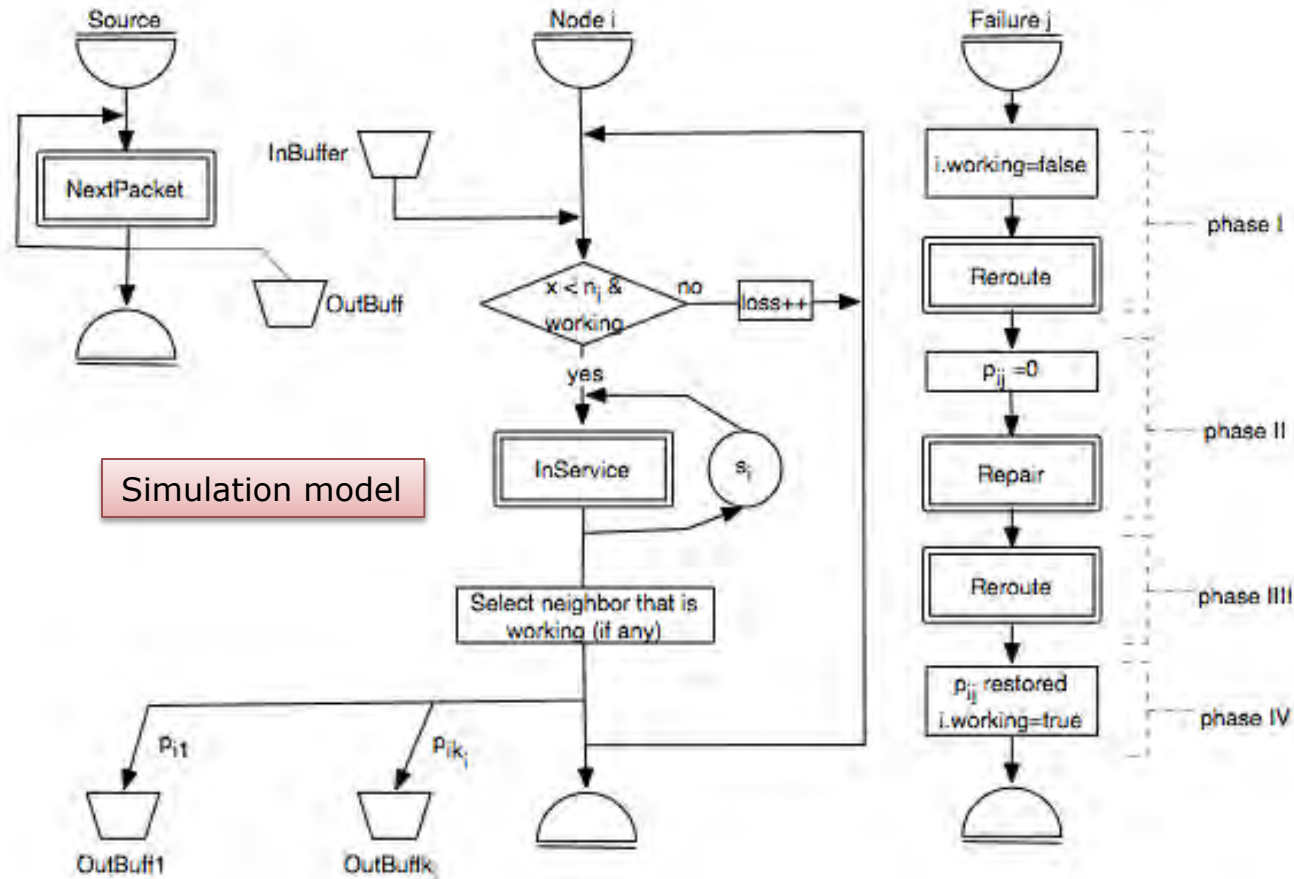


# Complete composite model

- Simulation
  - DEMOS/Simula
  - Discrete event, process-oriented simulation model
- Analytical
  - SRN: Stochastic Reward Nets
  - Full CTMC
  - Solved by SPNP and SHARPE



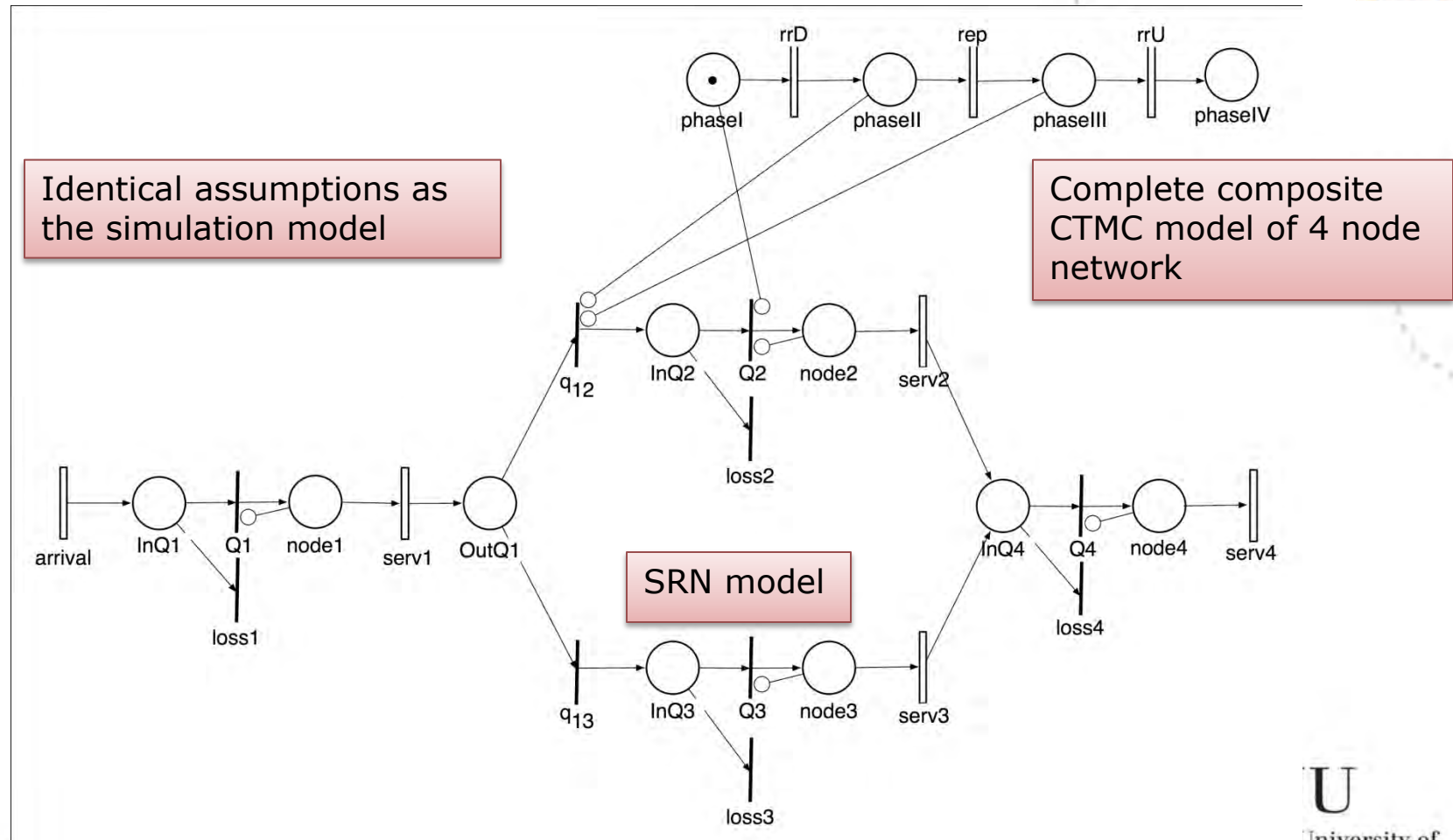
# Complete composite model



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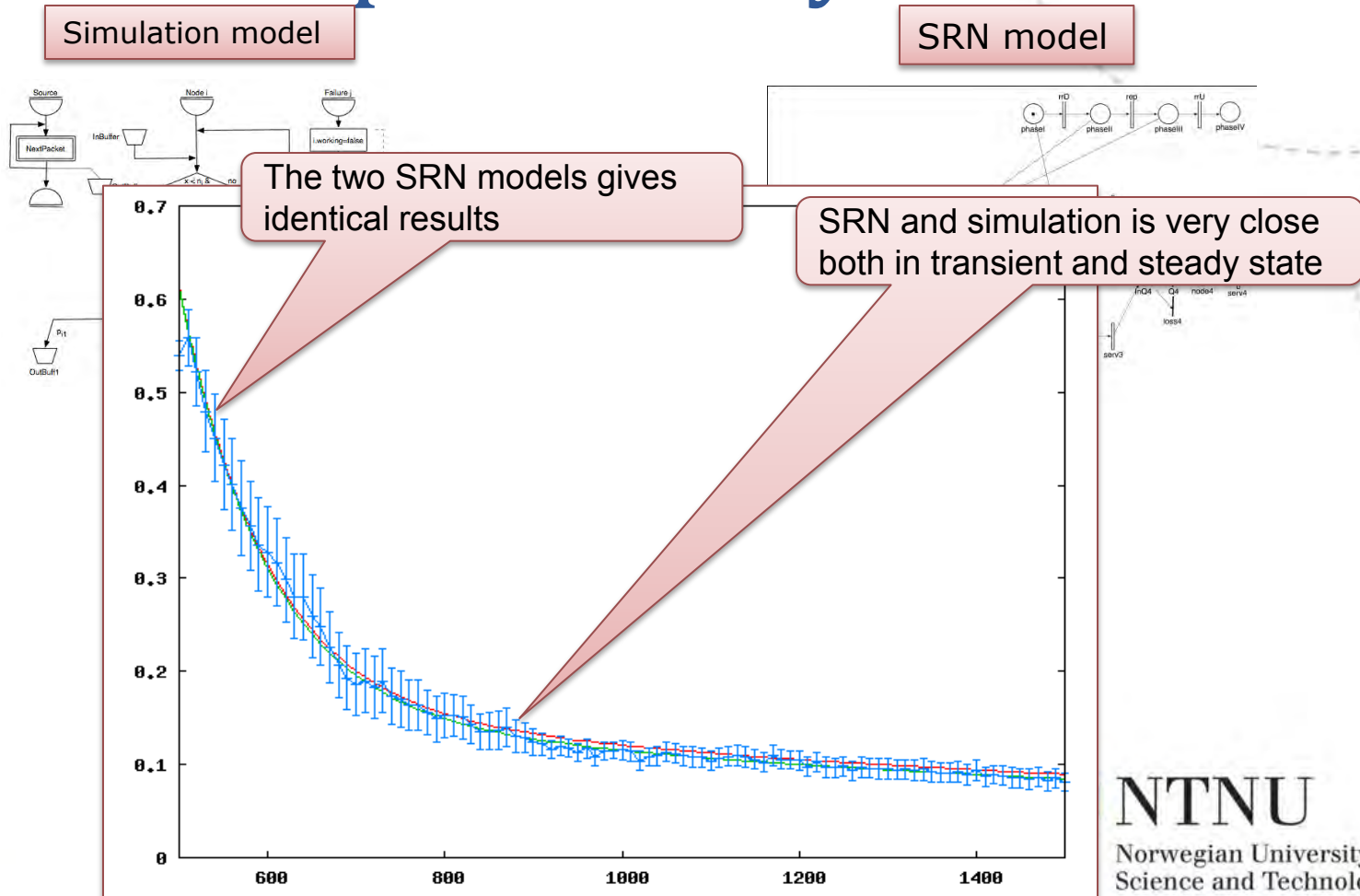
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# Complete composite model





# Numerical example: packet loss probability

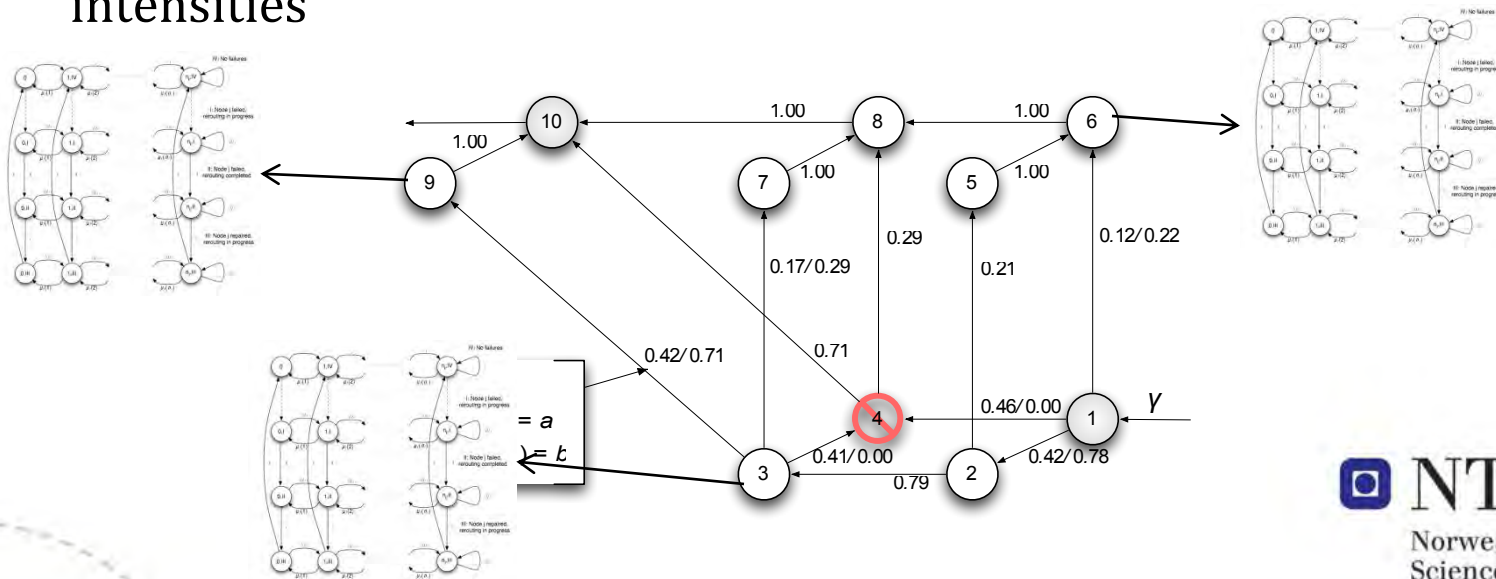


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Science and Technology



# Space-decomposed model

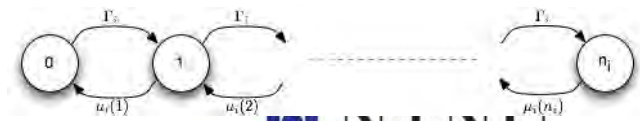
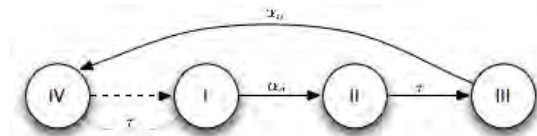
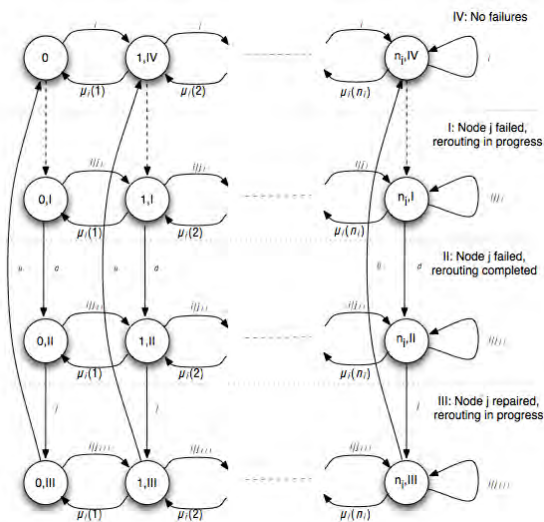
- Decomposed CTMC to reduce number of states
- Nodes modeled separately
- The arrival intensities change when node or link fails
- The resource utilization model below is solved for each set of intensities





# Time-decomposed model

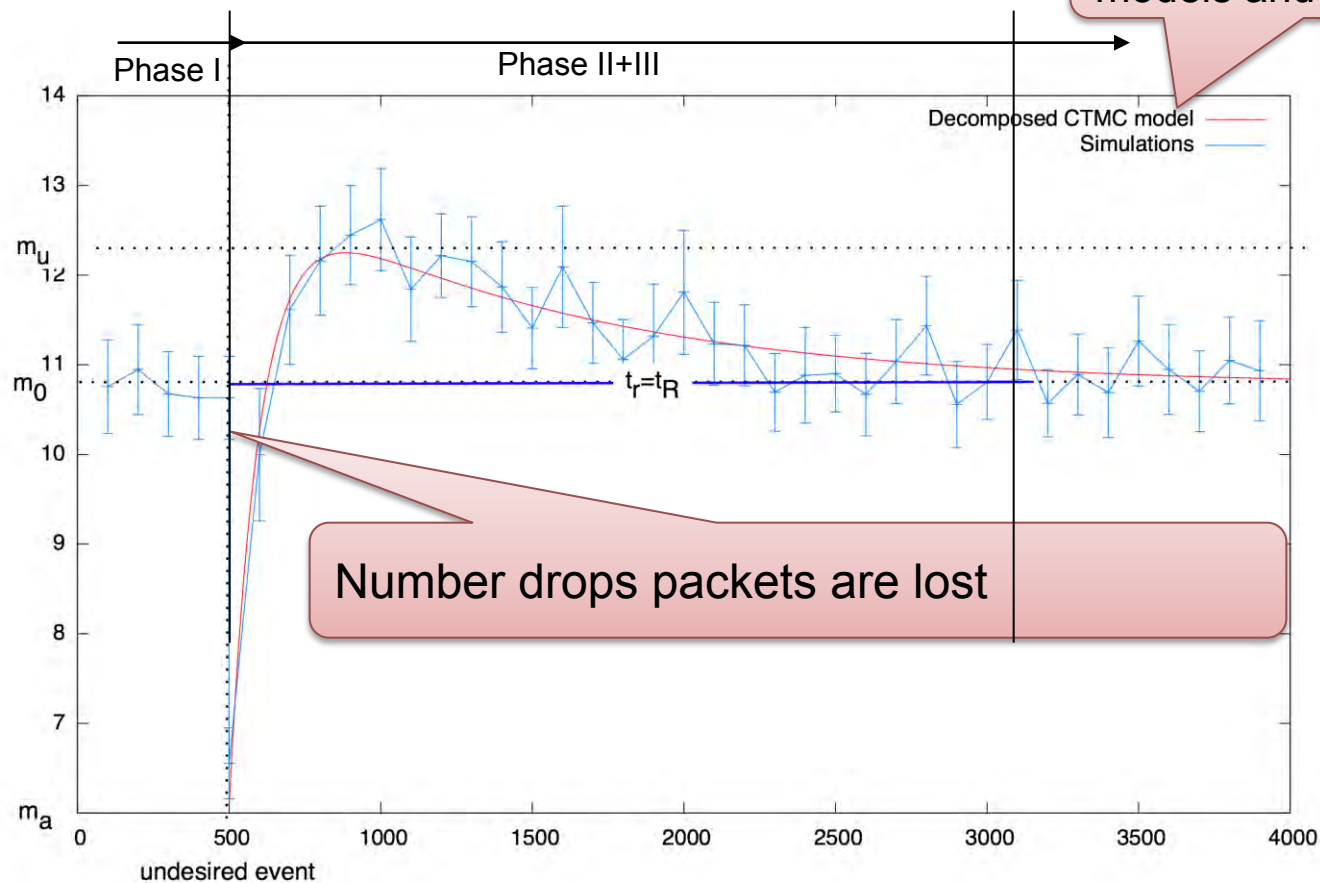
- When arrival and service rates are “significantly” higher than rerouting and failure rates (recall John Meyer’s Performability models)
- This means when the state of the performance model at state changes in the dependability model does not have a significant impact on the transient behavior



# Numerical example: average number in system



Compares decomposed models and simulations



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# Modeling assumptions

- External packet arrivals are Poisson
- Packet service time distribution is assumed to be exponential
- Space decomposition assumes independent network nodes
- Each recovery phase has steady-state performance
- Phase time distribution in the recovery model is (for simplicity) assumed to be exponential





# Modeling scalability

- Complete composite model - SRN
  - Transient solution of model with  $N_{\text{node}} \times N_{\text{res}} \times N_{\text{phase}}$  states
- Space decomposed CTMC
  - Transient solution of  $N_{\text{node}}$  models with  $N_{\text{res}} \times N_{\text{phase}}$  states
- Time decomposed CTMC
  - Steady state solution of  $N_{\text{node}} \times N_{\text{phase}}$  models with  $N_{\text{res}}$  states
  - Transient solution of one model with  $N_{\text{phase}}$  states





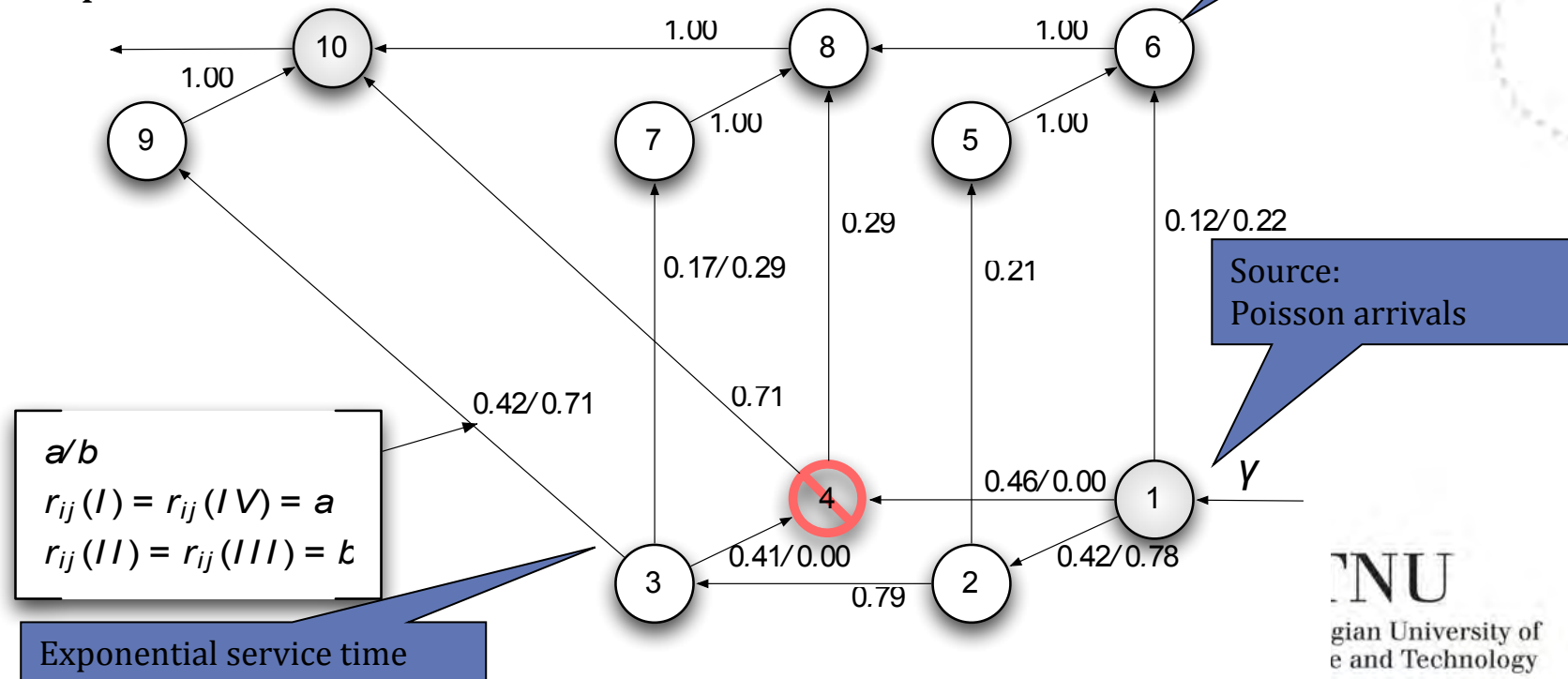
# Summary of real sized network application

- Complete composite CTMC
  - Identical assumptions as in the simulation model
  - State space explosion and transient solution is slow
- Space decomposed CTMC
  - Models of nodes are independent
  - High accuracy when performance is dominated by failed node and its neighborhood
  - Reduced state space but transient solution is still rather slow
- Time composed CTMC
  - Approximation is very good with orders of magnitude different rates
  - Significantly reduces computation time because transient model is reduced



## Illustrative example 2: Network with 10 nodes

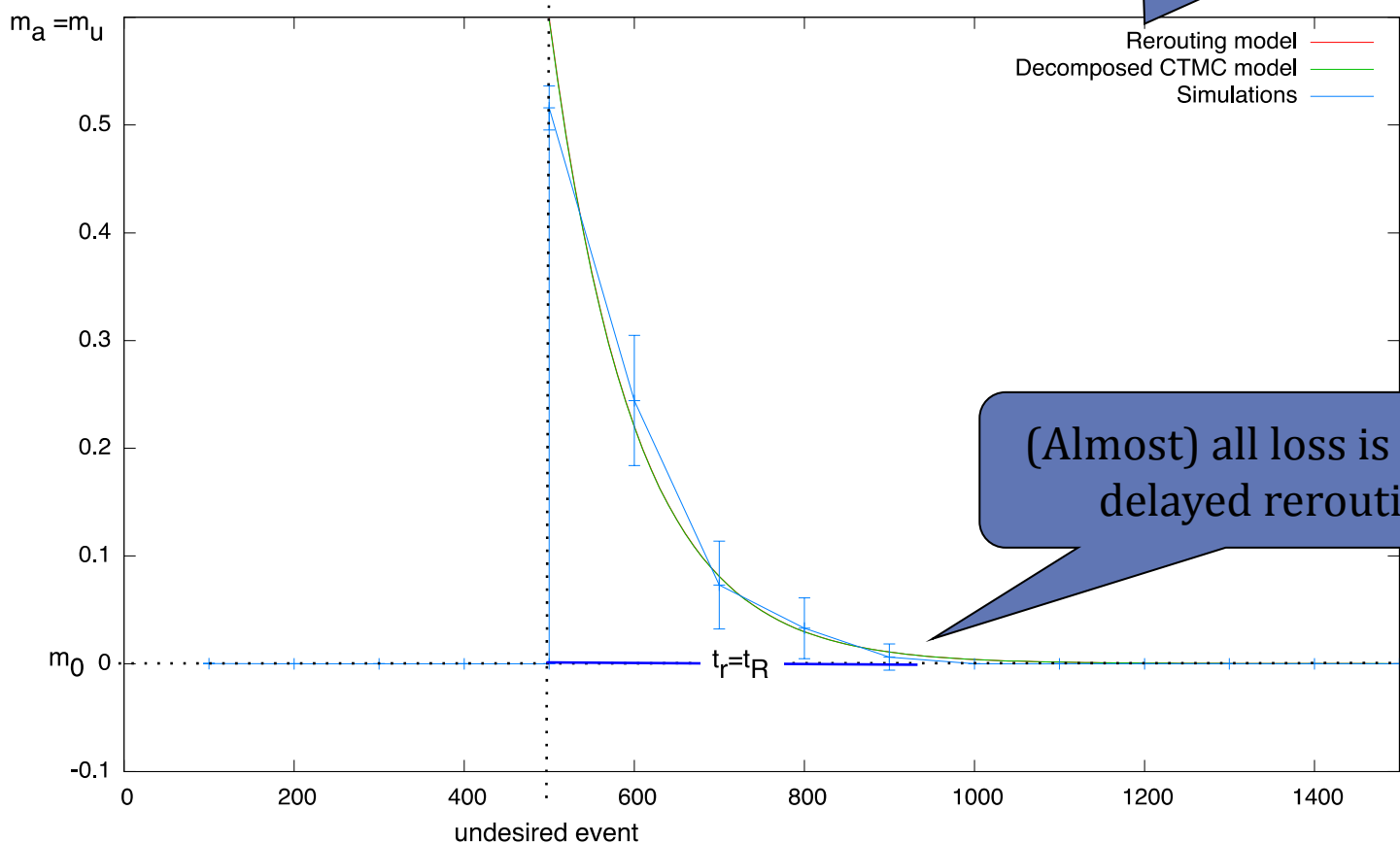
- Simulation model
- Closed form solution
- Comparisons





# Network 10 nodes: loss delay

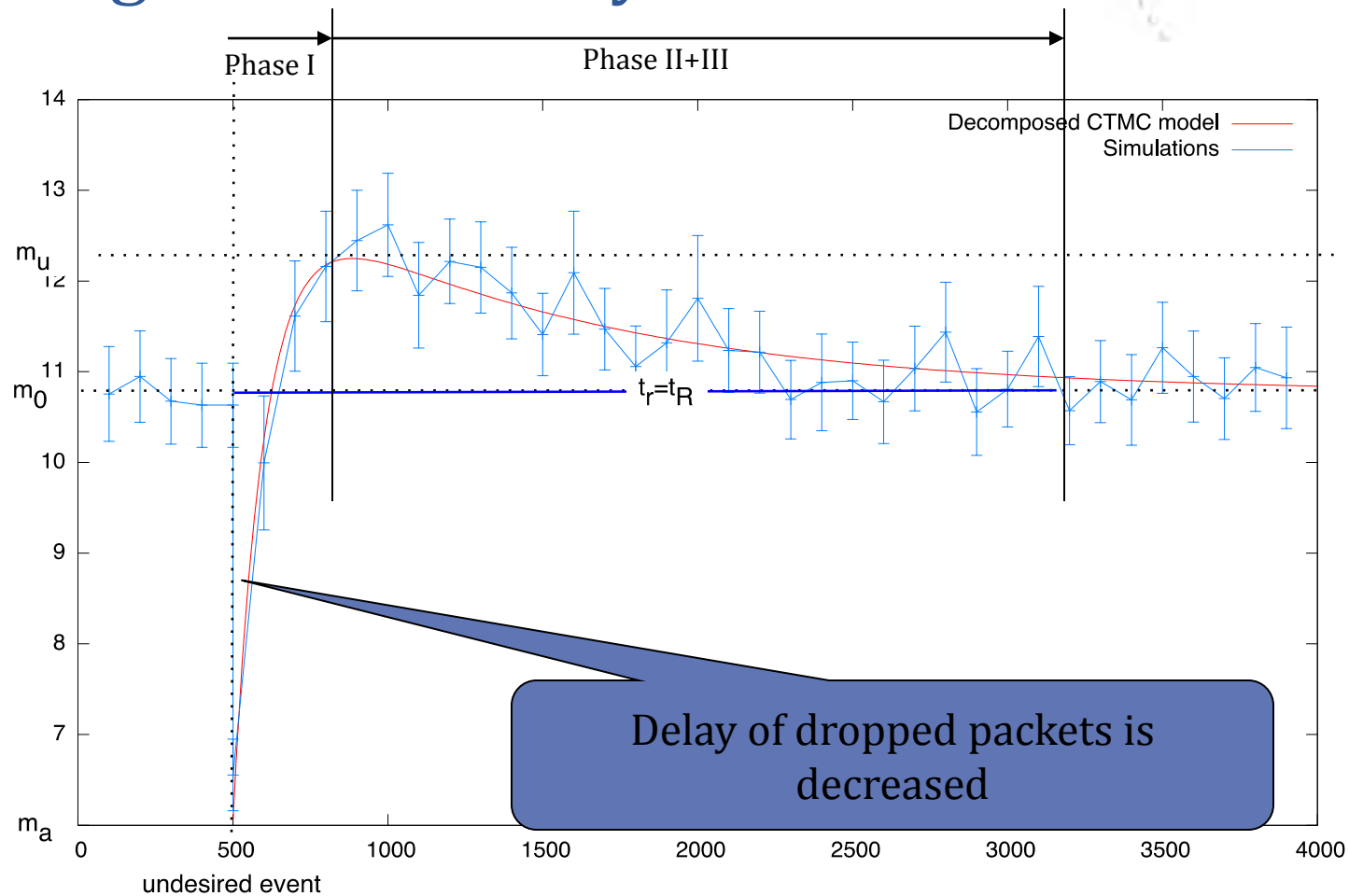
Rerouting model is  
 $F(t) = p^* \exp(-t \alpha_D)$



(Almost) all loss is due to delayed rerouting



# Network 10 nodes: average number in system



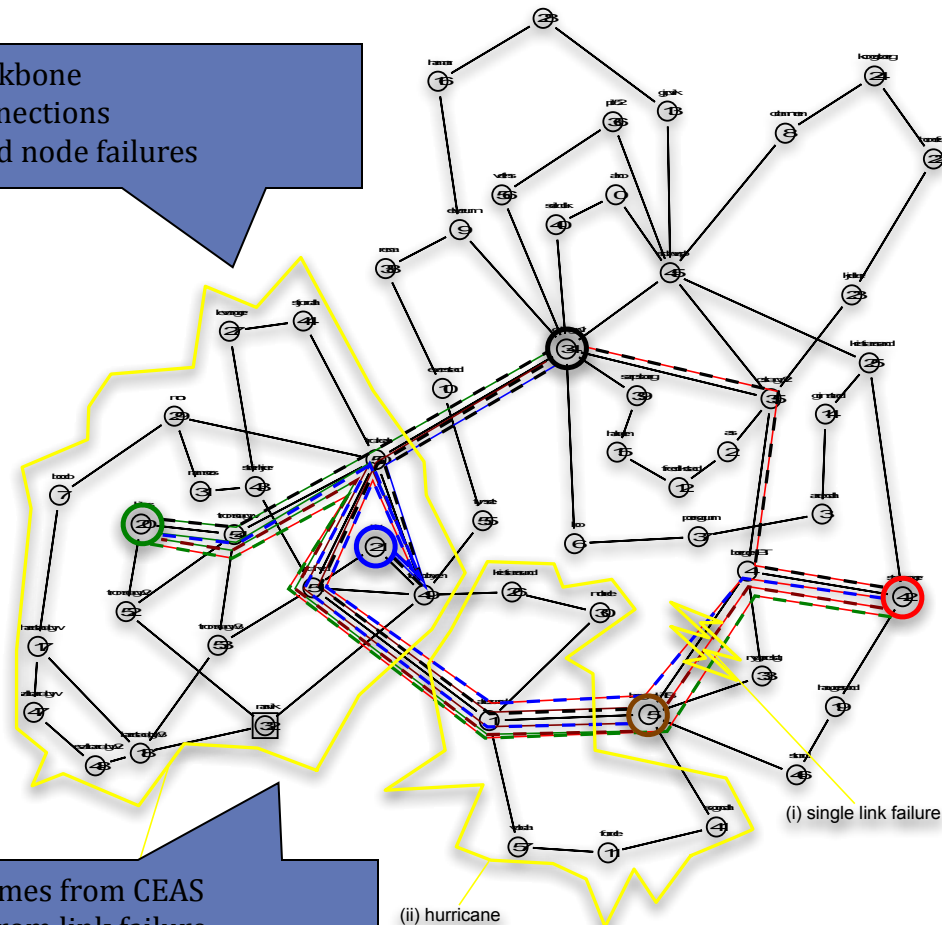


# Summary of observations

- SRN with complete CTMC
  - Identical to simulation model
  - State space explosion and transient solution is slow
- Node independent CTMC
  - Breaks dependence between nodes
  - Close to complete model when performance is dominated by failed node and its neighborhood
  - Reduced state space but transient solution is still rather slow
- Node independent and product form approximation CTMC
  - Approximation is very good with orders of magnitude different rates
  - Significantly reduces computation because transient model is reduced

# Network with 58 nodes

Uninett IP backbone  
20 virtual connections  
Severe link and node failures



Routing schemes from CEAS  
Five phases from link failure





# Network with 58 nodes

- Each phase has a routing scheme
- Determine (steady state) performance for each phase
  - Jacksson Network
  - Determine loss: only on failure before rerouting
  - Determine delay: approximate model
- Assume change from phase to phase will instantaneously change performance model
- Transient model for phase changes
- Combine transient phase and steady state performance solutions
- Compare analytic vs. simulation

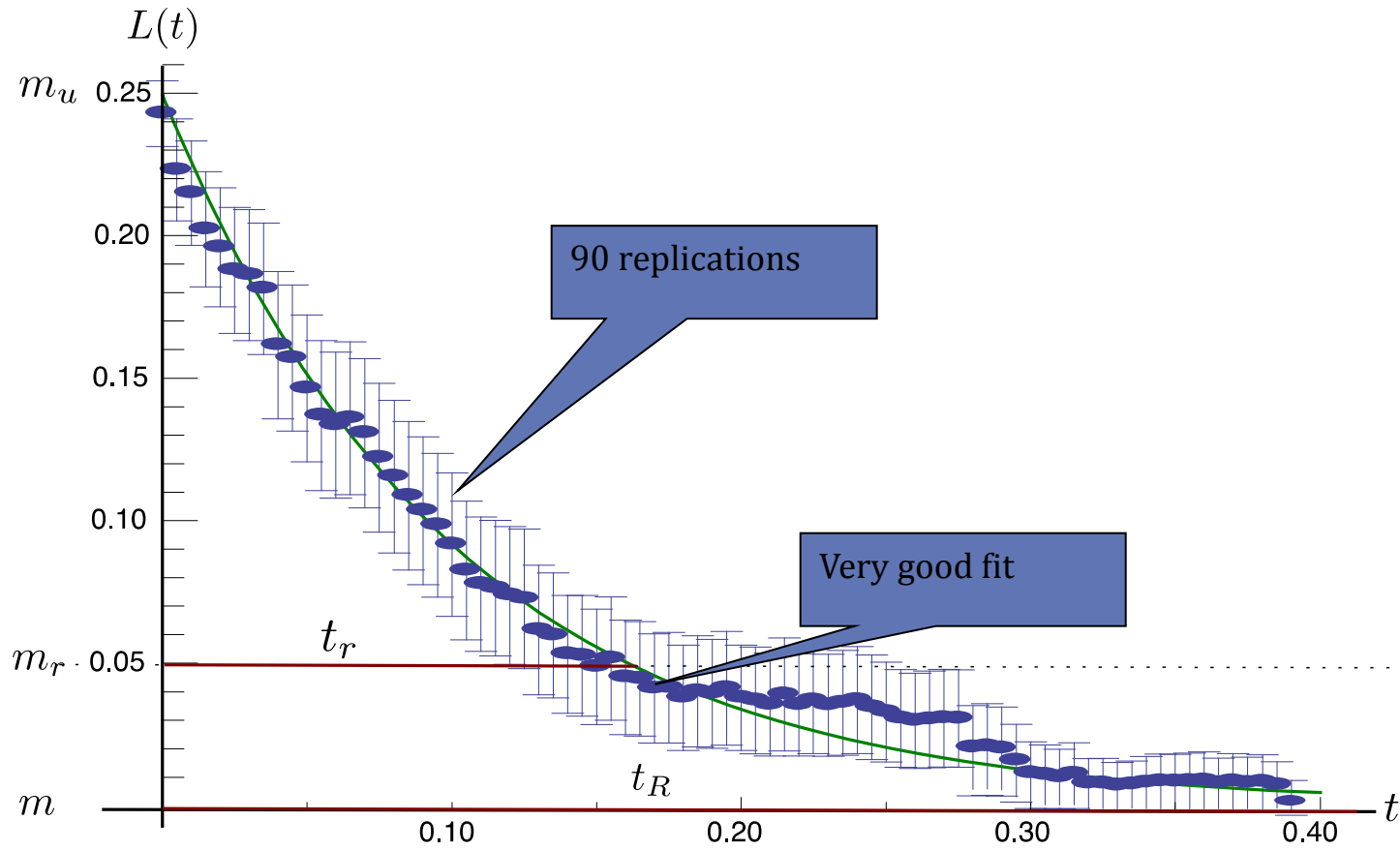


# Network with 58 nodes

- Assumptions
  - Infinite buffers
  - (Semi) Markov properties
  - Significant difference between activities in performance and availability models allows immediate shift in performance
  - Product form solution enables much more details in the availability model, such as multiple failure modes and failure types



# Network with 58 nodes: loss ratio

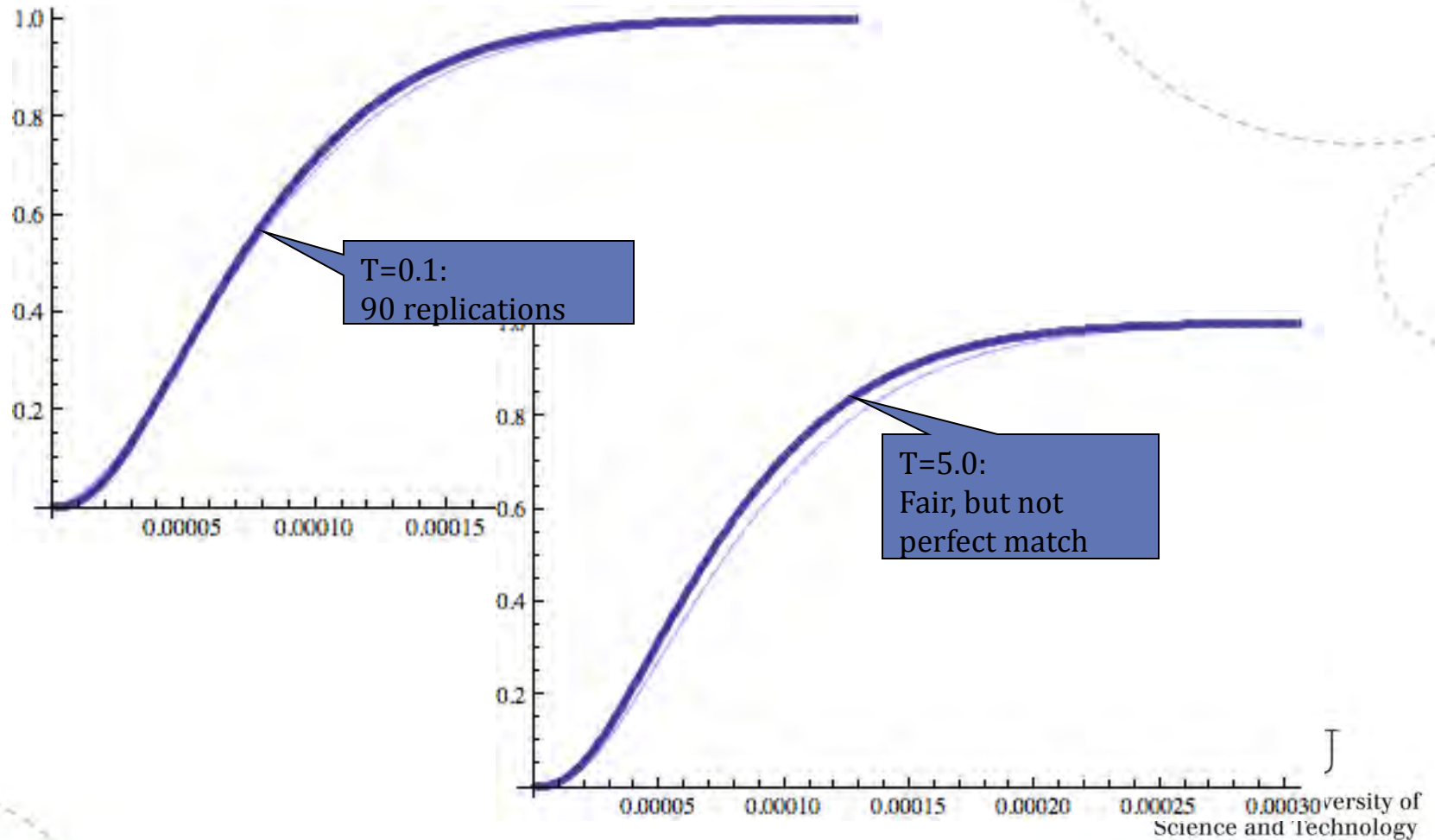


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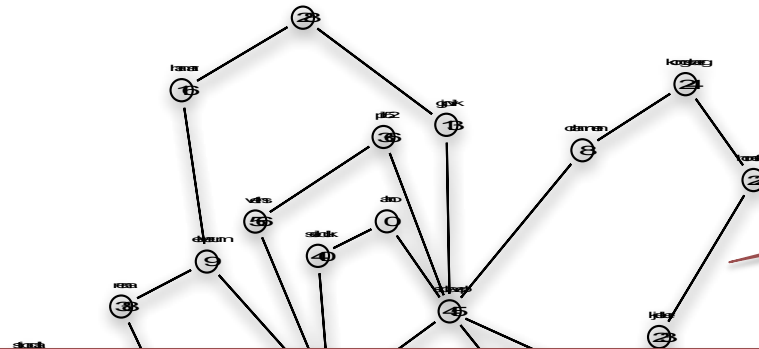
# Network with 58 nodes: delay distribution



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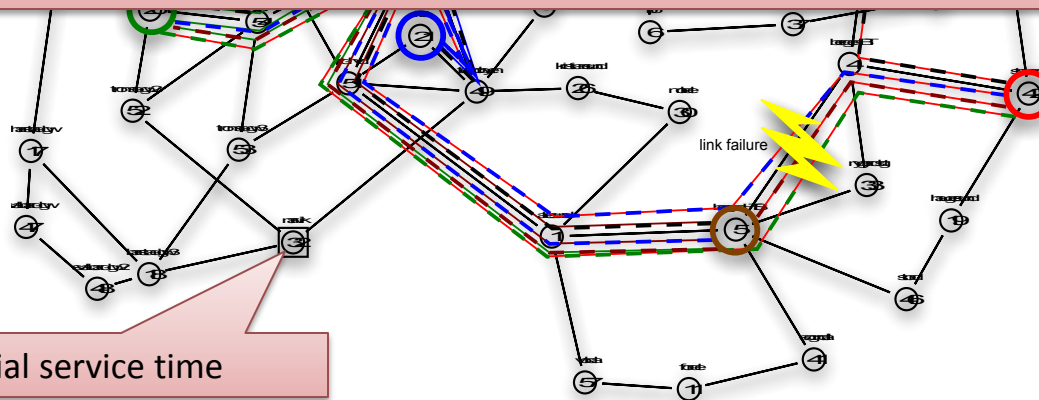


# Objectives and target system



58 nodes

- Transient performance in networks with virtual connections
- From occurrence of an undesired event until steady state operation is restored
- **Goal:** Survivability model of performance after network failure(s)

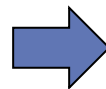
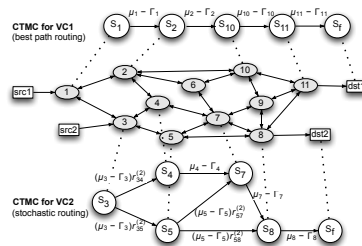
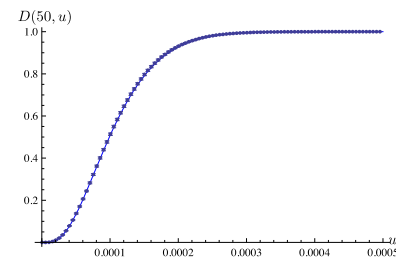
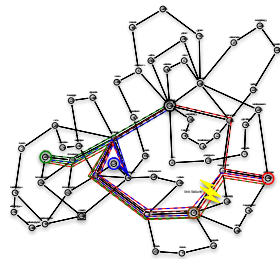


Source:  
Poisson arrivals

Exponential service time

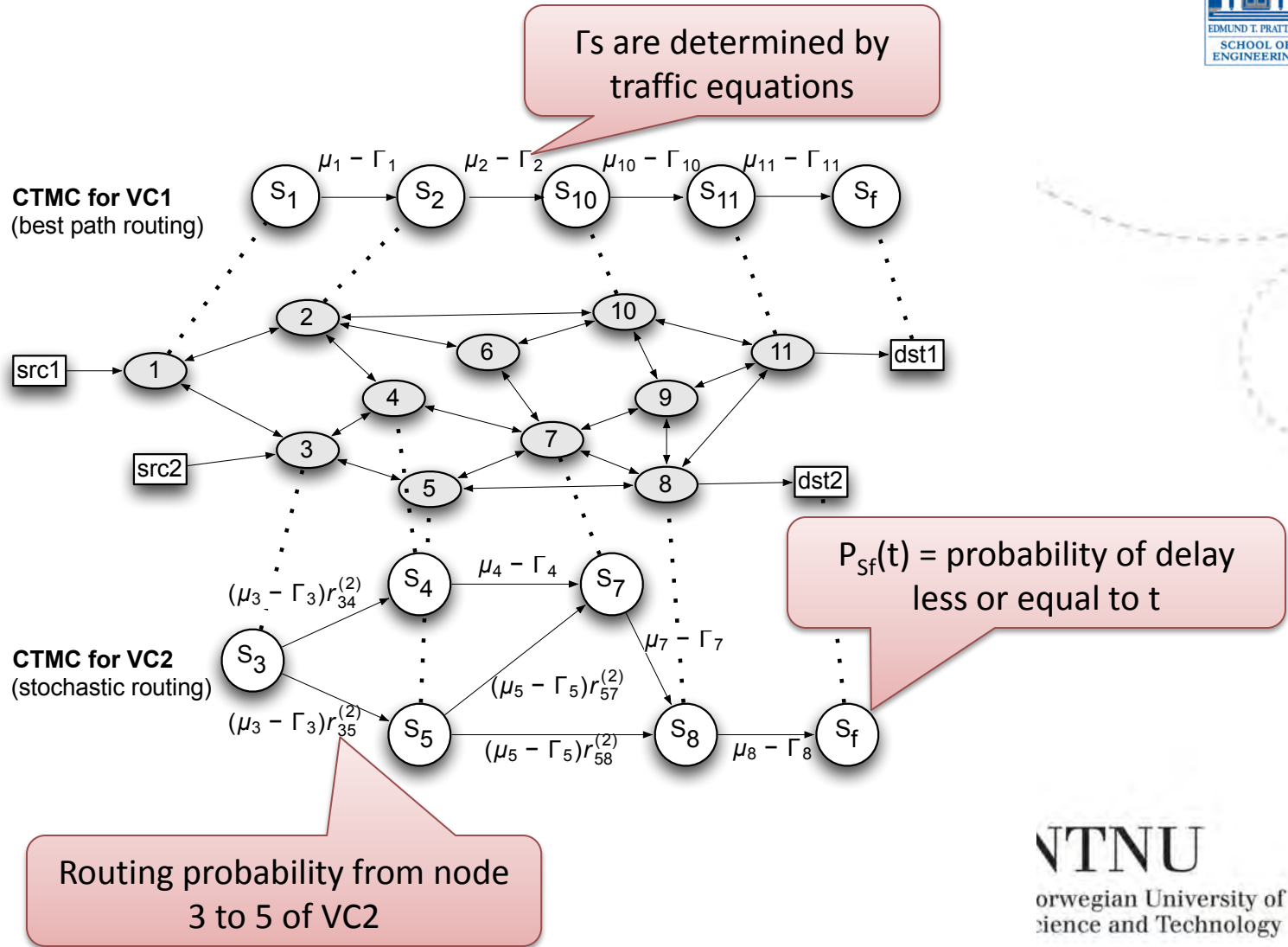
# Modeling approach

- Response time blocks for delay distributions
- Space-time decomposition to reduce models
- Time samples to model routing protocol behavior





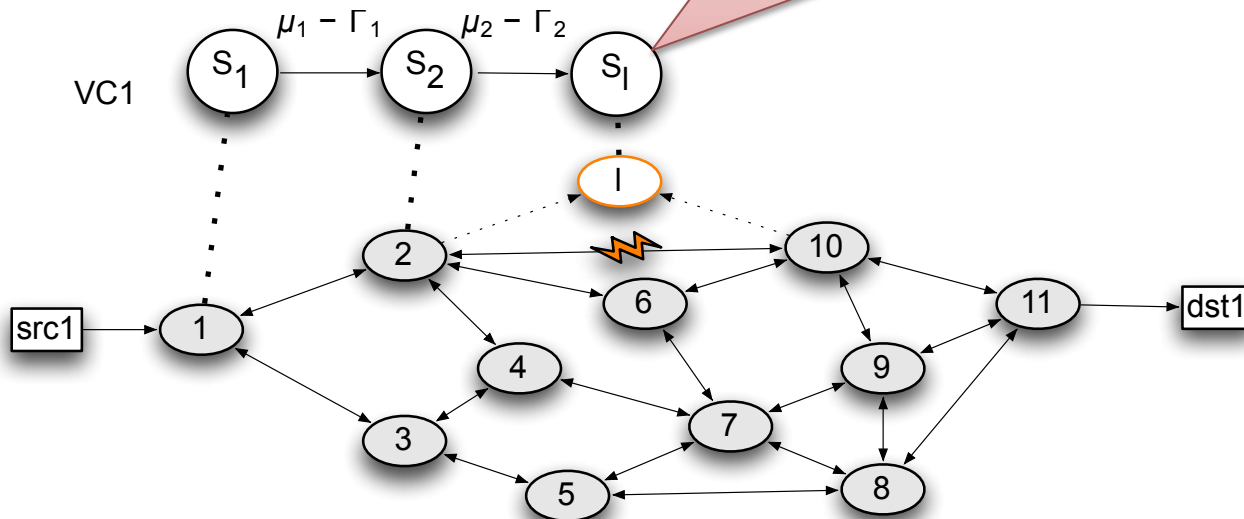
# Resq



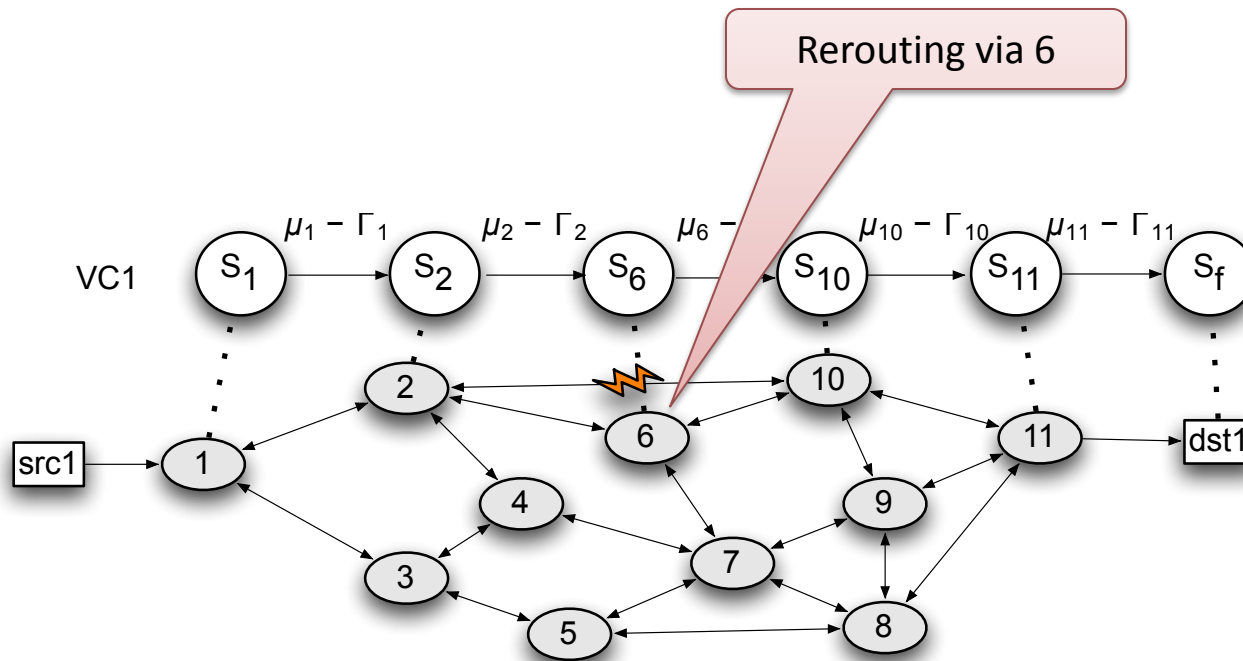


# Response time blocks –link down

All traffic lost until rerouting takes effect,  $P_{sf}(t) = 0$



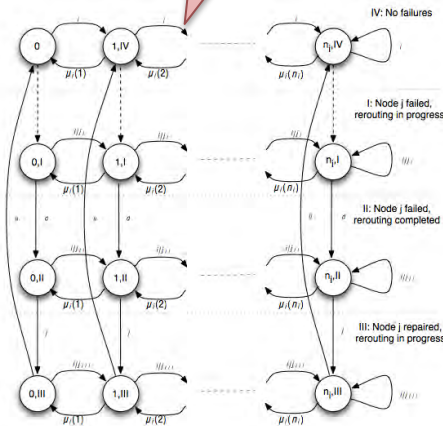
# Response time blocks – rerouting



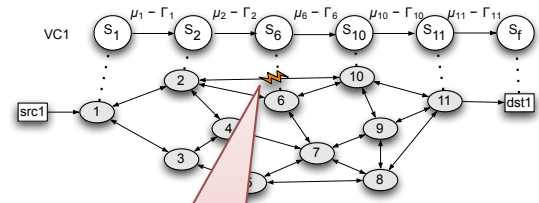


# Space-time decomposition

State space explosion!



Each phase (routing time sample) reaches stable state

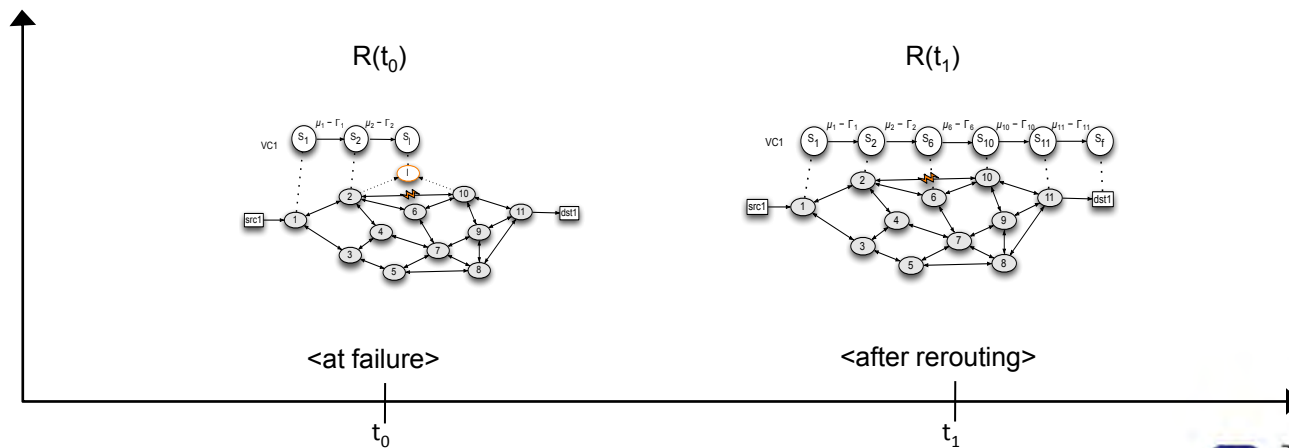


Traffic to each node treated independently



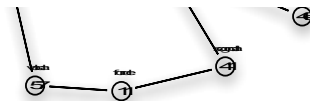
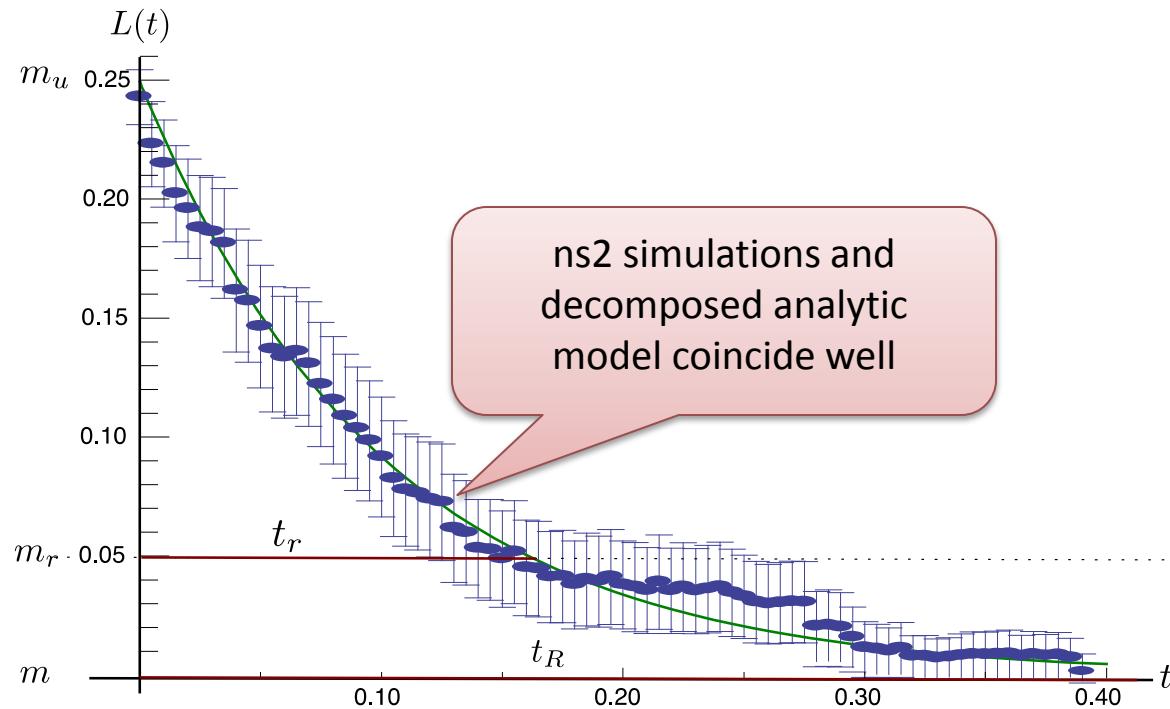
# Phased recovery model

- Sample routing probabilities at different phases
  - Simulations in ns-2 (this paper)
  - Routing table dumps from routers
- Routing probability matrix,  $R(t) = \{r_{ij}^{(vc)}(t)\}$



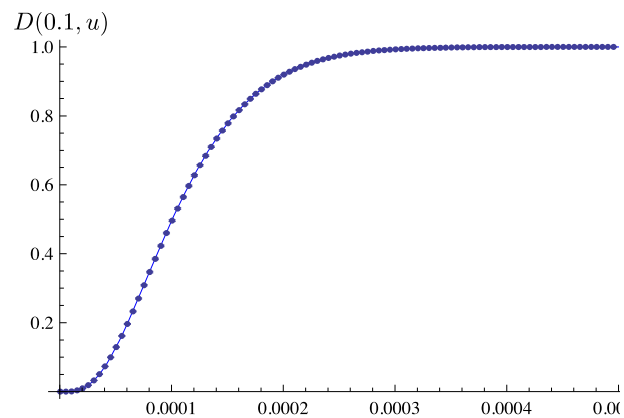


# Numerical example: packet loss probability

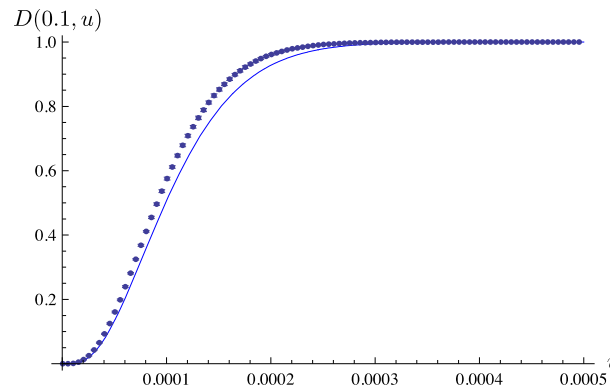




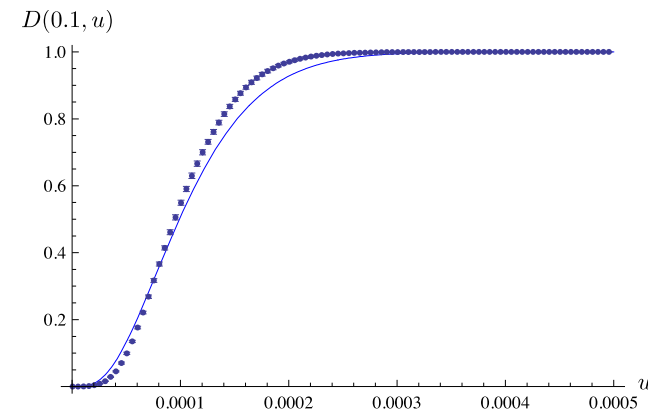
# Numerical example: delay distribution



All exponential



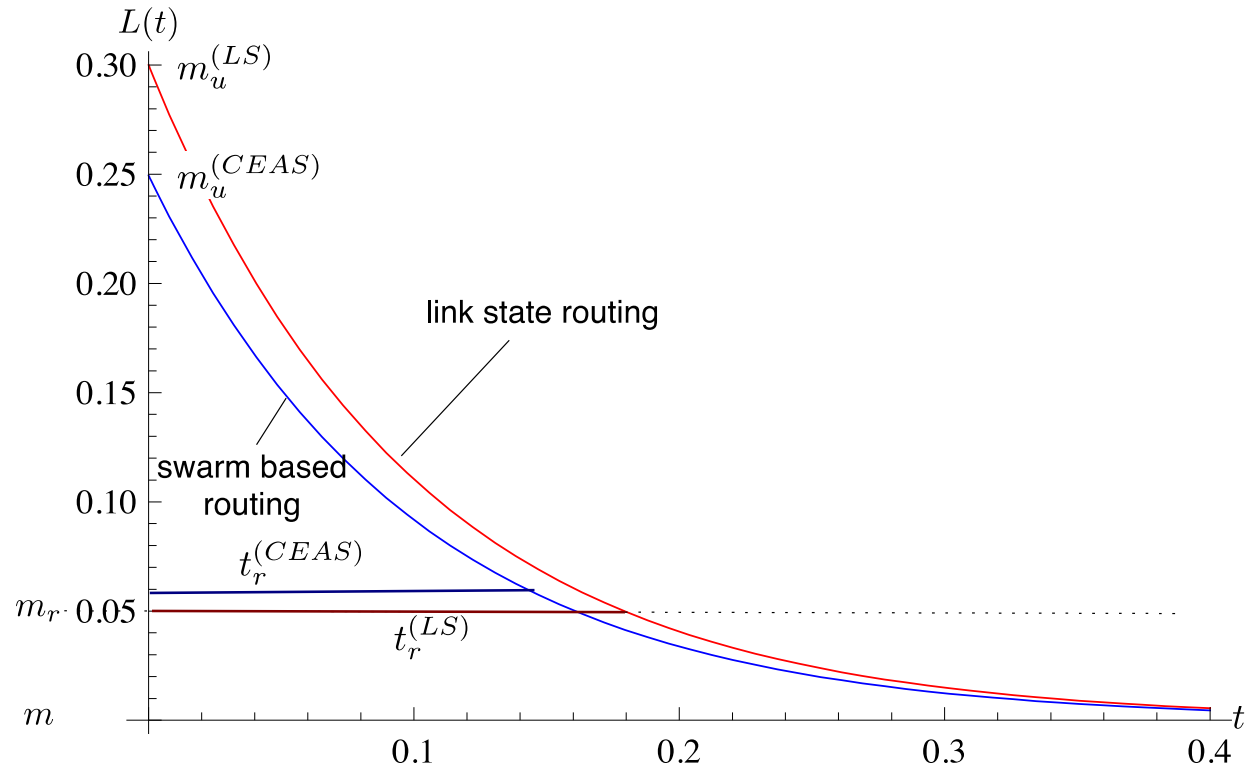
Pareto service times



Pareto arrival times



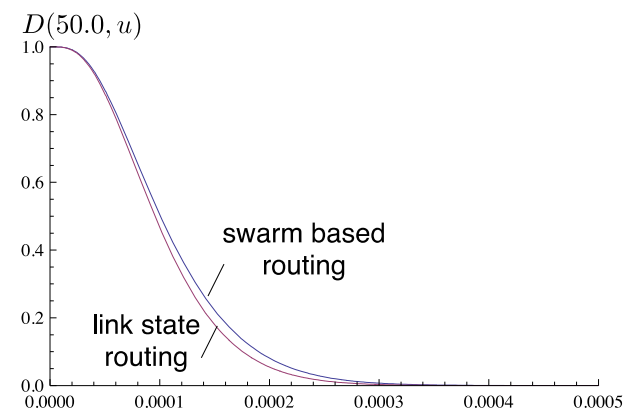
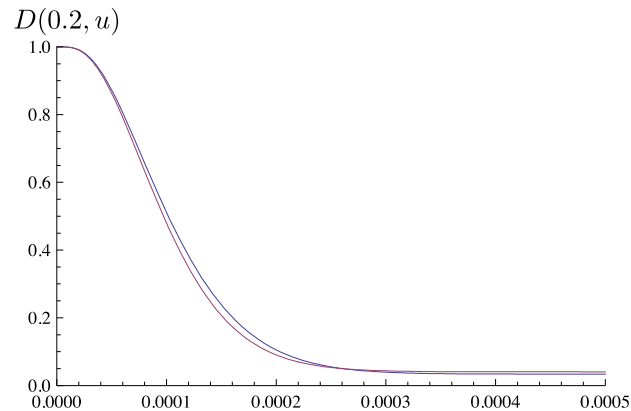
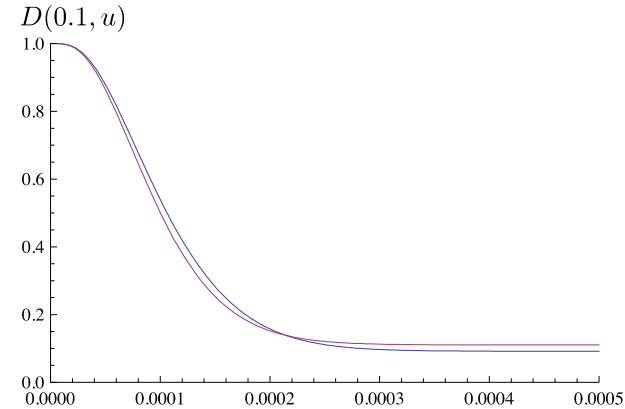
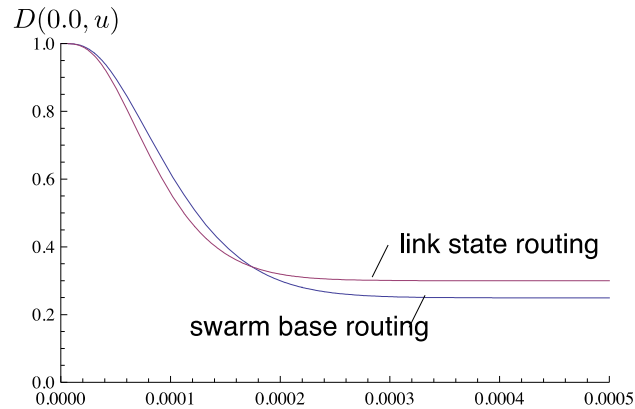
# Numerical example: packet loss probability







# Numerical example: delay distribution





# Closing remarks

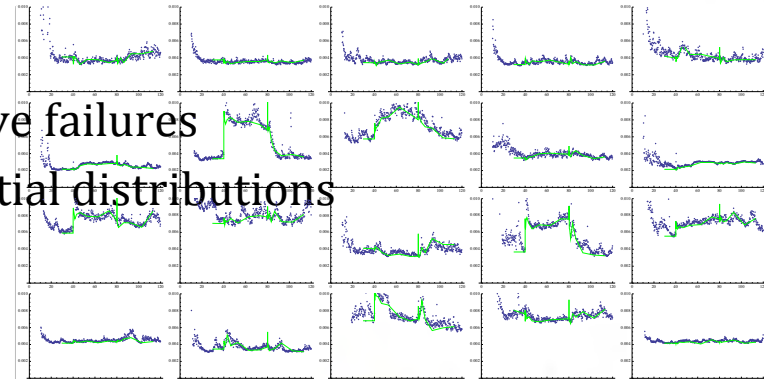
- Choose an appropriate definition of survivability
- Established a general analytical modeling approach for survivability quantification
- Extended the work to wireless cellular networks
- For complex systems
  - Rough assumption provide significant simplifications, or
  - Simulative (rather than analytic) solution
- Network models
  - State space explosion
  - Significant simplifications in analytic models
  - Realistic simulation models
  - Compare survivability quantifications



# Closing remarks



- In summary
  - Survivability in networks under failures
  - Time-decomposed model approach for large networks
  - Delay distribution of virtual connections
  - Very good correspondence with simulation results
- Current and planned work
  - Large scale networks exposed to extensive failures
  - Semi-Markov approach for non-Exponential distributions
  - Validate and relax assumptions





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